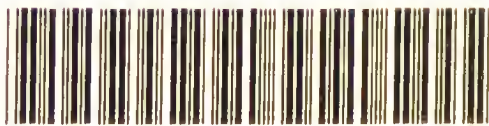


CHEMISTRY



W. Godfrey Seaton.



22101674602

Med  
K1884



Digitized by the Internet Archive  
in 2016

<https://archive.org/details/b28089649>

A SERIES OF  
CHEMICAL PROBLEMS



A SERIES OF  
(CHEMICAL PROBLEMS

With Key

*FOR USE IN COLLEGES AND SCHOOLS*

T. E. THORPE, LL.D., F.R.S.

REVISED AND ENLARGED BY

W. TATE, ASSOC. N.S.S. (HONOURS), F.C.S.

*(Professor in the Civil Engineering College, Calcutta)*

WITH A PREFACE

BY SIR H. E. ROSCOE, LL.D., F.R.S.

London

MACMILLAN AND CO., LIMITED

NEW YORK: THE MACMILLAN COMPANY

1907

*All rights reserved*

10095

829134

RICHARD CLAY AND SONS, LIMITED,  
BREAD STREET HILL, E.C. , AND  
BUNGAY, SUFFOLK.

*Copies Received 1870-1874.*

*First Edition Printed for MACMILLAN & CO., 1874.*

*Reprinted 1876, 1877.*

*With Key 1878. Reprinted 1880, 1881, February and December 1882, 1885,  
April and December 1888, 1890.*

*New Edition 1891.*

*Reprinted 1892, 1897, 1907.*

|                               |     |
|-------------------------------|-----|
| WELLCOME INSTITUTE<br>LIBRARY |     |
| Coll.                         | wel |
| Call<br>No.                   | 81  |



## PREFACE

THE following complete series of Questions and Problems in Elementary Chemistry will prove a great boon to those engaged either in teaching or in learning the science. They were prepared by my friend DR. THORPE, with special reference to our junior classes in Owens College, in which my "Elementary Chemistry" is used; but they will of course also be available where any other modern text-book is employed.

My experience has led me to feel more and more strongly that by no method can accuracy in a knowledge of Chemistry be more surely secured than by attention to the working of well-selected problems, and Dr. Thorpe's thorough acquaintance with the wants of the student is a sufficient guarantee that this selection has been carefully made. I intend largely to use these Questions in my own classes, and I can confidently recommend them to all teachers and students of the science.

HENRY E. ROSCOE.

*Ox. 13, 1870.*



# TABLE OF CONTENTS

|   | PAGE |
|---|------|
| Metric System of Weights and Measures . . . . .   | 1    |
| Conversion of Thermometric Scales . . . . .   | 6    |
| Correction of Thermometer Readings . . . . .  | 8    |
| Correction of Barometer Readings . . . . .  | 10   |
| Gay Lussac's Law ; Boyle's Law ; Correction of the<br>Volumes of Gases for Temperature and Pressure ; Law<br>of Partial Pressures . . . . .   | 13   |
| Relative Density of Solids, Liquids, and Gases ; Vapour<br>Density . . . . .  | 17   |
| Avogadro's Hypothesis ; Density and Molecular Weight ;<br>Valency, Equivalents, and Atomic Weights . . . . .  | 33   |
| Deduction of Empirical Formula from Percentage Compo-<br>sition. Formulæ of Minerals . . . . .  | 36   |
| To Calculate the Percentage Composition of a Compound<br>from its Formula . . . . .   | 42   |
| Chemical Equations ; to Calculate the Amount of Material<br>Required to Produce a Given Weight of any Substance,<br>or the Quantity of the Substance Produced by the De-<br>composition of a known Weight of the Material . . . . . | 44   |
| Combination and Decomposition of Gaseous Bodies . . . . .   | 52   |
| Gas Analysis Calculations . . . . .   | 54   |
| Calculation of the Results of Atomic Weight Determina-<br>tions . . . . .   | 67   |
| Calculations Involved in Indirect Analysis . . . . .  | 70   |
| General Analytical Questions . . . . .  | 74   |

|   | PAGE |
|---|------|
| Solution of Gases in Liquids . . . . .  | 78   |
| Solubility of Solids in Liquids ; Molecular Weight and the<br>Lowering of the Freezing-Point of Solutions . . . . . | 82   |
| Exercises on the Specific Heat, Latent Heat, and Atomic<br>Heat of Substances . . . . .                             | 86   |
| Heat of Solution ; Heat of Combination ; Calorific Power<br>and Calorific Intensity . . . . .                       | 91   |

## APPENDIX.

|  |     |
|--|-----|
| Table I.—Atomic Weights and Symbols of the Elements . . . . .  | 97  |
| Table II.—Weight of One Cubic Centimetre of Atmospheric Air at Different Temperatures from 0° to 300°,<br>at 760 mm. Pressure . . . . .  | 99  |
| Table III.—The Weight of 1000 c.c. of Water at t°C.,<br>when Determined by Means of Brass Weights in Air of<br>0°C., and at a Tension 0.76 m., is equal to 1000-x<br>grams . . . . . | 100 |
| Table IV.—Volume and Density of Water at Different<br>Temperatures . . . . .   | 101 |
| Table V.—For the Calculation of $\frac{1}{1 + 0.00367 \cdot T}$ . . . . .  | 102 |
| Table VI.—Vapour Pressure (Tension) of Water . . . . .   | 103 |
| Table VII.—For the Conversion of Degrees (T°) of a<br>Mercurial Thermometer into the Corresponding Values<br>of an Air Thermometer . . . . .   | 104 |
| Table VIII.—Table for Correction of Thermometer Read-<br>ings . . . . .  | 105 |
| Table IX.—Table of Useful Constants . . . . .  | 106 |
| Table X.—Logarithms and Anti-Logarithms . . . . .  | 107 |
| KEY TO CHEMICAL PROBLEMS . . . . .   | 117 |

# CHEMICAL CALCULATIONS.

## METRIC SYSTEM OF WEIGHTS AND MEASURES.

### MEASURES OF LENGTH.

Standard :—1 metre, the length at  $0^{\circ}\text{C.}$  of a platinum bar preserved in Paris. Originally constructed to represent the  $\frac{1}{40000000}$  part of the earth's circumference, measured along the Paris meridian ; according to modern measurements it does not fulfil this intention and can therefore only be viewed as an empirical standard.

|                        |       |                       |
|------------------------|-------|-----------------------|
| 10 decimetres (dcm.)   | . . . | 1 metre (m.).         |
| 100 centimetres (cm.)  | . . . | "                     |
| 1000 millimetres (mm.) | . . . | "                     |
| 1000 metres            | . . . | 1 kilometre.          |
| 1 inch                 | =     | 2·539954 centimetres. |
| 1 foot                 | =     | 3·047945 decimetres.  |
| 1 yard                 | =     | 0·914383 metre.       |
| 1 mile                 | =     | 1·609315 kilometres.  |

### MEASURES OF SURFACE.

|                                   |   |
|-----------------------------------|---|
| 100 square decimetres (sq. dcm.)  | 1 square metre or<br>centiare (sq. m.). |
| 10,000 " centimetres (sq. cm.)    | "                                       |
| 1,000,000 " millimetres (sq. mm.) | "                                       |
| 100 square metres                 | . . . . 1 are.                          |
| 10,000 " "                        | . . . . 1 hectare.                      |
| 1 square inch                     | = 6·4513669 sq. cm.                     |
| 1 " foot                          | = 9·2899683 sq. dcm.                    |
| 1 " yard                          | = 0·83609715 sq. m.                     |
| 1 " acre                          | = 0·404671021 hectare.                  |

## MEASURES OF CAPACITY.

|                                     |                            |
|-------------------------------------|----------------------------|
| 1000 cubic decimetres (c.dcm.)      | 1 cubic metre<br>or stere. |
| 1,000,000 „ centimetres (c.c.)      | „                          |
| 1,000,000,000 „ millimetres (c.mm.) | „                          |
| 1 cubic decimetre . . .             | 1 litre.                   |
| 1 cubic inch = 16·386176 c.c.       |                            |
| 1 „ foot = 28·315312 c.dcm.         |                            |
| 1 gallon = 4·54345797 litres.       |                            |

## MEASURES OF WEIGHT.

Standard :—1 kilogram, the mass of a piece of platinum weighed *in vacuo*; preserved in Paris.

Theoretically the gram equals the mass of 1c.c. and the kilogram the mass of 1000 c.c. of distilled water at 4°C., at the latitude of Paris; the actual standard differs slightly from its value as thus defined.

|                               |            |
|-------------------------------|------------|
| 1000 grams (grms.) . . .      | 1 kilogram |
| 10,000 decigrams. . . .       | „          |
| 100,000 centigrams . . . .    | „          |
| 1,000 000 milligrams . . . .  | „          |
| 1 grain = 0·06479895 gram.    |            |
| 1 troy oz. = 31·103496 grms.  |            |
| 1 lb. avd. = 0·45359265 kilo. |            |
| 1 cwt. = 50·80237689 kilos.   |            |

*To reduce grams to grains.*

Log. grams + 1·188432 = log. grains.

*To reduce cubic centimetres to cubic inches.*

Log. c.c. + (-2·7855224) = log. cubic inches.

*To reduce millimetres to inches.*

Log. mm. + (-2·5951742) = log. inches.

*To convert grains into grams.*

Log. grains + (-2·8115680) = log. grams.

*To convert cubic inches into cubic centimetres.*

Log. cb. in. + 1·2144776 = log. c.c.

*To convert inches into millimetres.*

Log. inches + 1·4048258 = log. mm.

## SURFACES AND CAPACITIES.

Area of a square = side<sup>2</sup>.

Area of a rectangle, rhombus, or rhomboid = side  $\times$  perpendicular height.

Area of a triangle = half the side  $\times$  perpendicular height.

Area of a circle =  $3\cdot141593 \times \text{radius}^2$ .

Area of an ellipse =  $3\cdot141593 \times \text{major semi-axis} \times \text{minor semi-axis}$ .

Surface of a cube =  $6 \times \text{edge}^2$ .

Surface of a sphere =  $12\cdot566370 \times \text{radius}^2$ .

Surface of a cylinder =  $6\cdot283185 \times \text{radius of base} \times \text{sum of height and radius of base}$ .

Surface of a spherical segment =  $6\cdot283185 \times \text{height} \times \text{radius of circular base}$ .

Volume of a cube =  $\text{edge}^3$ .

Volume of a sphere =  $\frac{4}{3} \times 3\cdot141593 \times \text{radius}^3$ .

Volume of a cylinder =  $3\cdot141593 \times \text{height} \times \text{radius}^2$ .

Volume of a prism =  $\text{base area} \times \text{height}$ .

Volume of a cone or pyramid =  $\frac{1}{3} \times \text{base area} \times \text{height}$ .

## EXAMPLES.

1. How many millimetres are contained in 5 metres?  
From the table we find that 1000 millimetres = 1 metre.

$\therefore$  5 metres =  $1000 \times 5$ , or 5000 millimetres.

2. How many decimetres are equivalent to 106725 millimetres?

1 decimetre = 100 millimetres.

$\therefore$  106725 millimetres = 106725 decimetres.

3. How many litres of air are contained in a room measuring  $4 \times 3 \times 2$  metres?

$4 \times 3 \times 2 = 24$  cubic metres.

1 cubic metre = 1000 litres.

$\therefore$   $1000 \times 24 = 24,000$  litres.

4. Required the number of milligrams in 15 c.c. of water measured at  $4^\circ \text{C}$ .

1 c.c. of water at  $4^\circ \text{C}$ . = 1 gram.

1000 milligrams = 1 gram.

$\therefore$   $15 \times 1000 = 15,000$  milligrams.

## QUESTIONS.

1. How many millimetres, centimetres, and decimetres are respectively contained in 0·437 of a decimetre?

2. Required the number of (*a*) centimetres, (*b*) decimetres, (*c*) metres, in 1098765421 millimetres.

3. Required the number of square millimetres, square centimetres, square decimetres contained in the top of a table measuring 1 metre by 70 centimetres.

4. Define the gram and the litre. How many grams are contained in 1·725 kilograms?

5. How many centigrams are contained in 2·567 kilograms?

6. Required the number of milligrams contained in 5 cubic centimetres of water measured at 4°C.

7. Calculate the number of square centimetres contained on the surface of a paper filter possessing a radius of 5 centimetres.

8. In an English inch are contained 25·3995 millimetres. How many kilometres are there in a mile?

9. The mean height of the barometer in the latitude of Greenwich at the level of the sea is 30 inches. How many millimetres is this equivalent to?

10. A gallon is equal to 4·543 litres. How many cubic centimetres are contained in one pint?

11. A spherical glass bulb possesses a radius of 3 centimetres; calculate its capacity.

12. Calculate the length of the polar axis on the supposition that the earth is spherical, and that the actual metre is identical with the metre as defined.

13. A fine wire 255 millimetres in length weighs 0·172 grams. What length of such wire would it take to make a centigram 'rider'?



14. A piece of platinum foil measuring 10.5 centimetres by 1.5 centimetres weighs 0.723 gram. Into how many pieces, each weighing one decigram, may it be divided?

15. A piece of Swedish filter paper measuring 60 centimetres square, leaves on burning 0.1062 gram of ash. Calculate the amount of ash left on burning filters possessing the following radii: (a) 3 centimetres, (b) 4 centimetres, (c) 5 centimetres, (d) 6 centimetres, (e) 8 centimetres, (f) 10 centimetres.

16. A perfectly cylindrical tube 90 millimetres in length holds exactly one gram of water at  $4^{\circ}$  C. Calculate its internal diameter.

17. I require a perfectly spherical bulb to hold 300 cubic centimetres. What internal diameter must it have?

18. A cylindrical graduated tube 15 millimetres in diameter holds 25 cb. centimetres up to the hundredth division. Calculate the value in grams of water at  $4^{\circ}$  C. of one division. What will be the length between each division?

19. A flask, nominally of 1 litre capacity, is found to contain 997 grams of distilled water at  $15^{\circ}$  C., when the lowest point of the meniscus coincides with the graduation mark; (see table III) by how much do its contents fall short of their supposed value?

20. A 50 c.c. pipette delivers 50 grams of water at  $16^{\circ}$  C.; what is the true volume of the space up to the graduation mark?

21. In the verification of a Mohr's burette successive volumes of 10 c.c.'s of water, at  $15^{\circ}$  C., weighed 9.94 gm., 9.99 gm., 10.06 gm., 10.13 gm., 10.19 gm. What corrections should be applied to obtain the volumes delivered from the zero-mark to the 20, 40, and 50 c.c. marks respectively?

## CONVERSION OF THERMOMETRIC SCALES.

(C. Centigrade ; F. Fahrenheit ; R. Reaumur.)

|                          |                                 |                |
|--------------------------|---------------------------------|----------------|
| Fahrenheit to Centigrade | $\frac{5}{9} (F.^{\circ} - 32)$ | $= C.^{\circ}$ |
| Centigrade to Fahrenheit | $\frac{9}{5} C.^{\circ} + 32$   | $= F.^{\circ}$ |
| Reaumur to Fahrenheit    | $\frac{9}{4} R.^{\circ} + 32$   | $= F.^{\circ}$ |
| Fahrenheit to Reaumur    | $\frac{4}{9} (F.^{\circ} - 32)$ | $= R.^{\circ}$ |
| Centigrade to Reaumur    | $\frac{4}{5} C.^{\circ}$        | $= R.^{\circ}$ |
| Reaumur to Centigrade    | $\frac{5}{4} R.^{\circ}$        | $= C.^{\circ}$ |

## EXAMPLES.

1. What temperature on the Centigrade scale is equal to  $212^{\circ} F.$ ?

$$212 - 32 = 180$$

$$\frac{180 \times 5}{9} = \frac{900}{9} = 100^{\circ}$$

*Ans.*  $= 100^{\circ} C.$

2. What temperature on the Centigrade scale is equal to  $0^{\circ} F.$ ?

$$0 - 32 = - 32$$

$$\frac{32 \times 5}{9} = \frac{160}{9} = 17.77 C$$

3. Express  $60^{\circ} C.$  on Fahrenheit's scale.

$$\frac{60 \times 9}{5} = \frac{540}{5} = 108$$

*Ans.*  $108 + 32 = 140^{\circ} F.$

4. Express  $- 15 C.$  on Fahrenheit's scale.

$$\frac{- 15 \times 9}{5} = \frac{- 135}{5} = - 27$$

*Ans.*  $- 27 + 32 = + 5 F.$

## QUESTIONS.

22. Express the following temperatures in  $^{\circ}\text{C}$ .

|                        |                                |                               |
|------------------------|--------------------------------|-------------------------------|
| $60^{\circ}\text{ F.}$ | $0^{\circ}\text{ R.}$          | $-10^{\circ}\text{ R.}$       |
| $80^{\circ}\text{ R.}$ | $-15^{\circ}\cdot 5\text{ F.}$ | $25^{\circ}\cdot 5\text{ R.}$ |
| $0^{\circ}\text{ F.}$  | $500^{\circ}\text{ F.}$        | $0^{\circ}\cdot 2\text{ F.}$  |

23. Express the following temperatures in  $^{\circ}\text{R}$ .

|                               |                          |                               |
|-------------------------------|--------------------------|-------------------------------|
| $15^{\circ}\cdot 5\text{ C.}$ | $1200^{\circ}\text{ F.}$ | $0^{\circ}\cdot 25\text{ C.}$ |
| $60^{\circ}\text{ F.}$        | $-40^{\circ}\text{ C.}$  | $0^{\circ}\cdot 0\text{ F.}$  |
| $32^{\circ}\text{ F.}$        | $240^{\circ}\text{ C.}$  | $15^{\circ}\cdot 0\text{ F.}$ |

24. Express the following temperatures in  $^{\circ}\text{F}$ .

|                               |                              |                              |
|-------------------------------|------------------------------|------------------------------|
| $4^{\circ}\cdot 0\text{ C.}$  | $12^{\circ}\text{ R.}$       | $212^{\circ}\text{ C.}$      |
| $15^{\circ}\cdot 5\text{ C.}$ | $0^{\circ}\cdot 1\text{ C.}$ | $360^{\circ}\text{ R.}$      |
| $60^{\circ}\text{ C.}$        | $80^{\circ}\text{ R.}$       | $1^{\circ}\cdot 0\text{ C.}$ |

25. Bromine boils at  $138^{\circ}\cdot 7\text{ F}$ . What is the corresponding temperature on the Centigrade scale?

26. Ether boils at  $34^{\circ}\cdot 9\text{ C}$ ., alcohol at  $78^{\circ}\cdot 4\text{ C}$ ., and sulphuric acid at  $338^{\circ}\text{ C}$ . What are the corresponding boiling-points on Fahrenheit's scale?

27. Mercury freezes at  $-38^{\circ}\cdot 8\text{ C}$ . and boils at  $357^{\circ}\cdot 25\text{ C}$ . Calculate the corresponding temperatures on the scales of Reaumur and Fahrenheit.

28. Cast-iron melts at  $1550^{\circ}\text{ C}$ ., zinc at  $423^{\circ}\text{ C}$ ., lead at  $327^{\circ}\text{ C}$ ., tin at  $235^{\circ}\text{ C}$ . Calculate these temperatures in  $^{\circ}\text{F}$ .

29. At what point are the numbers on the scales of Fahrenheit and Celsius identical? To what temperature does this point correspond on the scale of Reaumur?

## CORRECTION OF THERMOMETER READINGS.

Thermometer readings require, in general, to be corrected :

(1) For change in the zero-point.

(2) For the cooling of that portion of the thread not immersed in the heating medium (the emergent thread). For the most accurate work a correction is also applied for the want of uniformity of the bore of the capillary stem, generally by means of a table formed by calibration of the tube or by comparison of the individual thermometer with a standard instrument. Finally, the mercurial-thermometer readings, to be comparable, should all be reduced to air-thermometer readings by means of Table VII. (Appendix).

An approximate correction for the emergent thread may be obtained by means of the expression  $\delta (t - t')n$ , where  $\delta$  the co-efficient of apparent expansion of mercury in glass = '000154,  $t$  = the observed temperature on the thermometer,  $t'$  = the mean temperature of the cooled column as determined by an attached thermometer, and  $n$  = the length in degrees of the cooled column.

In ordinary cases  $\delta = '000143$  gives a result nearer the truth than the actual coefficient ; a useful table calculated by means of this constant is appended (Table VIII).\*

### EXAMPLES.

1. In the determination of the boiling-point of a sample of ethyl formate a thermometer is used indicating  $0^{\circ}8$  when plunged into melting ice. When the stem is entirely surrounded by vapour the reading taken is  $55^{\circ}$ . What is the corrected boiling-point?

\* Several other formulæ have been proposed to calculate the correction required, but neither these nor the one given above give the true correction in all cases ; for moderate values of  $n$  Table VIII. is fairly true if thermometers of the ordinary type are employed. See the article "Zur Korrektion der Thermometerablesungen für den herausragenden Faden," by Dr. E. Rimbach, in the *Zeitschrift für Instrumentenkunde*, May 1890.

The zero of this thermometer has risen  $0.8$ , hence all readings must be diminished by this amount and we have  $55 - 0.8 = 54.2$  BP required.

2. With a thermometer reading  $0.2$  in melting ice, the BP of propionic acid is indicated as  $139.2$ ; the column is immersed in the vapour to the  $70^\circ$  mark and the temperature of the exposed part is  $26^\circ$ ; what is the corrected BP? What is the corresponding H-thermometer temperature?

Correction for change of zero-point =  $-0.2$ .

Correction for cooled column =  $+1.13$  for  $n = 139.2 - 70 = 69.2$  ( $70$  nearly), and  $t - t' = 139.2 - 26 = 113.2$ , while from Table VIII. for  $n = 70$  and  $t - t' = 110$  and  $120$  the corrections are  $+1.10$  and  $+1.20$  respectively.

The required BP is therefore

$$139.2 - 0.2 + 1.13 = 140.13.$$

From Table VII.  $139.85^\circ$  mercury thermr. =  $140^\circ$  hydrogen thermr.; hence  $140.13 = (140 - 139.85)^\circ = 140.13 + 0.15 = 140.28$  is the corresponding hydrogen-thermometer temperature.

### QUESTIONS.

30. The indicated temperature of the vapour of boiling methyl acetate is  $57.9$  when the thermometer is immersed in the vapour to the  $100^\circ$  mark; the same instrument reads  $0.5$  in melting snow; what is the corrected boiling point?

31. During a fractionation of isobutyric acid 4 portions are collected (*a*) from  $149.5$  to  $150.3$  (*b*) from  $150.3$  to  $150.9$  (*c*) from  $150.9$  to  $151.1$  (*d*)  $151.1$  to  $151.5$  as indicated by a thermometer (standing at  $0.4$  in clean melting ice), having  $55$  immersed in the vapour, temperature of outside column as given by a second thermometer being  $27$ . What are the corrected temperatures between which the four fractions pass over?

32. A sample of ethene dibromide distils over mostly between  $130.6$  and  $130.7$ ,  $n = 55$  and  $t' = 11.3$ . What is the corrected BP of this fraction? What is the corresponding temperature on the hydrogen thermometer scale?

33. Reduce the indicated BP's given below to temperatures on the hydrogen-thermometer scale.

$$\text{N}_2\text{O}_4 \quad 21^\circ.85 \quad (\mu = 22, t' = 13^\circ.5)$$

$$\text{SiCl}_4 \quad 58^\circ.20 \quad (\mu = 0)$$

$$\text{PCl}_3 \quad 76^\circ.15 \quad (\mu = 18.2, t' = 26^\circ)$$

$$\text{POCl}_3 \quad 107^\circ.30 \quad (\mu = 0).$$

$$\text{VOCl}_3 \quad 127^\circ.15 \quad (\mu = 10, t' = 30^\circ)$$

## CORRECTION OF BAROMETER READINGS.

Observed barometric heights are reduced to the height of a column of mercury at  $0^\circ$  and at the level of the sea in latitude  $45^\circ$ , which would produce the same pressure.

The corrections needed for this reduction are :—

I. Correction for temperature, due to expansion of the mercury and the material of the scale.

Let  $m$  = coefficient of expansion of Hg,  $s$  = coefficient of linear expansion of the substance of the scale,  $h$  = the observed height of the barometer, and  $H$  = the corrected height ; then  $H = h \left( \frac{1 + st'}{1 + mt} \right)$

or approximately  $H = h \{1 - (m - s)t'\}$

Hence the required correction is  $-(m - s)t.h.$

With a brass scale we have  $H = h (1 - 0.000162t)$

and the correction is  $-0.000162.t.h$  ;

and with a glass scale similarly

$$H = h (1 - 0.000157t)$$

and the correction is  $-0.000157.t.h.$

II. Correction for height above the sea-level and latitude, obtained as follows :—

If  $\lambda$  be the latitude, and  $x$  the height expressed in metres of the place of observation above the sea-level, the length of the column of mercury which produces the standard pressure is

$760.000 - 1.946 \cos 2 \lambda + 0.000149.1$  mm. therefore if the observed height of the barometer be  $h$  the true or reduced height

$$H = \frac{h \times 760}{760 + 1.946 \cos 2\lambda + 0.000149.1}$$

If  $\lambda$  be less than  $100m$ . the term  $0.000149.1$  may be omitted.

As these corrections are small, a result approximately true is obtained by taking

$$H = h - 1.946 \cos 2\lambda - 0.000149.1$$

the greatest error so made being  $0.04$  mm. A further correction is required for the combined effects of error in adjustment of the scale and the depression of the column produced by capillarity, this correction should be given by the maker from comparison with a standard instrument.

#### EXAMPLE.

A Fortin barometer at latitude  $52^\circ$  and  $21m$ . above sea-level stands at  $754.34$  mm. The instrument has a brass scale, the correction for index-error and capillarity is  $+0.26$  mm., and the temperature at time of observation is  $16^\circ C.$ ; what is the reduced reading?

Neglecting quantities beyond the second place of decimals.

$$\begin{aligned} I. \quad H &= 754.34 (1 - 0.000162.1) \text{ mm.} \\ &= 754.34 - 754.34 \times 0.000162 \times 16 \text{ mm.} \\ &= 754.34 - 1.96 \text{ mm.} \\ &= 752.38 \text{ mm.} \end{aligned}$$

$$\begin{aligned} II. \quad H &= \frac{H \times 760}{760 + 1.946 \cos 2\lambda + 0.000149.1} \\ &= \frac{752.38 \times 760}{760 + 1.946 \cos 104^\circ + 0.000149.21} \\ &= \frac{752.38 \times 760}{760 + 1.946 (-0.2419)} \\ &= \frac{752.38 \times 760}{759.53} = 752.84 \text{ mm.} \end{aligned}$$

Hence true height of barometer, reduced to  $0^{\circ}\text{C}$ , sea-level, and latitude  $45^{\circ} = 752\cdot84 + \cdot26 \text{ mm.} = 753\cdot10 \text{ mm.}$

### QUESTIONS.

34. The barometer-readings taken during a gas-analysis with a Fortin barometer, of which the maker's correction was  $+0\cdot19 \text{ mm.}$ , were  $754\cdot83 \text{ mm.}$ ,  $756\cdot21 \text{ mm.}$ ,  $757\cdot39 \text{ mm.}$ , and  $758\cdot27 \text{ mm.}$  The temperature of the instrument was throughout  $18^{\circ}\text{C}$ ., what were the barometer-heights reduced to  $0^{\circ}\text{C}$ .?

35. Supposing the barometer to stand at  $753\cdot82 \text{ mm.}$  at London (Lat.  $51^{\circ}30' \text{ N.}$   $T = 8^{\circ}\text{C}$ .), Liverpool (Lat.  $53^{\circ}25' \text{ N.}$   $T = 14^{\circ}\text{C}$ .), Madeira I. (Lat.  $32^{\circ}45' \text{ N.}$   $T = 20^{\circ}\text{C}$ .), and Bombay (Lat.  $19^{\circ}8' \text{ N.}$   $T = 19^{\circ}\text{C}$ .); what is the true pressure of the atmosphere at each of these places?

36. Fill in the reduced barometric heights, in column VI. of the annexed table. All the barometers have brass scales.

I. Temperature of barometer at the time of observation.

II. Height of place of observation above the sea-level.

III. Latitude of „ „

IV. Maker's correction.

V. Observed height of mercury column.

| I.                              | II.    | III.                   | IV.                     | V.                       | VI. |
|---------------------------------|--------|------------------------|-------------------------|--------------------------|-----|
| A. $10^{\circ}\text{C}$ .       | 20 m.  | $45^{\circ}\text{N}$ . | $-0\cdot12 \text{ mm.}$ | $753\cdot72 \text{ mm.}$ |     |
| B. $15^{\circ}\text{C}$ .       | 357 m. | $52^{\circ}\text{S}$ . | $-0\cdot35 \text{ mm.}$ | $761\cdot08 \text{ mm.}$ |     |
| C. $13\cdot5^{\circ}\text{C}$ . | 75 m.  | $63^{\circ}\text{N}$ . | $+0\cdot08 \text{ mm.}$ | $755\cdot59 \text{ mm.}$ |     |
| D. $17\cdot2^{\circ}\text{C}$ . | 28 m.  | $25^{\circ}\text{S}$ . | $-0\cdot21 \text{ mm.}$ | $765\cdot34 \text{ mm.}$ |     |
| E. $16\cdot8^{\circ}\text{C}$ . | 234 m. | $0^{\circ}$            | $+0\cdot17 \text{ mm.}$ | $759\cdot37 \text{ mm.}$ |     |
| F. $20^{\circ}\text{C}$ .       | 998 m. | $72^{\circ}\text{N}$ . | $+0\cdot15 \text{ mm.}$ | $760\cdot18 \text{ mm.}$ |     |
| G. $11^{\circ}\text{C}$ .       | 105 m. | $58^{\circ}\text{N}$ . | $-0\cdot23 \text{ mm.}$ | $762\cdot15 \text{ mm.}$ |     |



## CORRECTION OF THE VOLUMES OF GASES FOR TEMPERATURE AND PRESSURE.

*Law of Charles* :— Gases under constant pressure expand  $\frac{1}{273}$  part of their volume at  $0^{\circ}$  C. for every increase in temperature of  $1^{\circ}$  C.

|  |                |
|--|----------------|
| Thus 273 volumes of any gas at $0^{\circ}$ C.          |                |
| become 274                    "                    "   | $1^{\circ}$ C. |
| "        275                    "                    " | $2^{\circ}$ C. |
| "        276                    "                    " | $3^{\circ}$ C. |
| " $273 + t$ "                    "                     | $t^{\circ}$    |

This fraction  $\frac{1}{273}$ , or the slightly more accurate decimal fraction 0.003665, is termed the *coefficient of expansion of gases*.

### EXAMPLES.

1. 10 c.c. of a gas are measured at  $15^{\circ}$  C. What volume will the gas occupy at  $150^{\circ}$  C.?

$$273 + 15 : 273 + 150 :: 10 : x$$

$$x = \frac{423 \times 10}{288} = 14.69 \text{ c.c.}$$

2. 100 c.c. of hydrogen are measured at  $100^{\circ}$  C. How many cubic centimetres will the gas occupy at  $-100^{\circ}$  C.?

$$273 + 100 : 273 - 100 :: 100 : x$$

$$x = \frac{173 \times 100}{373} = 46.37 \text{ c.c.}$$

3. What will be the volume at  $25^{\circ}$  C. of 252 c.c. of oxygen measured at  $15^{\circ}$  C.?

$$1 + (15 \times 0.003665) : 1 + (25 \times 0.003665) :: 252 : x$$

$$1.054975 : 1.091625 :: 252 : x$$

$$x = \frac{1.091625 \times 252}{1.054975} = 260.75 \text{ c.c.}$$

By increasing the pressure upon a gas its volume is diminished : by diminishing the pressure the volume is increased.

*Boyle's Law* :—The volume of a gas at constant temperature is inversely proportional to the pressure to which it is subjected.

1. 1000 c.c. of hydrogen are measured under a barometric pressure of 740 mm. What will the volume become under the standard pressure of 760 mm.?

$$760 : 740 :: 1000 : x$$

$$x = \frac{740 \times 1000}{760} = 973.6 \text{ c.c.}$$

2. A litre of air is measured at  $0^{\circ}$  C. and 760 mm. What volume will it occupy at 740 mm. and  $15^{\circ}.5$  C.?

$$\left. \begin{array}{l} 273 : 273 + 15.5 \\ 740 : 760 \end{array} \right\} :: 1000 : x.$$

$$x = \frac{288.5 \times 760 \times 1000}{273 \times 740} = 1085.34 \text{ c.c.}$$

*Dalton's Law of Partial Pressures* :—The pressure of a mixture of chemically indifferent gases and vapours is equal to the sum of the pressures which each would exert if it alone occupied the whole space.

#### EXAMPLES.

1. If 100 vols. of air consist of 20.66 O, 77.9 N, 0.03 CO<sub>2</sub>, and 1.40 of aqueous vapour, and the barometer stands at 760 mm. ; what is the partial pressure of each of these vapours and gases?

$$\text{Partial pressure of O} = \frac{760 \times 20.66}{100} = 157.01 \text{ mm.}$$

$$\text{'' '' '' N} = \frac{760 \times 77.91}{100} = 592.11 \text{ mm.}$$

$$\text{'' '' '' CO}_2 = \frac{760 \times 0.03}{100} = 0.23 \text{ mm}$$

$$\text{'' '' '' H}_2\text{O} = \frac{760 \times 1.40}{100} = 10.64 \text{ mm.}$$

The pressure of a vapour in contact with its own liquid is always the same at the same temperature.

2. An eudiometer, graduated in mm. from the closed end, contains coal gas ; pure boiled water is introduced until the mercury meniscus remains wet ; the upper level of the mercury with gas dry stands at 400 mm., the lower level at 800 mm. ; the average volume of 1 cm. of the tube = 1.66 c.c., barometer stands at 756 mm., temp. of air is 18°C. What are the volumes of the dry coal gas and of the vapour of water in the moist gas respectively, reduced to standard conditions?

Vol. of dry coal gas =  $1.66 \times 40.0 = 66.4$  c.c. at 756 - (800 - 400) or 356 mm. and 18°C.

Hence vol. at 0°C. and 760 mm. = 
$$\frac{66.4 \times 356 \times 273}{760 \times 291} = 29.18 \text{ c.c.}$$

Tension of aqueous vapour at 18°C. = 15.33 mm. ; hence upper level of mercury is depressed to  $(400 \times 15.33)$  mm. and vol. of aqueous vapour =  $1.66 \times 41.536 = 68.95$  c.c. at 15.33 mm. and 18°C., and this volume of a gas

= 
$$\frac{68.95 \times 15.33 \times 273}{760 \times 291} = 1.304 \text{ c.c. at } 760 \text{ mm. and } 0^\circ\text{C.}$$

### QUESTIONS.

37. 170 volumes of oxygen are measured at 10°C. What will the volume be on the temperature sinking to 0°C.?

38. A certain weight of air measures a litre at 0°C. How much will the air expand on being heated to 100°C.?

39. A gas has its temperature raised from 15° C. to 50° C. ; at the latter temperature it measures 15 litres. What was the initial volume?

40. A volume of hydrogen measures 1500 cubic centimetres at 0° C. How many cubic centimetres will it measure at (a) 15.5 C., (b) at 50° C., (c) at 100° C., and (d) at 300° C.? At what temperature will it measure exactly 1000 cubic centimetres?

41. The coefficient of expansion for gases for  $1^{\circ}\text{C.}$  is 0.003665. What is the coefficient for (a)  $1^{\circ}\text{F.}$ , and (b)  $1^{\circ}\text{R.}$ ?

42. A certain volume of air preserved at a constant temperature measures 150 cubic centimetres when the barometer stands at 760 millimetres. On the following day its volume is found to have decreased 1.52 cubic centimetres. Calculate the alteration in the height of the barometer which must have ensued.

43. A balloon containing 1200 cubic metres of coal gas under a pressure of 770 millimetres of mercury ascends until the barometer stands at 530 millimetres. What volume would the gas in the balloon now occupy supposing none to have escaped?

44. A certain quantity of nitrogen measures 155 cubic centimetres at  $10^{\circ}\text{C.}$ , and under a pressure of 530 millimetres of mercury. What will the volume become at  $18.7^{\circ}\text{C.}$ , and under a pressure of 590 millimetres of mercury.

45. Calculate the temperature at which air possesses a density equal to that of hydrogen at  $0^{\circ}\text{C.}$

46. Oxygen is passed into an eudiometer till the upper level of the mercury stands at 250 mm., level in trough at 780 mm. It is required to add double the quantity of hydrogen; if the tube be adjusted till the trough level becomes again 780 mm. and the average volume of 10 mm. of tube is 1.74 c.c., what will be the reduced volume of the added hydrogen, and what the reading of the upper level of the mercury in the eudiometer after the addition (Bar. 754 mm., T.  $17.5^{\circ}\text{C.}$ )?

47. Supposing the atmosphere to be saturated at  $15^{\circ}\text{C.}$ , barometer 754 mm., what is the per centage volume of aqueous vapour contained in the air?

48. Defining the dew-point as the temperature at which the air would be saturated when containing the amount of vapour of water present at the time of observation, give the per centage volume of aqueous vapour present in the air when the dew-point is  $15^{\circ}\text{C.}$  and  $5^{\circ}\text{C.}$  respectively (Bar. 765 mm.).

49. A gas burette contains 53.2 c.c. of moist coal gas at 760 mm. pressure and 18.5° C.: find the volume of the dry gas under standard conditions.

50. 23.70 c.c. of dry nitrogen are contained in an absorptiometer, 5 c.c. of water are introduced and by agitation 0.07 c.c. of the gas is absorbed. The pressure is brought to that of the atmosphere, 757.3 mm., when reading the volumes, and the temperature remains at 16° C.: what is the volume of moist nitrogen indicated at the end of the experiment?

## RELATIVE DENSITY OF SOLIDS, LIQUIDS, AND GASES; VAPOUR DENSITY.

THE specific gravity (sp. gr.) or relative density of a solid or liquid substance is the ratio of its mass to the mass of an equal volume of some liquid taken as unity.

The standard universally adopted is pure water at its maximum density. The number which expresses the relative density of a solid or liquid substance denotes, therefore, how much heavier or lighter the substance is than an equal bulk of water at 4° C.

1. The relative density of a solid is generally ascertained by :—

I. The hydrostatic balance method.

$$\text{Rel. dens.} = \frac{\text{Weight of substance } (W)}{\text{Weight of equal vol. water at } 4^{\circ}\text{C.}} = \frac{W}{W - w}$$

where  $w$  = weight of substance in water at 4° C.

If the solid be lighter, bulk for bulk, than water a sinker is employed of weight in water =  $x$ ; and rel. dens. =  $d$ .

$$\text{Rel. dens.} = \frac{W}{W + x - w'}$$

where  $w'$  = weight of combination in water.

If the determination be made at  $t^{\circ}$  C., then

$$\text{Rel. dens.} = \frac{H'}{H' - w'} \times \text{rel. dens. of water at } t^{\circ} \text{ C.}$$

#### EXAMPLE.

A piece of iron sulphide (white pyrites) weighed in air 4.8934 grams : in water it weighed 3.8860 grams. Calculate its rel. dens.

$$\text{Rel. dens.} = \frac{4.8934}{4.8934 - 3.8860} = \frac{4.8934}{1.0074} = 4.857.$$

#### II. The specific gravity flask method.

If  $H'$  = weight of substance in air,  $w'$  = weight of flask filled with water,  $w''$  = weight of flask filled with substance and water ; we have weight of substance in water =  $w'' - w'$  and hence

$$\text{Rel. dens.} = \frac{H'}{H' - w'' + w'} \times \text{rel. dens. of water at } t^{\circ} \text{ C.}$$

2. The relative density of a liquid is commonly found by :

#### I. The specific gravity flask method.

Let  $x$  = weight of the empty flask,  $w$  = weight of flask filled with water at  $t^{\circ}$  C.,  $w'$  = weight of flask filled with liquid under examination, then

$$\text{Rel. dens.} = \frac{w' - x}{w - x} \times \text{rel. dens. of water at } t^{\circ} \text{ C.}$$

#### II. Weighing an insoluble solid in water and in the liquid.

Let  $x$  = weight of solid in air,  $w$  = weight in water at  $t^{\circ}$  C.,  $w'$  = weight in liquid, then

$$\text{Rel. dens.} = \frac{x - w'}{x - w} \times \text{rel. dens. of water at } t^{\circ} \text{ C.}$$

## III. The method of balanced liquid columns.

If  $h$  = height of column of water and  $h'$  = height of balancing column of liquid, then

$$\text{Rel. dens.} = \frac{h}{h'}.$$

## EXAMPLES.

1. Find the rel. dens. of absolute alcohol from the following data :—

|                        |           |        |        |
|------------------------|-----------|--------|--------|
| Weight of bottle empty | . . . . . | 3.7200 | grams. |
| „ filled with water    | . . . . . | 7.9582 | „      |
| „ „ alcohol            | . . . . . | 7.1508 | „      |

$$\text{Rel. dens.} = \frac{7.1508 - 3.7200}{7.9582 - 3.7200} = \frac{3.4308}{4.2382} = 0.8095.$$

2. A glass rod, weighing 13 grams in air, weighs 8 grams in water, and 3.8 grams in sulphuric acid ; what is the sp. gr. of the sulphuric acid ?

$$\text{Sp. gr.} = \frac{13 - 3.8}{13 - 8} = \frac{9.2}{5} = 1.84.$$

*Density of gases and vapours* :—The density of any substance at a known temperature (and pressure, in the case of gases and vapours) is the mass of a unit of volume of the substance at that temperature (and pressure).

The sp. gr. or rel. dens. of a gas or vapour is the ratio of its mass to the mass of an equal volume of hydrogen measured at the same temperature and pressure.

The rel. dens. of a gas is commonly termed the density of the gas, and the rel. dens. of the vapour of any substance the vapour density of the substance.

One gram of hydrogen under standard conditions measures 11.1636 litres ; this volume accordingly becomes a convenient unit of volume for measuring densities. Using this unit, the densities are expressed by the same numbers as the relative densities or specific gravities.

One litre of hydrogen gas at 0° C. and 760 mm.

barometric pressure and at the level of the sea and latitude 45° weighs 0.08958 gram.

3. The rel. dens. of a gas is determined by :—

1. Weighing a known volume of the gas by means of :—

*A.* A counterbalanced globe, filled by the evacuation method.

*B.* The displacement method : a bulb of known volume containing an inert gas is kept at a constant temperature while the experimental gas is passed in through one of the leading tubes in such a way as, so far as possible, to fill the bulb by the displacement of the contained gas.

*C.* The method of collecting in a light small flask over mercury (Bunsen).

11. The effusion method (Bunsen).

The rel. dens. varies directly as the square of the time of effusion of equal volumes.

#### EXAMPLE.

In one of Bunsen's experiments, a certain volume of air escaped under pressure through a minute orifice in 102.7 seconds ; under exactly similar conditions, the same volume of  $\text{CO}_2$  required 127.0 seconds to escape through the same orifice. What is the rel. dens. of  $\text{CO}_2$  (air = 1) ?

$$\frac{\text{Rel. dens. of } \text{CO}_2}{\text{Rel. dens. of air}} = \frac{127.0^2}{102.7^2} = \frac{16129}{10547} = 1.5292 = \text{Rel. dens. of } \text{CO}_2.$$

4. The rel. dens. of a vapour is found usually by :—

*I. A.* The direct measurement of the volume of vapour produced by the evaporation in an enclosed space of a known weight of the substance—the principle of the methods of Gay Lussac and Hofmann.

*B.* The indirect measurement of the same quantity, the volume of an inert gas displaced being actually measured—the principle of Victor Meyer's method.



Or II. The weighing of a known volume of the vapour taken at an ascertained temperature and pressure—the methods of Dumas, and Deville and Troost.

If  $D$  = the required density of the vapour referred to  $H$  as unity, we have in case I. A.

$$D = \frac{w \cdot 760 \cdot (1 + 0.00367 T)}{v \cdot 0.00008958 \cdot (H - h) \cdot (1 + kT)}, \quad \text{where}$$

$w$  = weight of liquid taken, and hence weight of vapour formed.

$v$  = observed volume of vapour in c.c.

$H$  = reduced height of bar. at time of experiment.

$h$  = reduced height of mercury in tube above that in cistern.

$T$  = temperature of vapour.

$k$  = coefficient of cubical expansion of glass for  $1^\circ \text{C}$ .

And in case I. B.

$$D = \frac{w \cdot 760 \cdot (1 + 0.00367 T)}{v \cdot 0.00008958 \cdot (H - p)}, \quad \text{where}$$

$w$  = weight of liquid taken.

$v$  = the observed volume of displaced gas in c.c.

$H$  = reduced height of bar. at time of experiment.

$p$  = vapour tension of water at temperature  $t$  of measuring vessel.

$T$  = temperature of water in collecting trough.

The methods under 4. II. for determining vapour density and under 3. I. for finding the rel. dens. of a gas require the following data ;—

$P$  = the weight of bulb in air empty.

$P'$  = the weight of bulb filled with gas or vapour in air.

$V$  = the capacity of bulb in c.c.

$v$  = the volume of the residual air in c.c.

$H$  = height of bar, and  $t$  = the temp. at which  $P'$  is found.

$H'$  = height of bar, and  $T$  = the reduced temp. of the bath at the time of sealing or closing the bulb.

$k$  = the coefficient of cubical expansion of the material of the bulb.

0.00367 = the coefficient of expansion at constant pressure of a gas.

Then  $P' = P + \frac{0.0012932 \cdot (I' - v) H}{(1 + 0.00367 \cdot t) \cdot 760}$  = the weight of

vapour taken for  $(I' - v)$  is the volume occupied by the air displaced by the vapour or gas and the weight of the

displaced air =  $\frac{0.0012932 \cdot (I' - v) H}{(1 + 0.00367 \cdot t) \cdot 760}$ ;

(As  $v$  is generally small, any small differences between the pressure and temperature under which it is measured and  $H$  and  $t$  may be neglected.)

and the volume occupied by this weight at  $H'$  and  $T$  is

$\left[ V(1 + k T) - v \cdot \frac{1 + 0.00367 \cdot T}{1 + 0.00367 \cdot t} \right]$  which equals under

standard conditions

$\left[ V(1 + k T) - v \cdot \frac{1 + 0.00367 \cdot T}{1 + 0.00367 \cdot t} \right] \cdot 760 \cdot (1 + 0.00367 \cdot T)$

hence the rel. dens. referred to air as unity is given by the formula

$$\frac{P' = P + \frac{0.0012932 \cdot (I' - v) \cdot H}{(1 + 0.00367 \cdot t) \cdot 760}}{\left[ V(1 + k T) - v \cdot \frac{1 + 0.00367 \cdot T}{1 + 0.00367 \cdot t} \right] \cdot 760 \cdot (1 + 0.00367 \cdot T) \cdot \frac{H'}{0.0012932}}$$

if hydrogen be taken as unity 0.0012932 is replaced by 0.00008958 the weight of 1 c.c. of hydrogen in grams.

The expression  $\frac{1}{1 + 0.00367 \cdot T}$  can be at once obtained from Table V. in the Appendix.

An approximate value for the rel. dens. of a gas or vapour is given by

$$D = \frac{P' - P + Vn^t}{(V - v)n^T} \cdot 14.436.$$

in which

$D$  = the required rel. dens. referred to hydrogen as unity.

$n^t$  = the weight of 1 c.c. of air at  $t$ .

$n^T$  = the weight of 1 c.c. of air at  $T$ .

#### EXAMPLES.

1. In a determination of the vapour density of heptane by Hofmann's method (I. A.), the following data were obtained:—

|                              |              |
|------------------------------|--------------|
| Weight of liquid taken . . . | 0.0769 gram. |
| Volume of vapour . . .       | 69.77 c.c.   |
| Temperature . . .            | 99.60°C.     |
| Barometer . . .              | 749.0 mm.    |
| Height of mercury column .   | 493.4 mm.    |

Find the vapour density of heptane.

$$\text{From table V. } \frac{1}{1 + 0.00367 \cdot 99.6} = \frac{0.73232}{1}$$

$$\text{and } (H - h) = 749.0 - 493.4 = 255.6$$

Therefore, neglecting the expansion of the glass,

$$D = \frac{0.0769 \times 760.1}{69.77 \times 255.6 \times 0.73232 \times 0.00008958} = 49.96.$$

2. Find the vapour density of anthracene from the given data, determined by Victor Meyer's method.

Weight of anthracene taken = 0.0530 gram.  
 Temperature of water in measuring cylinder . 17.2°C.  
 Reduced height of barometer . . . . . 720.8 mm.  
 Volume of air collected . . . . . 7.8 c.c.

$$D = \frac{0.0530 \times 760 \times (1 + 0.00367 \times 17.2)}{7.8 \times 0.00008958 \times (720.8 - 14.6)} = 86.77.$$

3. Calculate the vapour density of the body furnishing the following data :—

Weight of empty globe, in air, 24.4722 grams.  
 Weight of globe sealed, with vapour, } 25.0122 grams.  
     in air at 9° C. and 762 mm. }  
 Temp. 215° C., bar. 762 mm., at time of sealing.  
 Capacity of the globe, 169.5 c.c.  
 Residual air, 12.5 c.c.

Our approximate formula is

$$D = \frac{P' - P + Vn^t}{(V - v)n^T} = 14.436$$

$$\begin{aligned} \therefore D &= \frac{(25.0122 - 24.4722) + (169.5 \times 0.001252 \cdot \frac{7.62}{7.60})}{(169.5 - 12.5) \cdot 0.000722 \cdot \frac{7.62}{7.60}} \cdot 14.436 \\ &= \frac{0.5400 + 0.2128}{157.000722 \cdot \frac{7.62}{7.60}} \cdot 14.436 \\ &= \frac{0.7528 \cdot 14.436}{157.000722 \cdot \frac{7.62}{7.60}} = 95.62. \end{aligned}$$

From the more accurate formula

$$D = \frac{P' - P + \frac{0.0012932 \cdot (V - v) \cdot H}{(1 + 0.00367 T) \cdot 760.}}{[V(1 + kT) - v \frac{1 + 0.00367 T}{1 + 0.00367 t}] \frac{H \cdot 0.00008958}{760 \cdot (1 + 0.00367 T)}}$$

Taking  $k$  for glass equal to 0.000023, we have

$$\begin{aligned}
 D &= \frac{25.0122 - 24.4722 + \frac{0.0012932 \cdot (169.5 - 12.5) \cdot 762}{(1 + 0.00367 \times 215) 760}}{\left[ 169.5(1 + 0.000023 \times 215) - 12.5 \frac{1 + 0.00367 \times 215}{1 + 0.00367 \times 9} \right]} \\
 &\quad \frac{762.00008958}{760 \cdot (1 + 0.00367 \times 215)} \\
 &\quad \frac{0.5400 + 0.1971}{[170.3 - 21.6] \frac{762}{760} \cdot \frac{0.00008958}{1.789}} \\
 &= \frac{0.7371 \times 1.789 \times 760}{148.7 \times 0.00008958 \times 762} = 98.73.
 \end{aligned}$$

## QUESTIONS.

51. Calculate the relative density of a solid substance from the following numbers:—

Weight of substance in air . . . 2.4554 grams.  
 „ „ water . . . 2.0778 grams.

52. Determine the relative density of gold from the following data:—

Weight of gold in air . . . 4.6764 grams.  
 Loss of weight in water . . . 0.2447 grams.

53. Find the relative densities of the following substances:—

|                | <i>Granite</i> | <i>Marble</i>  | <i>Hematite</i> |
|----------------|----------------|----------------|-----------------|
| Weight in air. | 409.82 grams.  | 53.2841 grams. | 13.6287 grms.   |
| „ water.       | 259.31 „       | 33.4020 „      | 10.9406 „       |

54. Determine the relative density of wood from the following numbers:—

Weights of: wood in air, 4 grams; a silver sinker, 10 grams; wood and sinker under water, 8.5 grams.  
 Relative density of silver = 10.5.

55. A platinum wire 10 cm. in length weighs 0.12 gram. The relative density of platinum being 21.275, calculate the diameter of the wire.

56. A glass bulb of 120 c.c. capacity weighs 14.5 grams. The relative density of the glass being 2.48, calculate the thickness of the walls of the bulb.

57. Faraday calculated that the gold contained in 4 sovereigns could be drawn into a wire long enough to surround the earth. The weight of a sovereign is 7.988 grams, and 91.66% of this is pure gold, possessing a relative density of 19.3. Assuming that the length of a quadrant of the earth is 10,000,857 metres, find the thickness of the wire.

58. A piece of bell-metal, weighing 7.550 grams in air, weighs 6.6635 grams when weighed under water.

Determine the percentage amount of copper and of tin in the piece on the assumption that no alteration in bulk has occurred in alloying the two metals.

Relative density of copper = 8.93; of tin = 7.292.

59. A piece of cast iron, the relative density of which is known to be 7.2, is suspected to have internal cavities.

Its weight is found to be 203.04 grams, and when suspended in water at 4° C. it is found to weigh 171.84 grams. What is the total volume of these cavities?

60. Find the relative density of calcium from the following determination by Bunsen:—

|  |               |
|--|---------------|
| Weight of empty bottle . . . . .       | 13.640 grams. |
| „ bottle filled with naphtha . . . . . | 20.275 „ .    |
| „ „ partly „ „ . . . . .               | 16.650 „ .    |
| „ „ „ „ and calcium . . . . .          | 19.150 „ .    |
| „ „ „ full of naphtha and „ . . . . .  | 21.576 „ .    |
| Relative density of naphtha . . . . .  | 0.758 „ .     |

61. From the given data, calculate the relative densities of:—

| Weights of     | Substance in air. | Bottle + water. | Bottle + water and substance. |
|----------------|-------------------|-----------------|-------------------------------|
| Quartz . . .   | 3.445 grams.      | 75.103 grams.   | 77.248 grams.                 |
| Heavy-spar .   | 11.216 „          | 69.002 „        | 77.718 „                      |
| Calcite . . .  | 34.151 „          | 80.201 „        | 101.824 „                     |
| Iron pyrites . | 0.795 „           | 5.337 „         | 5.973 „                       |

62. Calculate the relative density of sea water from the following data :—

|                                    |               |
|------------------------------------|---------------|
| Weight of bottle empty . . . . .   | 3.5305 grams. |
| „ filled with sea water, . . . . . | 7.7849 „      |
| „ filled with water . . . . .      | 7.6722 „      |

63. From the given data, calculate the relative densities of the liquids given.

| Weights of                       | Bottle empty. | Bottle filled with water. | Bottle filled with substance. |
|----------------------------------|---------------|---------------------------|-------------------------------|
| A. A mineral water . . . . .     | 14.1256 gm.   | 111.1370 gm.              | 111.7050 gm.                  |
| B. Vanadyl trichloride . . . . . | 1.7413 „      | 6.8880 „                  | 11.2190 „                     |
| C. Chromyl dichloride . . . . .  | 3.5312 „      | 7.6649 „                  | 11.4692 „                     |
| D. Alcohol . . . . .             | 5.2013 „      | 20.2051 „                 | 17.0876 „                     |

64. A specific gravity flask holds 2,545 milligrams of alcohol, 42,740 of mercury, and 5,829 of sulphuric acid.

Calculate the relative density of the sulphuric acid and mercury, the density of the alcohol being 0.8095.

65. A solid weighs *in vacuo* 100 grams; in water 85 grams; and in another liquid 88 grams. What is the relative density of this liquid?

66. A piece of a certain metal weighs 3.7395 grams in air; 2.3545 grams in water; and 2.0896 grams in another liquid. Calculate the relative density of the metal and of the liquid.

67. A column of distilled water 100 mm. high is found to balance columns of (a) glycerine 79.3 mm. high, (b) olive oil 109.3 mm. high, (c) turpentine 114.9 mm. high. What are the relative densities of these three liquids?

68. When a mercury barometer registers 760 mm., a glycerine barometer indicates 8203 mm., and a water barometer 10,162 mm.; the vapour tension of water at the temperature of the air, 15° C., is 12.7 mm. of mercury. What are the relative densities of the mercury and glycerine?

69. Regnault obtained, by his method of counter-balanced glass globes, the following data, from which it is required to calculate the relative density of nitrogen (air = 1).

I. Balloon filled with air while immersed in melting ice. Height of barometer, reduced to  $0^{\circ}$  C., at the moment of closing the tap. . . . .

$$H_0 = 761.19 \text{ mm.}$$

Weight added to balloon . . . . .  $p = 1.487 \text{ gram.}$

II. Balloon evacuated. Pressure of residual air, when balloon is immersed in ice. . . . .

$$h_0 = 8.43 \text{ mm.}$$

Weight added to balloon . . . . .  $P = 14.141 \text{ gram.}$

Air being replaced by nitrogen, same conditions.

$$\begin{aligned} \text{I.} \quad & H_0 = 758.55 \text{ mm.} \\ & p = 1.8725 \text{ gram.} \end{aligned}$$

$$\begin{aligned} \text{II.} \quad & h_0 = 2.18 \text{ mm.} \\ & P = 14.227 \text{ gram.} \end{aligned}$$

70. With the same apparatus, the figures given for hydrogen were :—

$$\begin{aligned} \text{I.} \quad & H_0 = 756.16 \text{ mm.} \\ & p = 13.301 \text{ gram.} \end{aligned}$$

$$\begin{aligned} \text{II.} \quad & h_0 = 3.40 \text{ mm.} \\ & P = 14.1785 \text{ gram.} \end{aligned}$$

With air = 1, find the relative density of hydrogen.

71. Calculate the density of thiophosphoryl fluoride from the following data :—

I. Capacity of glass bulb at  $15.8^{\circ}$  C. and

$$776 \text{ mm.} \quad . . . . . 239.86 \text{ c.c.}$$

Weight of bulb in air at  $17.1^{\circ}$  C. and

$$771 \text{ mm.} \quad . . . . . 59.7543 \text{ grams.}$$

Weight of bulb in air at  $17^{\circ}$  C. and

$$771 \text{ mm. filled with gas and residual nitrogen at } 10.7^{\circ} \text{ C. and}$$

$$771 \text{ mm.} \quad . . . . . 60.3954 \text{ grams.}$$

Volume of residual nitrogen at  $11.3^{\circ}$  C.

$$\text{and } 771 \text{ mm.} \quad . . . . . 78.9 \text{ c.c.}$$

II. Capacity of glass bulb at  $15.8^{\circ}$  C. and

$$776 \text{ mm.} \quad . . . . . 239.86 \text{ c.c.}$$

Weight of bulb in air at  $15.8^{\circ}$  C. and

$$776 \text{ mm.} \quad . . . . . 59.7282 \text{ grams.}$$

Weight of bulb in air at  $15.8^{\circ}$  C. and



778 mm. filled with gas and residual  
 nitrogen at  $77^{\circ}\text{C}$ . and 778 mm. 60.5274 grams.  
 Volume of residual nitrogen at  $9.6^{\circ}\text{C}$ .  
 and 777 mm. . . . . 43.4 c.c.

72. An experimental determination of the density of hydrofluoric acid under diminished pressure gave :—

Weight of bulb and caps in air at  
 $19.7^{\circ}\text{C}$ . and 772 mm. . . . . 244.0120 grams.  
 Weight of bulb and caps and vapour  
 in air at  $17.5^{\circ}\text{C}$ . and 772 mm. . . . . 244.0025 „  
 Cocks turned off at  $31.8^{\circ}\text{C}$ .  
 Bar 772.3 mm., manometer reading  
 106.2 mm.  
 Weight of bulb and caps + water at  
 $24.3^{\circ}\text{C}$ . . . . . 528.18 grams.  
 Residual air, reduced to  $0^{\circ}\text{C}$ . and  
 760 mm. . . . . 3.58 c.c. „  
 Weight of 1 c.c. of air at  $0^{\circ}\text{C}$ . and  
 760 mm. . . . . 0.0012928 „  
 Coefficient of cubical expansion of  
 platinum for  $1^{\circ}\text{C}$ . . . . . 0.000027 „  
 Sp. gr. of air,  $H = 1$ . . . . . 14.435

Hence find the rel. dens. of the vapour of hydrofluoric acid, under the conditions at closing the cocks, as compared with air, and with hydrogen.

73. From the tabulated data, calculate the corresponding relative densities of hydrofluoric acid at the given temperatures.

| $T^{\circ}\text{C}$ . | Height of Bar. | Percentage vol. of residual air. | Pressure of vapour. |
|-----------------------|----------------|----------------------------------|---------------------|
| 26.4                  | 756 mm.        | 1.51                             | 745 mm.             |
| 27.8                  | 763 „          | 2.23                             | 746 „               |
| 29.2                  | 762 „          | 1.55                             | 750 „               |
| 32.0                  | 754.5 „        | 1.52                             | 743 „               |
| 33.1                  | 770.5 „        | 2.64                             | 750 „               |
| 33.8                  | 767 „          | 1.14                             | 758 „               |
| 36.3                  | 751 „          | 1.58                             | 739 „               |
| 38.7                  | 764 „          | 1.69                             | 751 „               |

74. A determination of the density of methyl bromide made by Bunsen according to his method yielded the following data. Calculate the relative density of the compound ( $H = 1$ ).

|  |               |
|--|---------------|
| Vol. of gas, at 0.7464 m. and 16.8° C. . . . .                       | 42.19 c.c.    |
| Height of mercury above the level of the<br>metal in trough. . . . . | 0.0243 m.     |
| Weight of the flask and gas. . . . .                                 | 7.9465 grams. |
| Weight of the flask and air. . . . .                                 | 7.8397 "      |
| Temperature in balance case. . . . .                                 | 6.2 C.        |
| Height of barometer. . . . .   | 0.7421 m.     |

75. Bunsen determined the times of effusion through a minute aperture of the same volume of gases as follows :—

| <i>Air. Hydrogen.</i> |               | <i>Air. Oxygen.</i> |       | <i>Air. Carbon dioxide.</i> |        |
|-----------------------|---------------|---------------------|-------|-----------------------------|--------|
| (1)                   | 105.5    29.7 | 102.5               | 108.5 | 102.7                       | 127.0. |
| (2)                   | 105.6    29.3 | 103                 | 109   | 102.7                       | 127.5. |

Find the rel. dens. of each gas compared with air.

76. The data below were obtained in three determinations of the vapour density of  $P_2O_5$  according to Hofmann's method; calculate the V.D. in each case, (A) Air = 1. (B)  $H = 1$ .

|   | I.            | II.          | III.         |
|---|---------------|--------------|--------------|
| Weight of substance taken                   | 0.1887 grams. | 0.1887 grams | 0.1887 grams |
| Temperature of tube and<br>vapour . . . . . | 132° C.       | 159° C.      | 184° C.      |
| Temperature of air. . . .                   | 20° C.        | 20° C.       | 20° C.       |
| Barometer . . . . .                         | 770 mm.       | 769 mm.      | 769 mm.      |
| Height of mercury column                    | 625 mm.       | 616 mm.      | 605 mm.      |
| Volume of vapour at T° C.                   | 137.5 c.c.    | 139.6 c.c.   | 141.45 c.c.  |
| Tension of mercury at<br>T° C. . . . .      | 1.5 mm.       | 5.6 mm.      | 12 mm.       |

77. A series of experiments by Ramsay and Young, under varying conditions, yielded the following data, from which the vapour-density of acetic acid is to be found in each case (Hofmann's method). ( $H = 1$ ).

| Weight taken.    | Reduced Temp. | Corrected pressure. | Volume.     |
|------------------|---------------|---------------------|-------------|
| A. 0.01126 gram. | 50° C.        | 13.4 mm.            | 170.05 c.c. |
| B. 0.03565 "     | 78.4 "        | 63.2 "              | 137.8 "     |
| C. 0.01126 "     | 118.2 "       | 84.05 "             | 45.15 "     |
| D. 0.03565 "     | 162.5 "       | 373.1 "             | 37.0 "      |
| E. 0.03565 "     | 184.1 "       | 791.6 "             | 18 "        |

78. In the determination of a vapour density by Gay-Lussac's method the following data were obtained :—

Weight of substance taken, 0.1163 grams. Temp. of bath, 215° C. Observed volume of vapour, 50.77 c.c. Barometer, 755.5 mm. Difference of height of mercury inside and outside of tube, 80.0 mm. Height of spermaceti column reduced to mm. of mercury, 16.9 mm. Required the sp. gr. of the vapour ( $H = 1$ ) ; also the weight of one litre at 0° C. and 760 mm. barometric pressure, assuming the vapour to behave like a perfect gas.

79. Using a porcelain vessel, heated in a Perrot's furnace to 1027° C., Victor Meyer obtained the data given below, from which the vapour density is to be calculated.

|                                    | I.            | II.           |
|------------------------------------|---------------|---------------|
| Weight of substance taken (Iodine) | 0.0874 grams. | 0.0847 grams. |
| Barometer . . . . .                | 722.8 mm.     | 722.8 mm.     |
| Temperature of the room . . . . .  | 21.5° C.      | 21.5° C.      |
| Volume of air displaced . . . . .  | 13.7 c.c.     | 13.3 c.c.     |

80. From the tabulated data, obtained by Victor Meyer's method, find the sp. gr. of the vapour of each substance, referred (1) to air, (2) to hydrogen, as unity.

| Substance.         | Weight taken. | Temp. of room. | Bar.      | Volume of air displaced. |
|--------------------|---------------|----------------|-----------|--------------------------|
| A. $\text{CHCl}_3$ | 0.1008 gram.  | 16.5° C.       | 707.5 mm. | 22 c.c.                  |
| B. $\text{CS}_2$   | 0.0495 "      | 16.5° C.       | 717.8 mm. | 16.4 c.c.                |
| C. $\text{OH}_2$   | 0.0102 "      | 16.1° C.       | 723.3 mm. | 14.6 c.c.                |
| D. Iodine          | 0.1105 "      | 16.0° C.       | 714.8 mm. | 11.1 c.c.                |

81. The specific gravity of coal-gas is about 0.5 referred to air as unity, and air is 14.435 times heavier than hydrogen. Calculate from these data the weight of coal-gas, at 10° C. and 530 mm. pressure, required to fill a balloon having a capacity of 800 cu. m.

82. Calculate the vapour density ( $H = 1$ ) of a hydride from the following numbers :—

Balloon with air, 40.7955 grams. Temperature, 11° C.  
Balloon with vapour, 41.0960 grams. Temperature of sealing, 173° C. Capacity of balloon, 189 c.c.

83. Calculate the vapour density of camphor vapour ( $H = 1$ ) from the following numbers, obtained by Dumas according to his method :—

Temp. of air, 13.5° C. Bar. 742 mm. Temp. of bath at the moment of sealing the globe, 244° C. Increase of the weight of globe, 0.708 grams. Volume of mercury required to fill the globe, 295 c.c. Residual air *nil*.

84. In a series of determinations by Deville and Troost of the vapour density of sulphur, the following figures were obtained :—

|                             | I.           | II.          | III.         |
|-----------------------------|--------------|--------------|--------------|
| Temperature of the air . .  | 10° C.       | 15° C.       | 10° C.       |
| Height of barometer . .     | 769.5 mm.    | 760 mm.      | 769.4 mm.    |
| Difference of weighings . . | -0.190 gram. | -0.176 gram. | -0.203 gram. |
| Volume of porcelain bulb.   | 281 c.c.     | 280 c.c.     | 303.5 c.c.   |
| Residual air . . . . .      | 3 c.c.       | 6 c.c.       | 3.5 c.c.     |
| Temp. of bath (Zn vapour)   | 1040° C.     | 1040° C.     | 1040° C.     |

Find the vapour density in each case, taking air = 1. Coefficient of cubical expansion of porcelain = 0.000108. (N.B. The second weighing gives a figure here less than the first with the empty bulb in air.)

85. Using a modification of Dumas' method, Friedel and Crafts obtained the following data, from which the vapour density of aluminic chloride is to be calculated :—  
Temp. of vapour, 398.2° C. Pressure of vapour, 0.97

atmosphere. Barometer height, 754·8 mm. Volume of globe, 250 c.c. Residual air, 245 c.c. at 10·3 mm. and 17·2° C. Excess of weight of globe, 0·8765 gram. Weight of air displaced 0·3020 gram.

## AVOGADRO'S HYPOTHESIS ; DENSITY AND MOLECULAR WEIGHT ; VALENCY, EQUIVALENTS AND ATOMIC WEIGHTS.

According to *Avogadro's Hypothesis* equal volumes of gases, at the same temperature and pressure, contain the same number of molecules.

Hence it follows that the molecular weights of bodies in the state of gas or vapour are in the same ratio as their specific gravities or vapour densities : *e.g.* if  $H = 1$ , the sp. gr. of gaseous  $HCl = 18·18$ .

Assuming the molecular weight of  $H$  to be 2, the molecular weight of  $HCl$  is 36·36.

The molecular weight of a gaseous element or compound may be thus defined : The *molecular weight* of a gaseous element or compound is a number which expresses how many times greater than two unit masses of hydrogen is the mass of the specified element or compound which occupies (under the same conditions of temperature and pressure) the same volume as is occupied by these two unit masses of hydrogen. The *maximum atomic weight* of an element is a number which expresses how many times greater is the smallest mass of that element which combines with other elements to form a compound gaseous molecule, than the smallest mass of hydrogen which combines with other elements to produce a compound gaseous molecule, such smallest mass of hydrogen being taken as unity. (Watts's *Dict.* 1. p. 341.)

That property of an atom which determines the number of other atoms with which it can combine to form a compound molecule is termed its *valency* or atomic value. Valency is usually expressed as the number of hydrogen atoms, or atoms chemically equivalent to hydrogen, which one atom of the specified element can combine with or replace when in the same state as in the compound considered.

The *equivalent* of an element is the number expressing that weight of the element which will combine with or replace the unit weight of hydrogen.

Let  $E$  = the equivalent of any element,  $A$  = its atomic weight, and  $V$  = its valency in the compound used for determining the equivalent ; the relations between these quantities are expressed by the equation  $A = E \cdot V$ .

The numerical value of the molecular weight of any substance is obtained by the summation of the atomic weights of the component elements each multiplied by the number denoting how many of such atoms are contained in the molecule, *e.g.* the molecular weight of alcohol,  $C_2H_6O$ , is found thus  $(12 \times 2) + (1 \times 6) + 16 = 24 + 6 + 16 = 46$ .

#### QUESTIONS.

86. If the density of sulphuretted hydrogen = 1.791, ammonia = 0.597, nitrous oxide = 1.520, marsh gas = 0.555, chloroform = 4.20, and stannic chloride = 9.20, as compared with air, what are the molecular weights of these bodies taking the molecular weight of hydrogen as 2?

87. Determine the weight of one litre of the following simple gases and vapours at  $0^\circ$  and 760 mm., on the supposition that they can all exist as perfect gases at the standard temperature and pressure :—

|           |             |          |
|-----------|-------------|----------|
| Oxygen.   | Sulphur.    | Sodium.  |
| Chlorine. | Phosphorus. | Arsenic. |
| Iodine.   | Nitrogen.   | Mercury. |

88. Calculate the volume, at the standard temperature and pressure, of a kilogram of each of the following gases and vapours :—

|                    |                        |
|--------------------|------------------------|
| Carbon monoxide.   | Ethylene.              |
| Hydrogen sulphide. | Oxysulphide of carbon. |
| Marsh gas.         | Bromine.               |
| Water.             | Hydrochloric acid.     |

89. What weight of each of the specified substances is represented by the appended formulæ, taking one gram as the unit of weight?

Lead chloride,  $PbCl_2$ ; Silicon fluoride,  $SiF_4$ ;  
 Ferric chloride,  $FeCl_3$ ; Methyl bromide,  $CH_3Br$ .

90. Find the density (air = 1) of:—Carbon monoxide, CO; Carbon bisulphide, CS<sub>2</sub>; Sulphur trioxide, SO<sub>3</sub>; Boron trifluoride, BF<sub>3</sub>; Phosphorus pentafluoride, PF<sub>5</sub>.

91. If the electro-chemical equivalent of: Oxygen = 7.98, Silver = 107.66, Chlorine = 35.37, Antimony = 39.86, and Copper = 31.59, and the hydrogen replacing power of these elements in the compounds used in finding the equivalents be for one atom of the element taken, Oxygen 2, Silver 1, Chlorine 1, Antimony 3, and Copper 2 atoms; what are the atomic weights of these elements?

92. From the data given deduce the probable atomic weight of oxygen:

| Gaseous compound.      | Rel. dens. (air = 1). | Rel. dens. $\times 28.87$ approximate mol. wt. | Molecular weight. | Analysis stated in parts by wt. per mol. |
|------------------------|-----------------------|--|-------------------|--|
| Carbon dioxide . . .   | 1.53                  | 44.2   | 43.89             | 31.92 O + 11.97 C.                       |
| Sulphur dioxide . . .  | .25                   | 64.0   | 63.90             | 31.92 O + 31.98 S.                       |
| Sulphur trioxide . . . | .29                   | 83.7   | 79.86             | 47.88 O + 31.98 S.                       |
| Carbon monoxide . . .  | 0.97                  | 27.97  | 28.93             | 15.96 O + 11.97 C.                       |
| Water . . . . .        | 0.63                  | 18.2   | 17.96             | 15.96 O + 2 H.                           |
| Nitric oxide . . . .   | 1.04                  | 30.0   | 29.97             | 15.96 O + 14.01 N.                       |

93. Find the most probable atomic weight of carbon from the appended experimental results:

| Gaseous compound.     | Rel. dens. (air = 1). | Analysis in parts by wt.      |
|-----------------------|-----------------------|-------------------------------|
| Marsh gas . . . . .   | 0.555                 | 11.97 C. + 2.0 H.             |
| Methyl iodide . . . . | 4.883                 | 11.97 C. + 126.53 I + 3.0 H.  |
| Chloroform . . . . .  | 4.30                  | 11.97 C. + 106.11 Cl + 1.0 H. |
| Carbon monoxide . . . | 0.968                 | 11.97 C. + 15.96 O.           |
| Carbon bisulphide . . | 2.645                 | 11.97 C. + 63.96 S.           |

94. Find the molecular weights of the following bodies:

Cadmium at 940°, Rel. dens. = 3.94, (air = 1).

Phosphorus at 500°, Rel. dens. = 4.35, „

Mercury at 446°, Rel. dens. = 6.98, „

95. Select the most probable atomic weight for phosphorus as indicated by the given experimental results :—

| Gaseous compound.            | Rel. dens.<br>(air = 1). | Analysis in parts by<br>wt.                   |
|------------------------------|--------------------------|---|
| Phosphorus hydride . . . .   | 1.15                     | 30.96 P. + 3.0 H.                             |
| Phosphorus chloride . . . .  | 4.88                     | 30.96 P. + 106.11 Cl.                         |
| Triethyl phosphine oxide . . | 4.60                     | 30.96 P. + 15.96 O.<br>(+ 71.82 C. + 15.0 H.) |

How many atoms are there in the phosphorus molecule?

## DEDUCTION OF THE EMPIRICAL FORMULA OF A BODY FROM ITS PERCENTAGE COMPOSITION; FORMULÆ OF MINERALS.

In order to calculate the empirical formula of a compound, divide the percentage amount of each constituent by its corresponding atomic weight; divide each of the quotients so obtained by the lowest number, and reduce them to their simplest ratios.

### EXAMPLES.

1. A body on analysis yielded the following percentage composition :—

|                |         |
|----------------|---------|
| Carbon . . . . | 27.273  |
| Oxygen . . . . | 72.727  |
|                | <hr/>   |
|                | 100.000 |
|                | <hr/>   |

Calculate its empirical formula.

The atomic weight of carbon = 12; that of oxygen = 16.



Then

$$C = \frac{27.273}{12} = 2.2727$$

$$O = \frac{72.727}{16} = 4.5454$$

The simplest relation between the carbon and oxygen is at once seen to be as 1 to 2, since

$$2.2727 : 4.5454 :: 1 : 2.$$

Hence the formula of the compound is  $\text{CO}_2$

2. A compound of hydrogen and nitrogen was found to possess the following percentage composition. Calculate its formula.

|                |         |
|----------------|---------|
| Nitrogen . . . | 82.353  |
| Hydrogen . . . | 17.647  |
|                | <hr/>   |
|                | 100.000 |
|                | <hr/>   |

The atomic weight of N = 14, and of H = 1.

$$N = \frac{82.353}{14} = 5.882$$

$$H = \frac{17.647}{1} = 17.647$$

The simplest ratio between the nitrogen and hydrogen is as 1 to 3, since

$$5.882 : 17.647 :: 1 : 3.$$

Hence the formula of the body is  $\text{NH}_3$ .

3. A compound of iron and oxygen possesses the following percentage composition. Calculate its formula.

|                  |        |
|------------------|--------|
| Iron . . . . .   | 70.01  |
| Oxygen . . . . . | 29.99  |
|                  | <hr/>  |
|                  | 100.00 |
|                  | <hr/>  |

At. weight of Fe = 56.0. At. weight of O = 16.

Then

$$\frac{70.01}{56} = 1.2514$$

$$\frac{29.99}{16} = 1.8744$$

The ratio between  $1.2514 : 1.8744 :: 1 : 1.5$

The simplest ratio, in whole numbers, is therefore  $2 : 3$ .  
Hence the formula of the body is  $\text{Fe}_2\text{O}_3$ .

#### FORMULÆ OF MINERALS.

There exist many groups of minerals of which the individual members are composed of equal numbers of atoms similarly combined, and which possess the same or nearly the same crystalline form; such groups are termed isomorphous groups, and the minerals forming each group are said to be isomorphous with each other.

Isomorphous minerals may replace each other without affecting the exterior form of the mineral partially replaced. As the percentage amount of the elements in such minerals is different in each case, mixed minerals do not admit of being directly represented by a simple formula derived as above from the percentage composition.

It is the practice to represent minerals of this type by a general formula obtained by considering the particular isomorphous substance present in greatest quantity as the typical substance and reducing the quantities of the replacing bodies to equivalent quantities of the typical body, when the formula may be at once obtained by the ordinary means.

When possible, mineral analyses are ordinarily reported as percentages of oxides, and in the calculation these oxides are considered as the isomorphous components to be reduced to terms of that present in greatest amount.

As an example we may consider the case of ankerite: an analysis of which by Schrötter yielded the following results:

|                         |       |
|-------------------------|-------|
| CaO . . . .             | 26.90 |
| MgO. . . .              | 7.84  |
| FeO . . . .             | 19.91 |
| MnO. . . .              | 1.82  |
| CO <sub>2</sub> . . . . | 43.05 |
|                         | <hr/> |
|                         | 99.52 |

CaO is the oxide present in greatest quantity : we therefore reduce the other oxides to their equivalents of CaO and adding all together we obtain the typical composition of the mineral considered as if it were a Ca compound ; thus :—

$$\frac{7.84 \times 56}{40} = 10.98 = \text{CaO equivalent to MgO present.}$$

$$\frac{19.91 \times 56}{72} = 15.48 = \text{CaO equivalent to FeO present.}$$

$$\frac{1.82 \times 56}{70} = 1.46 = \text{CaO equivalent to MnO present.}$$

Hence total typical oxide present (M'' O)

$$= 26.90 + 10.98 + 15.48 + 1.46 = 54.82 \text{ parts.}$$

combined with CO<sub>2</sub> . . . . . 43.05

By the ordinary method

$$\text{M'' O. . . . } \frac{54.82}{56} = 0.98 \text{ nearly, and } \frac{0.98}{0.98} = 1$$

$$\text{CO}_2 . . . . \frac{43.05}{44} = 0.98 \text{ nearly } \frac{0.98}{0.98} = 1$$

Hence typical composition is M''O.CO<sub>2</sub> or M''CO<sub>3</sub>, where M'' represents Ca, Mg, Fe, and Mn.

The formula of ankerite may therefore be written (Ca, Mg, Fe, Mn) CO<sub>3</sub>.

QUESTIONS.—Deduce the formulæ of the following substances :—

|                             |                            |
|-----------------------------|----------------------------|
| 96. Hydrogen . . . 5'88     | † 103. Calcium . . . 38'72 |
| Oxygen . . . 94'12          | Phosphorus . . . 20'00     |
| <hr/>                       | Oxygen . . . 41'28         |
| 100'00                      | <hr/>                      |
|                             | 100'00                     |
| 97. Nitrogen . . . 30'43    |                            |
| Oxygen . . . 69'57          | † 104. Sodium . . . 32'79  |
| <hr/>                       | Aluminium . . . 13'02      |
| 100'00                      | Fluorine . . . 54'19       |
|                             | <hr/>                      |
| ! 98. Iron . . . 70'01      |                            |
| Oxygen . . . 29'99          | 105. Potassium . . . 45'95 |
| <hr/>                       | Nitrogen . . . 16'45       |
| 100'00                      | Oxygen . . . 37'60         |
|                             | <hr/>                      |
| 99. Carbon . . . 20'00      | 100'00                     |
| Oxygen . . . 26'67          |                            |
| Sulphur . . . 53'33         |                            |
| <hr/>                       |                            |
| 100'00                      | 106. Aluminium . . . 16    |
|                             | Sulphur . . . 28           |
| 100. Potassium . . . 28'73  | Oxygen . . . 56            |
| Hydrogen . . . 0'73         | <hr/>                      |
| Sulphur . . . 23'52         | 100                        |
| Oxygen . . . 47'02          | <hr/>                      |
| <hr/>                       |                            |
| 100'00                      | 107. Copper . . . 57'46    |
|                             | Carbon . . . 5'43          |
| ! 101. Magnesium . . . 9'76 | Hydrogen . . . 0'91        |
| Sulphur . . . 13'01         | Oxygen . . . 36'20         |
| Oxygen . . . 26'01          | <hr/>                      |
| Water . . . 51'22           | 100'00                     |
| <hr/>                       |                            |
| 100'00                      |                            |
|                             | † 108. Hydrogen . . . 3'18 |
| 102. Zinc . . . 22'70       | Oxygen . . . 33'88         |
| Sulphur . . . 11'15         | Nitrogen . . . 14'84       |
| Oxygen . . . 22'28          | Sulphur . . . 16'95        |
| Water . . . 43'87           | Nickel . . . 31'15         |
| <hr/>                       | <hr/>                      |
| 100'00                      | 100'00                     |
| <hr/>                       | <hr/>                      |

|                         |                         |
|-------------------------|-------------------------|
| 109. Carbon . . . 85·71 | 112. Carbon . . . 74·07 |
| Hydrogen . . . 14·29    | Hydrogen. . . 8·64      |
|                         | Nitrogen . . . 17·29    |
| <hr/>                   | <hr/>                   |
| 100·00                  | 100·00                  |
| <hr/>                   | <hr/>                   |
| 110. Carbon . . . 92·3  |                         |
| Hydrogen . . . 7·7      |                         |
| <hr/>                   |                         |
| 100·0                   |                         |
| <hr/>                   |                         |
| 111. Carbon . . . 19·04 | 113. Carbon . . . 46·66 |
| Hydrogen . . . 4·76     | Hydrogen. . . 4·26      |
| Sulphur . . . 25·40     | Nitrogen . . . 5·20     |
| Oxygen . . . 50·80      | Oxygen . . . 5·92       |
| <hr/>                   | Platinum . . . 18·26    |
| 100·00                  | Chlorine . . . 19·70    |
| <hr/>                   | <hr/>                   |
|                         | 100·00                  |
|                         | <hr/>                   |

114. Show that a mineral having the following percentage composition is represented by the formula  $MOCO_2$  when M signifies a metal of the magnesium family :

|                              |       |
|------------------------------|-------|
| Lime . . . . .               | 28·4  |
| Magnesia . . . . .           | 12·3  |
| Iron monoxide . . . . .      | 12·3  |
| Manganese monoxide . . . . . | 1·9   |
| Carbon dioxide . . . . .     | 44·4  |
|                              | <hr/> |
|                              | 99·3  |
|                              | <hr/> |

115. The mineral kerolite gave the following numbers on analysis. Calculate its formula :

|         |       |        |        |
|---------|-------|--------|--------|
| $SiO_2$ | $MgO$ | $H_2O$ |        |
| 46·96   | 31·26 | 21·22  | 99·44. |

116. A specimen of cobalt-bloom was found to have the following composition. Determine its formula :

|           |       |       |        |          |
|-----------|-------|-------|--------|----------|
| $As_2O_3$ | $CoO$ | $FeO$ | $H_2O$ |          |
| 38·43     | 36·52 | 1·01  | 24·10  | = 100·06 |

117. Calculate the formula of soda-feldspar from the following analysis :—

|         |           |           |       |       |        |         |           |
|---------|-----------|-----------|-------|-------|--------|---------|-----------|
| $SiO_2$ | $Al_2O_3$ | $Fe_2O_3$ | $CaO$ | $MgO$ | $K_2O$ | $Na_2O$ |           |
| 68·45   | 18·71     | 0·27      | 0·50  | 0·18  | 0·65   | 11·24   | = 100·00. |

118. Calculate the formula of labradorite from the following analysis :—

|                  |                                |                                |       |      |                   |
|------------------|--------------------------------|--------------------------------|-------|------|-------------------|
| SiO <sub>2</sub> | Al <sub>2</sub> O <sub>3</sub> | Fe <sub>2</sub> O <sub>3</sub> | CaO   | MgO  | Na <sub>2</sub> O |
| 52.52            | 30.03                          | 1.72                           | 12.58 | 0.19 | 4.51 = 101.55.    |

### TO CALCULATE THE PERCENTAGE COMPOSITION OF A COMPOUND FROM ITS FORMULA.

FIRST calculate the molecular weight of the compound by adding together the sums of its atomic weights. Thus the formula for water is H<sub>2</sub>O ; its molecular weight is therefore 17.96.

$$\begin{array}{rcl}
 \text{Atomic weight of H.} & = & 1 \quad 1 \times 2 = 2 \\
 \text{Atomic weight of O.} & = & 15.96 \\
 & & \hline
 & & 17.96
 \end{array}$$

In order to calculate from the molecular weight of the compound the percentage amount of its constituents—that is, to determine how much of each constituent is contained in 100 parts of the compound—multiply the amounts of the several constituents in the compound by 100, and divide each of the products by the molecular weight of the compound. Thus, to calculate the amounts of hydrogen and oxygen contained in 100 parts of water :—

$$H = \frac{2 \times 100}{17.96} = 11.14$$

$$O = \frac{16 \times 100}{17.96} = 88.86$$

$$\begin{array}{r}
 \hline
 100.00 \\
 \hline
 \end{array}$$

Table I. in the Appendix gives the atomic weights of the elements according to the most trustworthy determinations.

## QUESTIONS.

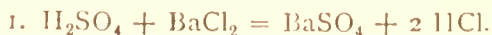
Calculate the percentage composition of the following compounds :—

|                                  |   |
|----------------------------------|---|
| 119. Water . . . . .             | $\text{H}_2 \text{O}.$  |
| 120. Potassium chlorate . . . .  | $\text{K Cl O}_3.$  |
| 121. Mercury monoxide . . . .    | $\text{Hg O}.$  |
| 122. Potassium nitrate . . . .   | $\text{K N O}_3.$   |
| 123. Sodium nitrate . . . . .    | $\text{Na N O}_3.$  |
| 124. Barium sulphate. . . . .    | $\text{Ba S O}_4.$  |
| 125. Calcium carbonate . . . .   | $\text{Ca C O}_3.$  |
| 126. Silver chloride . . . . .   | $\text{Ag Cl}.$   |
| 127. Magnesium pyrophosphate .   | $\text{Mg}_2 \text{P}_2 \text{O}_7.$  |
| 128. Potassium platinum chloride | $2 (\text{K Cl}) + \text{Pt Cl}_4.$   |
| 129. Sodium thiosulphate. . . .  | $\text{Na}_2 \text{S}_2 \text{O}_3 + 5 \text{H}_2 \text{O}.$  |
| 130. Magnetic oxide of iron . .  | $\text{Fe}_3 \text{O}_4.$   |
| 131. Hausmannite . . . . .       | $\text{Mn}_3 \text{O}_4.$   |
| 132. Copper pyrites . . . . .    | $\text{Cu}_2 \text{S} + \text{Fe}_2 \text{S}_3.$  |
| 133. Stromeyerite . . . . .      | $\text{Ag Cu S}.$   |
| 134. Stilbite . . . . .          | $\text{Ca O Al}_2 \text{O}_3 . 6 \text{Si O}_2$<br>$+ 5 \text{H}_2 \text{O}.$   |
| 135. Idocrase . . . . .          | $9 (2 \text{Ca O} . \text{Si O}_2) .$<br>$2 (2 \text{Al}_2 \text{O}_3 . 3 \text{Si O}_2).$  |
| 136. Spodumene . . . . .         | $3 (\text{Li}_2 \text{O} . \text{Si O}_2).$<br>$4 (\text{Al}_2 \text{O}_3 . 3 \text{Si O}_2).$  |
| 137. Sphene . . . . .            | $\text{Ca Si O}_3 . \text{Ca Ti O}_3.$  |
| 138. Pyromorphite . . . . .      | $3 \text{Pb}_3 \text{P}_2 \text{O}_8 . \text{Pb Cl}_2.$   |
| 139. Ethyl alcohol . . . . .     | $\text{C}_2 \text{H}_6 \text{O}.$   |
| 140. Cane sugar . . . . .        | $\text{C}_{12} \text{H}_{22} \text{O}_{11}.$  |
| 141. Xylene . . . . .            | $\text{C}_8 \text{H}_{10}.$   |
| 142. Cymene. . . . .             | $\text{C}_{10} \text{H}_{14}.$  |
| 143. Silicon ethyl . . . . .     | $\text{Si} \left\{ \begin{array}{l} \text{C}_2 \text{H}_5. \\ \text{C}_2 \text{H}_5. \\ \text{C}_2 \text{H}_5. \\ \text{C}_2 \text{H}_5. \end{array} \right.$ |
| 144. Potassium thiacetate . . .  | $\text{C}_2 \text{H}_3 \text{K O S}.$   |
| 145. Potassium ferrocyanide . .  | $\text{K}_4 \text{Fe C}_6 \text{N}_6.$  |
| 146. Kreatin . . . . .           | $\text{C}_4 \text{H}_8 \text{N}_3 \text{O}_2 + 11 \text{H}_2 \text{O}.$   |
| 147. Rosaniline . . . . .        | $\text{C}_{20} \text{H}_{21} \text{N}_3 \text{O}.$  |
| 148. Strychnine . . . . .        | $\text{C}_{21} \text{H}_{22} \text{N}_2 \text{O}_2.$  |

# CHEMICAL EQUATIONS; TO CALCULATE THE AMOUNT OF MATERIAL REQUIRED TO PRODUCE A GIVEN WEIGHT OF ANY SUBSTANCE OR THE QUANTITY OF THE SUBSTANCE PRODUCED BY THE DECOMPOSITION OF A KNOWN WEIGHT OF THE MATERIAL.

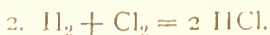
*Chemical equations*.:—The results of any chemical actions are represented by equations in which the signs + – and = are used in the same sense as in algebra, so far as regards the weights of matter represented by the symbols.

The meaning of such an equation will be best shown by examples.—



This equation indicates not only that sulphuric acid and barium chloride react to produce barium sulphate and hydrochloric acid, but, further, that the molecular weight of sulphuric acid reacts with the molecular weight of barium chloride to produce the molecular weight of barium sulphate and twice the molecular weight of hydrochloric acid; hence 98 parts by weight of sulphuric acid react with 208 parts by weight of barium chloride to form 233 parts by weight of barium sulphate and 73 parts by weight of hydrochloric acid gas.

The number of *atoms* of each element must be the same on either side of the equation, consequently the total number of *atoms* must be the same on either side. The numbers of *molecules* before and after a reaction are not necessarily the same.



Here, as in (1), it is indicated that 2 parts by weight of hydrogen combine with 71 parts by weight of chlorine to produce 73 parts by weight of hydrochloric acid. But the equation signifies more: as we know the molecular weights



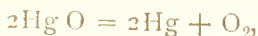
of all the reacting bodies and products it shows that a molecule of hydrogen combines with a molecule of chlorine to form two molecules of hydrochloric acid gas. If we state the molecular weights in grams we know from the equation that 22.4 litres of hydrogen combine with 22.4 litres of chlorine to yield 44.8 litres of hydrochloric acid, for two grams of hydrogen measure 22.4 litres approximately at the standard conditions and, by Avogadro's hypothesis, equal numbers of molecules under the same conditions occupy equal volumes.

## EXAMPLES.

1. How much oxygen can be obtained by the decomposition of 100 grams of mercury monoxide? The symbol for mercury monoxide is  $\text{HgO}$ : hence its molecular weight is 216.

$$\begin{array}{r} \text{Hg} = 200 \\ \text{O} = 16 \\ \hline 216 \\ \hline \end{array}$$

When mercury monoxide is heated, it is completely resolved into oxygen and metallic mercury,



432 parts of mercury monoxide giving 400 of mercury and 32 of oxygen. If, therefore, 32 grams of oxygen are evolved by the decomposition of 432 grams of mercury monoxide, how many grams of oxygen will be evolved by the decomposition of 100 grams of mercury monoxide?

$$432 : 100 :: 32 : x.$$

$$x = 7.407.$$

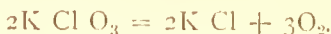
7.407 grams of oxygen will therefore be evolved on heating 100 grams of mercury monoxide.

2. I want 100 lbs. of oxygen: how many lbs. of potassium chlorate must I take?

The formula of potassium chlorate is  $\text{KClO}_3$ . Its molecular weight is therefore

$$\begin{array}{rcl}
 \text{K} & = & 39\cdot1 \\
 \text{Cl} & = & 35\cdot5 \\
 \text{O}_3 & = & (16 \times 3) 48\cdot0 \\
 \hline
 & & 122\cdot6 \\
 \hline
 \end{array}$$

This substance on being heated eventually decomposes into potassium chloride and oxygen.



That is, 96 lbs. of oxygen are evolved on heating 245·2 lbs. of potassium chlorate. Then how many lbs. of potassium chlorate are required to yield 100 lbs. of oxygen?

$$\begin{array}{l}
 96 : 100 : 245\cdot2 : x \\
 x = 255\cdot4 \text{ lbs.}
 \end{array}$$

Hence it would require 255·4 lbs. of potassium chlorate to yield 100 lbs. of oxygen.

3. How many cubic centimetres of oxygen and hydrogen, measured at 10° C. and 770 mm. pressure, can be obtained by the decomposition of 1 gram of water?

The symbol for water is  $\text{H}_2\text{O}$ , its molecular weight is 18. The weight of hydrogen yielded by a gram of water is

$$\begin{array}{l}
 18 : 1 :: 2 : x \\
 x = 0\cdot1111 \text{ gram.}
 \end{array}$$

The weight of oxygen is

$$\begin{array}{l}
 18 : 1 :: 16 : x \\
 x = 0\cdot8889 \\
 \text{1\cdot0000 gram.}
 \end{array}$$

1000 cubic centimetres of hydrogen at 0° C. and 760 mm. weigh 0·08936 grams. Then what volume would 0·1111 gram of hydrogen occupy?

$$\begin{array}{l}
 0\cdot08936 : 0\cdot1111 :: 1000 : x \\
 x = 1243\cdot28 \text{ c.c. of hydrogen.}
 \end{array}$$

This at 10° and 770 mm. would measure

$$\begin{array}{l}
 \left. \begin{array}{l} 273 : 273 + 10 \\ 770 : 760 \end{array} \right\} :: 1243\cdot28 : x \\
 x = 1272\cdot09 \text{ c.c.}
 \end{array}$$

1000 cubic centimetres of oxygen at  $0^{\circ}$  C. and 760 mm. weigh  $(16 \times 0.08936 \text{ gram}) = 1.42976 \text{ grams}$ . Then what volume would 0.8889 grams occupy ?

$$1.42976 : 0.8889 :: 1000 : x.$$

$$x = 621.713 \text{ c.c. of oxygen.}$$

This at  $10^{\circ}$  C. and 770 mm. would measure

$$\left. \begin{array}{l} 273 : 273 + 10 \\ 770 : 760 \end{array} \right\} :: 621.713 : x$$

$$x = 636.116 \text{ c.c.}$$

Therefore, a gram of water on being decomposed would yield at  $10^{\circ}$  C. and 770 mm. pressure, 1908.206 c.c. of mixed gases consisting of

|          |   |   |          |      |
|----------|---|---|----------|------|
| Hydrogen | . | . | 1272.09  | c.c. |
| Oxygen   | . | . | 636.116  | „    |
|          |   |   | <hr/>    |      |
|          |   |   | 1908.206 |      |
|          |   |   | <hr/>    |      |

### QUESTIONS.

149. How much potassium chlorate is needed to furnish 1 lb. of oxygen ?

150. I require 2 kilograms of oxygen : how much (a) mercury monoxide, (b) potassium chlorate, (c) manganese dioxide, (d) sulphuric acid, shall I need ?

151. On completely decomposing by heat a certain weight of potassium chlorate, I obtain 20.246 grams of potassium chloride. What weight of potassium chlorate did I take, and how much oxygen was evolved ?

152. A gas bag has a capacity of 45 litres : how much manganese dioxide containing 70 per cent. of  $\text{MnO}_2$  is required to fill it with oxygen at  $15^{\circ}$  C. and 760 mm. barometric pressure ?

153. 132.74 kilograms of hydrogen are needed to inflate a balloon. What weight of zinc and sulphuric acid will be required to produce this quantity of gas ?

154. Iron, zinc, and sulphuric acid diluted so as to contain 20 per cent. of real acid ( $\text{SO}_4\text{H}_2$ ), are supplied to you. Find the amount of these materials required to produce the above quantity of hydrogen, (1) by the action of sulphuric acid upon iron, (2) by the action of sulphuric acid upon zinc.

155. What weight of potassium chlorate is needed to furnish oxygen sufficient to burn the hydrogen evolved by the action of water upon 200 grams of sodium?

156. How many cubic centimetres of oxygen and hydrogen measured at  $12^\circ \text{C}$ . and under a pressure of 762 mm. of mercury can be obtained by the electrolysis of 10 grams of water?

157. 100 grams of steam is passed over 1000 grams of red-hot iron wire. Required the volume of hydrogen evolved measured at  $10^\circ \text{C}$ . and 742 mm. pressure, and the weight of iron oxide produced.

158. 77 per cent. of the weight of the air, freed from moisture and carbonic acid, consists of nitrogen. Calculate the weight of (a) metallic copper, and (b) of phosphorus required to abstract the oxygen from 1 lb. of air.

159. Required the weight of ammonia and of chlorine needed to produce a litre of nitrogen.

160. What quantities of nitre and Chili saltpetre respectively will be required to obtain the maximum quantity of nitric acid by reaction with 140 kilos. of 97 per cent. sulphuric acid?

! 161. How much nitre and sulphuric acid shall I need to prepare nitric acid enough to neutralize exactly 5 lbs. of chalk?

162. Calculate the volume of nitrogen monoxide at  $15^\circ \text{C}$ . and 740 mm. produced on heating 30 grams of ammonium nitrate.

163. What weight of copper is required to yield a litre of nitrogen dioxide at  $0^\circ \text{C}$ . and 760 mm.?

164. At the ordinary temperature and pressure water absorbs 50 per cent. of its weight of ammonia. Calculate the amount of sal-ammoniac and quicklime needed to produce 10 kilograms of *Liquor Ammoniac*.

165. Coal contains about 2 per cent. of nitrogen. Assuming that 75 per cent. of this amount escapes as ammonia on distillation, calculate the amount of coal required to furnish the sal-ammoniac needed to produce the 10 kilograms of *Liquor Ammoniac*.

166. Calculate the weight of air required to burn a ton of coal possessing the following percentage composition :—

Carbon, 88.42 ; Hydrogen, 5.61 ; Oxygen, 5.97.

167. How much marble and hydrochloric acid containing 22 per cent. HCl are needed to yield 10 litres of carbon dioxide at  $15^{\circ}$  C. and 760 mm. barometric pressure?

168. According to Boussingault, a square metre of leaf will decompose in sunlight 1.108 litres of carbon dioxide in an hour. Calculate in tons the amount of carbon assimilated in an hour by a million trees, each possessing 100,000 leaves, and each leaf containing 25 square centimetres. Calculate the volume of the carbon so assimilated on the assumption that it possesses a sp. gr. of 1.6.

! 169 How many litres of (1) hydrogen and of (2) carbonic oxide gases at  $10^{\circ}$  C. and 750 mm. can be obtained by the decomposition of 100 grams of steam by passing it over red-hot charcoal?

170. I require 10 litres of carbon monoxide at  $0^{\circ}$  C. and 760 mm. pressure. How many grams of (1) oxalic acid, (2) of formic acid, and (3) of potassium ferrocyanide shall I need?

171. Required the weight in grams of sodium acetate to yield 10 litres of methane at  $0^{\circ}$  and 760 mm.

172. Manchester coal-gas contains 35 per cent. by volume of marsh gas. Calculate the weight of this gas in a gasometer holding 100,000 cubic feet of coal-gas.

173. Calculate the weight in kilos. of air needed, and of carbon dioxide and water formed, by the complete com-

bustion of 10,000 litres of Manchester coal-gas possessing the following composition by volume :--

|                                 |        |
|---------------------------------|--------|
| Hydrogen . . . . .              | 45.58  |
| Marsh gas . . . . .             | 34.90  |
| Carbon monoxide . . . . .       | 6.64   |
| Ethylene . . . . .              | 4.08   |
| Butylene . . . . .              | 2.38   |
| Sulphuretted hydrogen . . . . . | 0.29   |
| Nitrogen . . . . .              | 2.46   |
| Carbonic acid . . . . .         | 3.67   |
|                                 | <hr/>  |
|                                 | 100.00 |
|                                 | <hr/>  |

174. 100 grams of pure silver cyanide are shaken up with 120 grams of hydrochloric acid containing 26.1 per cent. of HCl. Required the amount of silver chloride produced, and the percentage amount of hydrocyanic acid in solution.

175. Required the weight of manganese dioxide containing 60 per cent.  $\text{MnO}_2$  to liberate all the iodine from 100 grams of potassium iodide.

176. A manufacturer of bleaching powder requires 10 tons of chlorine. How much salt, manganese containing 59 per cent. of the dioxide, and sulphuric acid containing 58 per cent. of real acid, will he need?

177. What weight of hydrochloric acid gas is produced in the manufacture of 100 tons of salt cake? What volume of gas escapes supposing the manufacturer to condense only 92 per cent. of the quantity evolved?

178. 5.75 grams of silver nitrate are added to 5.75 grams of a solution of hydrochloric acid containing 10.22 per cent. HCl. How much silver is precipitated and how much remains in solution?

179. What weight of bleaching powder can be theoretically produced from 150 tons of manganese containing 68 per cent. of the dioxide?

180. Required the weight of potassium chlorate yielded by the chlorine evolved from 100 tons of manganese containing 60 per cent. of the dioxide.

181. What weight of potassium bromate can be obtained by neutralizing 520 grams of bromine with potash?

182. Iodic acid may be obtained by passing a stream of chlorine through water containing iodine in suspension. How much iodine and chlorine will be needed to prepare 100 grams of iodic acid?

183. Required the weight of copper and sulphuric acid needed to yield 3 litres of sulphurous acid at the standard temperature and pressure.

! 184. A vitriol-maker prepares 100 tons of vitriol of specific gravity 1.6, containing 70 per cent. of acid : how many tons of pyrites containing 42 per cent. of sulphur must for this purpose be burnt? Supposing that 3 per cent. of the theoretical yield of sulphur remained unburnt in the pyrites, what would be the difference in the production of sulphuric acid?

185. What volume of oxygen at 10° C. and 743 mm. of mercury can be obtained by the decomposition of a litre of sulphuric acid possessing a density of 1.854 at 0° C.?

186. What weight of iron sulphide will be needed to yield a litre of hydrogen sulphide at 0° C. and 760 mm., and how much air will be required to burn this gas completely to water and sulphur dioxide?

† 187. 1 gram of phosphorus is to be converted into the pentachloride. How many litres of chlorine at 0° C. and 760 mm. are required?

188. How much crystallized microcosmic salt must be ignited to furnish a gram of sodium metaphosphate?

! 189. An alkali-maker consumes 300 tons of salt per week : he divides three-quarters of his yield of soda-ash equally for the preparation of soda crystals, bicarbonate, and solid caustic containing 70 per cent.  $\text{Na}_2\text{O}$ . What weight of sulphur will he need to use weekly, and what is the theoretical weekly yield of the four products of manufacture?

190. Required the weight of limestone needed to convert 50 tons of soda crystals into bicarbonate.

! 191. 100 grams of pure iron is burnt in excess of (1) oxygen and (2) chlorine. What is the weight of oxide and chloride produced?

## COMBINATION AND DECOMPOSITION OF GASEOUS BODIES.

### EXAMPLES.

1. 4 litres of hydrogen are mixed with 5 litres of chlorine, and the mixture exploded. What volume of hydrochloric acid gas is produced? Which gas, and how much of it remains in excess?

From the equation



it is evident that 1 volume of hydrogen combines with 1 volume of chlorine to form 2 volumes of hydrochloric acid gas. Therefore 4 litres of hydrogen would require 4 litres of chlorine, and would form 8 litres of hydrochloric acid gas, 1 litre of chlorine remaining uncombined.

2. 150 cubic centimetres of oxygen are mixed with 400 cubic centimetres of hydrogen and the mixture exploded. What volume of steam is produced? Which gas, and how much of it, remains uncombined?

From the equation



it is evident that 150 cubic centimetres of oxygen would require 300 cubic centimetres of hydrogen, and yield 300 cubic centimetres of steam, 100 cubic centimetres of hydrogen remaining in excess.

3. 100 cubic centimetres of ammonia gas are completely decomposed by a series of electric sparks, yielding 200 cubic centimetres of mixed hydrogen and nitrogen: an excess of oxygen is next added, when the volume of mixed gases is found to amount to 290 cubic centimetres. The mixture is now exploded, when 65 cubic centimetres of gas remain. Show from these data that the symbol for ammonia is  $\text{NH}_3$ .



The total volume of the mixed gases before the explosion was 290 cubic centimetres; after the explosion 65 cubic centimetres remain. Hence  $(290 - 65) = 225$  cubic centimetres of oxygen and hydrogen have disappeared to form water, and two-thirds of this contraction gives the amount of hydrogen in the mixture, and hence in the 200 cubic centimetres resulting from the decomposition of the 100 cubic centimetres of ammonia gas  $\frac{2}{3}$  of  $225 = 150$  cubic centimetres. Hence in the 200 cubic centimetres of the gas, 150 cubic centimetres were hydrogen, the remaining 50 being nitrogen. The gases are therefore mixed in the proportion of 1 volume of nitrogen to 3 volumes of hydrogen, and hence the symbol for ammonia is  $\text{NH}_3$ .

## QUESTIONS.

! 192. 20 litres of hydrogen are mixed with 10 litres of chlorine. Which gas remains in excess? How many litres of hydrochloric acid are produced?

† 193. One cubic foot of hydriodic acid is decomposed by an excess of bromine. How many cubic feet of hydrobromic acid are formed?

† 194. The iodine in 100 volumes of hydriodic acid is liberated in succession by chlorine and by oxygen. How many volumes of chlorine and how many volumes of oxygen are required?

195. 50 cubic centimetres of hydrogen are exploded with 75 cubic centimetres of oxygen. Required the total volume of the gases after the explosion, measured at 150 C. and 760 mm. pressure.

196. How many litres of oxygen are contained in 5 litres of nitrogen peroxide ( $\text{N}_2\text{O}_1$ )?

197. An unknown volume of hydrogen sulphide required 110.34 cubic centimetres of chlorine for complete decomposition. What was the volume of the hydrogen sulphide?

198. How many cubic centimetres of hydrogen and nitrogen are contained in a litre of ammonia gas?

† 199.  $V$  volumes of a hydrocarbon  $C_n H_{2n}$  are submitted to combustion. How many volumes of oxygen are required for its complete combustion, and how many volumes of carbonic anhydride are generated?

200. How many litres of air at  $0^\circ$  and 760 mm. are required for the complete combustion of 10 litres of (1) marsh gas, (2) olefiant gas, (3) acetylene?

201. 5 litres of chlorine are mixed with 5 litres of carbon monoxide. What volume of phosgene gas is produced, and how much hydrochloric acid and carbon dioxide would be produced by the decomposition of this gas with water?

202. What volume of arsenic is contained in a litre of oxide of cacodyl vapour measured at  $500^\circ$  C.?

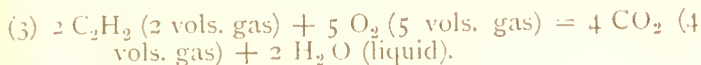
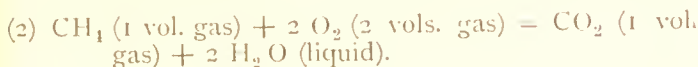
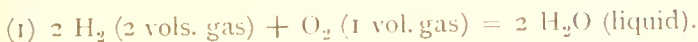
## GAS ANALYSIS CALCULATIONS.

The processes employed in gas analysis fall naturally under the heads :—

I. Proximate analysis, effected by the successive absorption of the various constituents of a gaseous mixture by suitable reagents.

Ultimate analysis, performed by the combustion of the gaseous mixture and calculation of the quantity of each element present from the observed alteration in volume due to the combustion, and the quantities of  $CO_2$  and residual gas resulting therefrom. The combustion method in most cases allows the proximate composition of the mixture to be obtained indirectly; e.g. a mixture of  $x$  c.c.  $H_2$ ,  $y$  c.c.  $CH_4$ , and  $z$  c.c.  $C_2H_2$  yields the following data :  $A$  = original volume of mixture,  $B$  = contraction due to combustion,  $C$  = volume of  $CO_2$  produced by the combustion.

From the equations



we have

$$A = x + y + z.$$

$$B = \frac{3}{2}x + 2y + \frac{5}{2}z.$$

$$C = y + 2z.$$

Hence

$$y = 2B - 3A, \quad z = \frac{3A - 2B + C}{2}, \quad x = \frac{5A - 2B - C}{2}.$$

$x$ ,  $y$ , and  $z$  are thus all expressed in terms of the measured quantities  $A$ ,  $B$ , and  $C$  and can therefore be readily found.

It is required to measure the comparative quantities of gas present before and after an experiment in both I. and II. Three quantities require to be taken into account in such measurements, namely : (a) the volume of the gas,  $V$ ; (b) its temperature,  $t$  (or absolute temperature  $273 + t$   $^\circ\text{K}$ ); (c) its pressure,  $P$ . With reference to the measurement of  $V$ ,  $T$ , and  $P$  four cases occur among common methods of gas analysis :—

(A).  $T$  and  $P$  are kept constant,  $V$  alone requires to be measured. Many technical processes, *e.g.* Orsat's method, follow this plan.

(B).  $V$  and  $T$  are maintained throughout the same,  $P$  is the measured quantity. Regnault's and derived processes use this method.

(C). The ratio  $\frac{T}{P}$ , termed the disgregation of the gas, is always brought to the same value,  $V$  is the recorded quantity. Doyère's method furnishes an example of this type.

(*D*). Analysis by the eudiometer and absorption tube needs the observation of all these variables,  $P$ ,  $V$ , and  $T$ .

In (*A*) and (*C*) the observed volumes are in the direct ratio of the volumes reduced to standard conditions and hence may be directly compared; in (*B*) the measured pressures vary directly as the corrected volumes and can therefore be substituted for the latter in all calculations of the relative composition of the gas sample; in (*D*) all volumes must be reduced to some standard conditions before they can be compared.

#### EXAMPLES.

1. A heating-gas, made by working coke-gas producers with air and steam, yielded on analysis the following data:—

- (*a*) Volume of gas employed . . . . . 97.7 c.c.
- (*b*) Vol. after absorption of  $\text{CO}_2$  by potash . . 87.5 c.c.
- (*c*) Vol. after absorption of CO by cuprous chloride . . . . . 68.6 c.c.
- (*d*) Vol. taken from (*c*) for estimation of H . . 59.3 c.c.
- (*e*) Vol. after addition of air . . . . . 98.8 c.c.
- (*f*) Vol. after combustion with palladium asbestos in capillary tube . . . . . 80.5 c.c.

Assuming the pressure and temperature to have remained constant during the analysis, calculate the percentage composition of the gas.

$$\text{CO}_2 \text{ absorbed by potash} = 97.7 - 87.5 = 10.2 \text{ c.c.}$$

$$\text{hence } \% \text{ of } \text{CO}_2 = \frac{10.2 \times 100}{97.7} = 10.45.$$

$$\text{CO absorbed by cuprous chloride} = 87.5 - 68.6 = 18.9 \text{ c.c.}$$

$$\text{hence } \% \text{ of CO} = \frac{18.9 \times 100}{97.7} = 19.34.$$

$$\text{Contraction on combustion} = 98.8 - 80.5 = 18.3 \text{ c.c.}$$

From equation  $2 \text{H}_2 + \text{O}_2 = 2 \text{H}_2\text{O}$ , it is seen that  $\frac{2}{3}$  of observed contraction represents vol. of H present ;

$$\text{hence vol. of H in } 59.3 \text{ c.c. (d)} = \frac{18.3 \times 2}{3} = 12.2 \text{ c.c.}$$

$$\text{and } \therefore \text{ of H in gas} = \frac{12.2 \times 68.6 \times 100}{59.3 \times 97.7} = 14.44.$$

By difference, the % of N is

$$100 - 10.45 - 19.34 - 14.44 = 55.77.$$

The percentage composition is then :—

|                         |                 |
|-------------------------|-----------------|
| Carbon dioxide . . . .  | 10.45 per cent. |
| Carbon monoxide . . . . | 19.34 „         |
| Hydrogen . . . . .      | 14.44 „         |
| Nitrogen . . . . .      | 55.77 „         |

2. A determination of the composition of air by Frankland and Ward's modification of Regnault's process supplied these figures ( $V$  and  $T$  are constant in this method) :

(a) Air alone :—

|                                      |           |
|--------------------------------------|-----------|
| Height of Hg. in barometer . . . .   | 673.0 mm. |
| Height of mark on measuring tube . . | 383.0 mm. |

(b) Air + hydrogen :—

|                     |           |
|---------------------|-----------|
| Height bar. . . . . | 945.0 mm. |
| „ mark . . . . .    | 383.0 mm. |

(c) After explosion :

|                     |           |
|---------------------|-----------|
| Height bar. . . . . | 763.3 mm. |
| „ mark . . . . .    | 383.0 mm. |

Hence *pressures* are :—(a) 290.0 mm. (b) 562.0 mm. (c) 380.3 mm.; and the *corrected volumes* are in the same ratio as the *observed pressures*, therefore the percentage of oxygen present in the sample of air is

$$\frac{562.0 - 380.3}{3} \cdot 100 = \frac{60.56 \times 100}{290} = 20.88.$$

3. Find the composition of a sample of coal-gas from the data given (Bunsen.)

|   | Volume. | Pressure. | Temperature<br>°C. |
|---|---------|-----------|--------------------|
| A. Gas taken . . . . .                      | 134.3   | 0.7285 m. | 14.5               |
| After KOH absorption . .                    | 131.1   | 0.7317 m. | 17.8               |
| After pyrogallate absorp-<br>tion . . . . . | 130.6   | 0.7293 m. | 17.5               |

A portion of the residue was treated in an absorption-tube with  $\text{H}_2\text{SO}_4$  containing excess of  $\text{SO}_3$ , and then washed with KOH.

|   | Volume. | Pressure. | Temperature<br>°C. |
|---|---------|-----------|--------------------|
| B. Portion taken. . . . .   | 97.3    | 0.6923 m. | 18.5               |
| After absorption of ethy-<br>lene, propylene, and<br>benzene-vapour . . . . | 93.2    | 0.6835 m. | 18.0               |

A part of the residue from *B* was then exploded in the eudiometer.

|   | Volume. | Pressure. | Temperature<br>°C. |
|---|---------|-----------|--------------------|
| C. Part taken. . . . .                    | 150.9   | 0.1774 m. | 18.4               |
| After addition of $\text{O}_2$ . . .      | 281.5   | 0.3041 m. | 18.9               |
| After further addition of<br>air. . . . . | 472.3   | 0.4942 m. | 19.0               |
| After explosion . . . . .                 | 425.5   | 0.4485 m. | 17.8               |
| After absorption of $\text{CO}_2$ .       | 407.7   | 0.4375 m. | 18.0               |
| On addition of $\text{H}_2$ . . . .       | 561.7   | 0.5888 m. | 19.1               |
| After explosion . . . . .                 | 307.5   | 0.3965 m. | 17.0               |

The remainder of the gas from *A* was then similarly analysed.

|   | Volume. | Pressure. | Temperature<br>°C. |
|---|---------|-----------|--------------------|
| D. Portion taken for analysis                 | 139.8   | 0.1623 m. | 15.2               |
| After addition of O <sub>2</sub> . . . . .    | 275.8   | 0.2963 m. | 15.7               |
| After further addition of<br>air . . . . .    | 446.6   | 0.4704 m. | 13.3               |
| After explosion . . . . .                     | 407.0   | 0.4296 m. | 14.1               |
| After absorption of CO <sub>2</sub> . . . . . | 383.0   | 0.4236 m. | 16.8               |
| Residue + H <sub>2</sub> . . . . .            | 592.8   | 0.6296 m. | 17.1               |
| After explosion . . . . .                     | 424.0   | 0.4629 m. | 17.2               |

All the volumes given in this example require to be reduced to some common temperature and pressure; taking 0° C. and 1 m. pressure for standards, we have :—

*A.* Gas taken = 92.91; after KOH absorption = 90.06;

hence % of CO<sub>2</sub> =  $\frac{(92.91 - 90.06) 100}{92.91} = \frac{285}{92.91} = 3.07$ .

After absorption by alkaline pyrogallate, remaining vol. = 89.51, hence % of

$$O = \frac{(90.06 - 89.51) 100}{92.91} = \frac{0.55 \times 100}{92.91} = 0.59.$$

*B.* Part taken = 63.08; after absorption of ethylene propylene, and benzene-vapour by SO<sub>3</sub> = 59.75; hence

$$\begin{aligned} \text{of these constituents} &= \frac{(63.08 - 59.75) \times 89.51 \times 100}{63.08 \times 92.91} = \\ &= \frac{3.33 \times 89.51 \times 100}{63.08 \times 92.91} = 5.09. \end{aligned}$$

*C.* Portion taken = 25.1; after addition of O = 80.1; after addition of air = 218.2; after explosion = 179.2; hence contraction = 218.2 - 179.2 = 39.0. (1)

After absorption of CO<sub>2</sub> produced = 167.4; hence vol. of CO<sub>2</sub> = 179.2 - 167.4 = 11.8 (2)

After addition of H<sub>2</sub> = 308.9; after explosion = 135.9; hence second contraction = 173. (3)

The incombustible residue of N from (2) is therefore, 167.4 -  $\frac{11.8}{5} = 167.4 - 2.36 = 165.04$ , of which 0.7904

$(218.2 - 80.1) = 109.15$  belongs to added air, hence N in 25.1 vols. taken  $= 109.74 - 109.15 = 0.59$  vols.; therefore

$$\% \text{ of N in gas} = \frac{0.59 \times 59.75 \times 89.51 \times 100}{25.1 \times 63.08 \times 92.91} = 2.15.$$

Combustible gas  $= 25.1 - 0.59 = 24.51$ ; and this consists of  $x$  vols. H +  $y$  vols.  $\text{CH}_4$  +  $z$  vols. CO.

From the equations :—



$$\text{we have, contraction } 39 = \frac{3}{2}x + 2y + \frac{1}{2}z \quad (a)$$

$$\text{CO}_2 \text{ formed } 11.8 = y + z. \quad (b);$$

$$\text{and total volume } 24.51 = x + y + z. \quad (c);$$

$$\text{hence } x \left\{ \text{from } (b) \text{ and } (c) \right\} = 12.71.$$

Solving  $(a)$  and  $(b)$  for  $z$ , we have :—

$$39 = 19.06 + 2y + \frac{1}{2}z$$

$$23 = \quad \quad \quad 2y + 2z$$

$$\text{hence } \frac{3z}{2} = 23.6 + 19.06 - 39 = 3.66.$$

$$\text{and } z = \frac{3.66 \times 2}{3} = 2.44.$$

$$\text{From } (b) \ y + z = 11.8$$

$$\text{so } y = 11.8 - z = 11.8 - 2.44 = 9.36.$$

$$\text{Therefore } \% \text{ of H} = \frac{12.71 \times 59.75 \times 89.51 \times 100}{25.1 \times 63.08 \times 92.91} = 46.21.$$

$$\% \text{ of CH}_4 = \frac{9.36 \times 59.75 \times 89.51 \times 100}{25.1 \times 63.08 \times 92.91} = 34.03.$$

$$\text{and } \% \text{ of CO}_2 = \frac{2.44 \times 59.75 \times 89.51 \times 100}{25.1 \times 63.08 \times 92.91} = 8.87.$$



*D.* Portion taken containing all the combustible gases  
 21.5; after addition of O = 77.3; after addition of air  
 200.4; after explosion = 166.2; hence contraction =  
 34.2. (1)

After absorption of CO<sub>2</sub> produced, vol. = 152.9; hence  
 CO<sub>2</sub> = 166.2 - 152.9 = 13.3. (2)

After addition of H to residue, vol. = 351.3; after ex-  
 plosion 184.8; hence second contraction = 166.5. (3)

The contraction on explosion

(1) =  $\frac{34.2 \times 89.51 \times 100}{21.5 \times 92.91} = 153.2$  per cent. of the volume  
 of the original gas.

The CO<sub>2</sub> produced

(2) =  $\frac{13.3 \times 89.51 \times 100}{21.5 \times 92.91} = 59.60$  per cent. of the same.

Contraction due to CH<sub>4</sub>, CO, and H, from C. (1),  
 =  $\frac{39 \times 59.75 \times 89.51 \times 100}{25.1 \times 63.08 \times 92.91} = 141.8$  per cent. of  
 original vol.; hence contraction due to ethylene, propylene,  
 and benzene, = 153.2 - 141.8 = 11.4 per cent. of vol.  
 of original gas.

Similarly, CO<sub>2</sub> produced from CH<sub>4</sub> and CO, from C (2)  
 =  $\frac{11.8 \times 59.75 \times 89.51 \times 100}{25.1 \times 63.08 \times 92.91} = 42.90$  per cent., and so  
 vol. of CO<sub>2</sub> produced from ethylene, propylene, and  
 benzene, = 59.60 - 42.90 = 16.70 per cent. of vol. of  
 original gas.

The percentage of ethylene, propylene, and benzene-  
 vapour, present in the original gas is 5.09. (B).

Let  $x$  = percentage of C<sub>2</sub>H<sub>4</sub>,  $y$  = percentage of C<sub>3</sub>H<sub>6</sub>,  
 and  $z$  = percentage of C<sub>6</sub>H<sub>6</sub>; then, from the equations:—



we have contraction  $11.4 = 2x + \frac{3}{2}y + \frac{5}{2}z$ . (4)

and vol. of  $\text{CO}_2$   $16.70 = 2x + 3y + 6z$ ; (5)

also vol. of gases  $5.09 = x + y + z$ . (6)

$$\text{From (4) and (6) } \begin{cases} 11.4 = 2x + \frac{3}{2}y + \frac{5}{2}z \\ 12.72 = \frac{3}{2}x + \frac{3}{2}y + \frac{5}{2}z \end{cases}$$

$$\text{whence } 1.32 = \frac{1}{2}x$$

$$\text{and } x = 2.64 \% \text{ of } \text{C}_2\text{H}_4.$$

$$\text{From (5) and (6) } \begin{cases} 16.70 = 5.28 + 3y + 6z \\ 5.09 = 2.64 + y + z \end{cases}$$

$$\text{or } \begin{cases} 11.42 = 3y + 6z \\ 2.45 = y + z \end{cases}$$

$$\text{or } \begin{cases} 11.42 = 3y + 6z \\ 14.70 = 6y + 6z \end{cases}$$

$$\text{whence } 3y = 3.28 \text{ and } y = 1.09 \% \text{ of } \text{C}_3\text{H}_6.$$

Again,  $y + z = 2.45 \therefore z = 2.45 - 1.09 = 1.36 \% \text{ of } \text{C}_6\text{H}_6.$

Tabulating our results, the percentage composition of coal gas is :—

|                                       |                            |
|---------------------------------------|----------------------------|
| Carbon dioxide . . . . .              | 3.07.                      |
| Oxygen . . . . .                      | 0.59.                      |
| Absorbed by SO <sub>3</sub> . . . . . | 5.09 %                     |
|                                       | { Ethylene . . . . .       |
|                                       | { Propylene . . . . .      |
|                                       | { Benzene-vapour . . . . . |
| Nitrogen . . . . .                    | 2.15.                      |
| Hydrogen . . . . .                    | 46.21.                     |
| Marsh-gas . . . . .                   | 34.03.                     |
| Carbon monoxide . . . . .             | 8.87.                      |

### QUESTIONS.

203. Calculate the percentage composition of a sample of atmospheric air from the following numbers :—

|                     | Volume. | Pressure. | Temperature<br>°C. |
|---------------------|---------|-----------|--------------------|
| Air employed        | 863.7   | 0.5576 m. | 5.5                |
| After addition of H | 1006.7  | 0.6911 m. | 5.5                |
| After explosion     | 800.7   | 0.4914 m. | 5.6                |

204. A gaseous mixture containing oxygen, nitrogen, and carbonic acid, yielded the following numbers on analysis. Calculate the proportion of the constituent gases in 100 volumes of the mixture (Bunsen):—

|                                   | Volume. | Pressure. | Temperature<br>°C. |
|-----------------------------------|---------|-----------|--------------------|
| Original gas                      | 171.2   | 0.6240 m. | 13.5               |
| After absorption of carbonic acid | 167.3   | 0.6196 m. | 13.5               |
| After absorption of oxygen        | 147.0   | 0.6058 m. | 13.9               |

205. Determine the amount of aqueous vapour in a sample of air which yielded the following numbers on analysis (Bunsen):—

*Air saturated with moisture.*

|                             |           |
|-----------------------------|-----------|
| Lower level Hg. stands at   | 565.9     |
| Upper level in eudiometer   | 317.3     |
| Vol. corresponding to 317.3 | 292.7     |
| Meniscus correction         | 0.4       |
| Air temperature             | 20.2° C.  |
| Height of barometer         | 0.7469 m. |

*Same volume of air dried by Ca Cl<sub>2</sub>.*

|                             |           |
|-----------------------------|-----------|
| Lower level Hg. stands at   | 565.9     |
| Upper level in eudiometer   | 310.7     |
| Vol. corresponding to 310.7 | 286.0     |
| Meniscus correction         | 0.4       |
| Air temperature             | 20.2° C.  |
| Height of barometer         | 0.7474 m. |

206. Calculate the composition by volume of water from the following eudiometric synthesis:—

- A. Hydrogen saturated with moisture.  
 B. Hydrogen + Oxygen saturated with moisture.  
 C. Residue after explosion saturated with moisture.

|   | A.        | B.        | C.       |
|---|-----------|-----------|----------|
| Observations at lower level of Hg. . . . .          | 771.8     | 768.2     | 771.9    |
| Observations at upper level in eudiometer . . . . . | 238.0     | 435.0     | 332.0    |
| Corresponding volume . . . . .                      | 262.5     | 468.3     | 360.8    |
| Barometer . . . . .                                 | 0.7540 m. | 0.7540 m. | 0.7540   |
| Thermometer . . . . .                               | 12.1°     | 12.6°     | 13.0°    |
| Corresponding tension of aqueous vapour . . . . .   | 10.5 mm.  | 10.9 mm.  | 11.2 mm. |

207. Find the volume of each constituent contained in one volume of methyl ether from the data below, and deduce its empirical formula:—

|   | Volume. | Pressure. | Temperature. |
|---|---------|-----------|--------------|
| A. Gas taken . . . . .                        | 50.6    | 0.1419 m. | 14°C.        |
| After addition of oxygen . . . . .            | 199.8   | 0.3112 m. | 2.6°C.       |
| After explosion . . . . .                     | 172.4   | 0.2738 m. | 3.7°C.       |
| After absorption of CO <sub>2</sub> . . . . . | 132.8   | 0.2409 m. | 3.9°C.       |
| After addition of H . . . . .                 | 547.3   | 0.6955 m. | 2.6°C.       |
| After explosion . . . . .                     | 466.6   | 0.6126 m. | 1.5°C.       |
| B. Gas taken . . . . .                        | 79.6    | 0.3140 m. | 4.0°C.       |
| After addition of oxygen . . . . .            | 327.2   | 0.5615 m. | 5.0°C.       |
| After explosion . . . . .                     | 268.7   | 0.4915 m. | 4.9°C.       |
| After heating to 99.5° . . . . .              | 418.1   | 0.6752 m. | 99.5°C.      |
| After cooling . . . . .                       | 268.2   | 0.4914 m. | 3.7°C.       |
| After absorption of CO <sub>2</sub> . . . . . | 193.3   | 0.4188 m. | 0.7°C.       |

208. Find the formula of nitrous oxide from the analytical results given:—

|                               | Volume. | Pressure. | Temperature. |
|-------------------------------|---------|-----------|--------------|
| Gas taken . . . . .           | 110.2   | 0.2175 m. | 14.4°C.      |
| After addition of H . . . . . | 248.4   | 0.3219 m. | 14.4°C.      |
| After explosion . . . . .     | 191.4   | 0.2664 m. | 14.0°C.      |
| After addition of O . . . . . | 228.8   | 0.2931 m. | 12.8°C.      |
| After explosion . . . . .     | 160.6   | 0.2253 m. | 13.7°C.      |

209. A gaseous mixture collected from Hekla a month after an eruption yielded the following figures : find its percentage composition :

|  | Volume. | Pressure. | Temperature. |
|--|---------|-----------|--------------|
| Gas taken . . . . .                            | 114.9   | 0.6944 m. | 20.4°C.      |
| After absorption with $\text{MnO}_2$ .         | 112.9   | 0.6958 m. | 20.4°C.      |
| After absorption with $\text{KOH}$ .           | 108.1   | 0.7092 m. | 20.6°C.      |
| Gas decanted into eudiometer                   | 136.7   | 0.3460 m. | 20.6°C.      |
| After explosion with $(\text{H}_2 + \text{O})$ | 137.2   | 0.3452 m. | 20.7°C.      |
| After addition of $\text{H}$ . . . .           | 190.4   | 0.3980 m. | 20.5°C.      |
| After explosion . . . . .                      | 152.7   | 0.3585 m. | 20.3°C.      |
| After absorption with $\text{KOH}$ .           | 148.9   | 0.3665 m. | 18.9°C.      |

210. Find the percentage volume of  $\text{H}_2\text{S}$ ,  $\text{CO}_2$ ,  $\text{N}$ ,  $\text{CO}$ , and  $\text{CH}_4$  present in a fumarolle-gas giving on analysis :—

|  | Volume. | Pressure. | Temperature. |
|--|---------|-----------|--------------|
| Gas taken . . . . .                          | 94.0    | 0.6945 m. | 13.3°C.      |
| After absorption of $\text{H}_2\text{S}$ . . | 73.7    | 0.6728 m. | 13.6°C.      |
| After absorption of $\text{CO}_2$ . .        | 46.1    | 0.6502 m. | 13.6°C.      |
| Gas decanted into eudiometer                 | 96.8    | 0.3093 m. | 13.1°C.      |
| After addition of air . . . .                | 243.0   | 0.4534 m. | 13.6°C.      |
| After explosion . . . . .                    | 172.0   | 0.3839 m. | 13.7°C.      |
| After treatment with $\text{KOH}$ .          | 168.6   | 0.3902 m. | 13.1°C.      |

211. From the tabulated data, calculate the percentage amount of nitrogen present in each body analysed, and give the volumes, reduced to standard conditions, of the nitrogen and nitric oxide respectively in each case.

*Measured in Frankland and Ward's apparatus.*

| Substance taken. | Volume in c.c. | Temperature. | Pressure N + NO | Pressure N. |
|------------------|----------------|--------------|-----------------|-------------|
| A. 0.1263 gm.    | 13.79          | 18°C.        | 451 mm.         | 423 mm.     |
| B. 0.0832 "      | 22.32          | 20°C.        | 411 "           | 378 "       |
| C. 0.0827 "      | 22.32          | 24°C.        | 416 "           | 373 "       |
| D. 0.0856 "      | 22.32          | 29°C.        | 396 "           | 375 "       |
| E. 0.0878 "      | 13.5           | 19°C.        | 597 "           | 582 "       |
| F. 0.1259 "      | 9.02           | 20°C.        | 408 "           | 405 "       |

212. Find the composition of marsh gas from the figures given below, obtained by Thomas's modification of Frankland and Ward's apparatus.

Temperature constant at  $15.4^{\circ}\text{C}$ .

Gas taken at 118.5 mm. pressure.

After addition of oxygen, pressure = 357.8 mm.

Pressure after explosion = 121.12 mm.

Pressure after absorption of  $\text{CO}_2$  = 2.32 mm.

213. Calculate the percentage of  $\text{CO}_2$  by volume contained in a sample of air which gave the accompanying data—10 c.c. of baryta solution agitated in a flask, containing the air, of 618 c.c. capacity, required 6.0 c.c. of normal oxalic acid for neutralization, of which 1 c.c. equals 1 c.c. of  $\text{CO}_2$  at  $0^{\circ}\text{C}$ . and 760 mm.; bar. 726 mm., temp.  $21^{\circ}\text{C}$ . The same amount of baryta solution directly titrated with normal oxalic acid required 8.8 c.c.

214. To a solution of baryta sufficient alcoholic solution of phenolphthalein is added to produce a distinctly pink coloration; 1 c.c. of the solution = 0.104 c.c. carbon dioxide. A volume of 25 c.c. of the coloured solution becomes decolorized on the aspiration of 540 c.c. of air through it, owing to the absorption of  $\text{CO}_2$ ; find percentage of  $\text{CO}_2$  present.

215. An analysis of a specimen of coal-gas is made by (1) successive absorption of carbon dioxide, ethylene (propylene, butylene), benzene, oxygen, and carbon monoxide by means of Hempel's pipettes; (2) combustion of the hydrogen in a palladium-asbestos tube; (3) combustion of the methane by red-hot copper oxide with estimation of the carbon dioxide produced by titration. From the subjoined figures find the composition by volume of the sample analysed:

|  |           |
|--|-----------|
| Volume of gas employed . . . . .                         | 99.1 c.c. |
| (1) Volume after absorption by KOH . . .                 | 97.7 c.c. |
| Volume after treatment with Br water . .                 | 93.9 c.c. |
| Volume after treatment with fuming $\text{NO}_3\text{H}$ | 92.9 c.c. |
| Volume after alkaline pyrogallol absorption              | 92.6 c.c. |
| Volume after treatment with cuprous chloride . . . . .   | 86.5 c.c. |

- (2) Non-absorbable gas used for H estimation 40·6 c.c.  
 Non-absorbable gas + air . . . . . 99·0 c.c.  
 Volume after combustion. . . . . 65·7 c.c.

(3) Residue of 65·7 c.c. is burned by air and copper oxide, and  $\text{CO}_2$  titrated by baryta-water and oxalic acid.

Gas measures 65·7 c.c. at 736 mm. and  $20^\circ \text{C}$ .

Baryta-water, 1 c.c. = 1·04 c.c. oxalic acid = 1·04 c.c. methane.

Baryta-water employed . . . . . 50 c.c.

Oxalic acid required for re-titration . . 37·4 c.c.

216. 100 volumes of Manchester cannel gas contained 4·98 volumes of olefines, which yielded on combustion 13·93 volumes of carbon dioxide. Required the volumes of ethylene ( $\text{C}_2\text{H}_4$ ) and butylene ( $\text{C}_4\text{H}_8$ ) contained in the gas, and the value of the illuminating power of the gas expressed in percentages of ethylene.

## CALCULATION OF THE RESULTS OF ATOMIC WEIGHT DETERMINATIONS.

*The data required for these calculations, when not otherwise given, may be obtained from Table I. in the Appendix.*

217. DUMAS found, on heating copper oxide in a stream of dry hydrogen, that a certain weight of this substance lost 59·789 grams of oxygen, and yielded 67·282 grams of water. Calculate from these numbers the atomic weight of hydrogen.

218. Marignac obtained 314·894 grams of silver nitrate from 200 grams of silver. 14·110 grams of silver nitrate required 6·191 grams of potassium chloride for complete precipitation, and 10·339 grams of silver dissolved in nitric acid required 5·120 grams of ammonium chloride for precipitation. Calculate the atomic weight of nitrogen from these data.

219. Stas found that 91.462 grams of metallic silver, when heated in a stream of chlorine, yielded 121.4993 grams of pure silver chloride. Calculate from this the atomic weight of chlorine.

220. Stas found, after adding 7.25682 grams of potassium chloride to 10.51995 grams of silver dissolved in nitric acid, that 0.0194 grams of silver remained in solution. Calculate from these data the atomic weight of potassium.

221. Erdmann and Marchand obtained 109.6308 grams of mercury from 118.3938 grams of the red oxide. Calculate the atomic weight of mercury.

222. Calculate the atomic weight of carbon from each of the following analyses by Redtenbacher and Liebig of

|                   | Salt.           |                   | Silver. |
|-------------------|-----------------|-------------------|---------|
| 1. Silveracetate  | $C_2H_3AgO_2$   | 28.803 grams gave | 18.612  |
| 2. Silvertartrate | $C_4H_4Ag_2O_6$ | 16.220 „ „        | 9.6175  |
| 3. Silvermalate   | $C_4H_4Ag_2O_6$ | 25.898 „ „        | 16.059  |

223. Mallet found that 8.2144 grams of ammonia-alum dried by exposure to air at  $21^{\circ}$ — $25^{\circ}$  C. yielded 0.9258 gram of  $Al_2O_3$ . Taking the following atomic weights : O = 15.961 ; S = 31.966 ; N = 14.010 ; find the atomic weight of aluminium.

224. Mallet found that 6.9617 grams  $Al Br_3$  required 8.4429 grams of Ag for precipitation of the bromine ; if  $Ag = 107.649$  and  $Br = 79.754$  what is the atomic weight of Al as deduced from this result ?

225. 0.3697 gram of aluminium liberated 0.04106 gram of hydrogen on being dissolved in a strong solution of sodium hydrate ; find atomic weight of aluminium.

226. A determination of the atomic weight of titanium was made by finding the weight of pure silver required to precipitate the chlorine from an aqueous solution in which a bulb containing a known weight of  $TiCl_4$  had been broken. A quantity of the pure silver nearly sufficient was in each experiment first converted into nitrate and then mixed with the titanium solution, the precipitation was finished by addition from a burette of a centinormal



solution of  $\text{AgNO}_3$ . Find the atomic weight of Ti from the annexed data in each case. (Take  $\text{Ag} = 6\cdot7456$ ,  $\text{Cl} = 2\cdot21586$ ,  $\text{H} = 0\cdot06265$ ,  $\text{O} = 1$ .)

| Corrected weight of $\text{TiCl}_4$ used. | Weight of silver weighed out. | Weight of silver added from burette. |
|---|-------------------------------|--------------------------------------|
| 2·43275 grams.                            | 5·49288 grams.                | 0·03509 gram.                        |
| 5·42332 "                                 | 12·30669 "                    | 0·01591 "                            |
| 3·59601 "                                 | 8·15960 "                     | 0·01501 "                            |
| 3·31222 "                                 | 7·44102 "                     | 0·08619 "                            |
| 4·20093 "                                 | 9·52445 "                     | 0·02234 "                            |

227. A series of experiments made for the purpose of determining the atomic weight of gold consisted in finding the ratio existing between the quantities of  $\text{KBr}$  and metallic  $\text{Au}$  remaining on the decomposition of potassium bromo-aurate by heat.

Taking the equivalent of  $\text{H}$ ,  $0\cdot06265$ ,  $\text{K}$ ,  $2\cdot44523$ , and  $\text{Br}$   $4\cdot99634$ , when  $\text{O} = 1$ , calculate the atomic weight of gold from the following data :

| <i>Weight of Au.</i> |   | <i>Weight of KBr.</i> |
|----------------------|---|-----------------------|
| 6·19001              | : | 3·73440.              |
| 4·76957              | : | 2·87715.              |
| 4·14050              | : | 2·49822.              |
| 3·60344              | : | 2·17440.              |
| 3·67963              | : | 2·21978.              |
| 4·57757              | : | 2·76195.              |
| 5·36659              | : | 3·23821.              |
| 5·16406              | : | 3·11533.              |

228. The atomic weight of silicon has been determined by estimating the amount of  $\text{SiO}_2$  obtained on treatment of known weights of  $\text{SiBr}_4$  with water.

From the following table of results, find the ratio  $\text{Si} : \text{H}$ , taking  $\text{H} = 0\cdot06265$ , and  $\text{Br} = 4\cdot99721$ , ( $\text{O} = 1$ ).

| <i>Weight of <math>\text{Si Br}_4</math> in vacuo.</i> |  | <i>Weight of <math>\text{Si O}_2</math> in vacuo.</i> |
|--|--|---|
| 9·63007 grams.   |  | 1·67070 grams.  |
| 12·36099 "   |  | 2·14318 "   |
| 12·98336 "   |  | 2·25244 "   |
| 9·02269 "  |  | 1·56542 "   |
| 15·38426 "   |  | 2·66518 "   |

229. Taking the atomic weights of  $O = 15.96$ ,  $N = 14.02$ ,  $H = 1$ , find the mean atomic weight of chromium from the given experimental results.

| <i>Corrected weight of<br/>(NH<sub>4</sub>)<sub>2</sub>Cr<sub>2</sub>O<sub>7</sub>.</i> | <i>Corrected weight of Cr<sub>2</sub>O<sub>3</sub><br/>obtained therefrom.</i> |
|---|--|
| 1.01275   | 0.61134  |
| 1.08181   | 0.65266  |
| 1.29430   | 0.78090  |
| 1.13966   | 0.68799  |
| 0.98778   | 0.59595  |
| 1.14319   | 0.68987  |

230. From the following readings given by Ramsay, showing the volume of hydrogen obtained by means of pure zinc, calculate the equivalent of zinc ( $H = 1$ ).

| Weight, in a vacuum,<br>of the zinc used. | Reduced volume<br>of hydrogen. | Reduced<br>pressure. | Thermometer<br>reading, C. |
|---|--------------------------------|----------------------|----------------------------|
| 3.299584                                  | 1216.86 cc.                    | 729.18 mm.           | 10.54                      |
|   | 1219.64 "                      | 727.78 "             | 10.54                      |
|   | 1222.73 "                      | 725.78 "             | 10.54                      |
|   | 1225.62 "                      | 724.08 "             | 10.54                      |
|   | 1233.05 "                      | 719.72 "             | 10.53                      |
|   | 1230.54 "                      | 721.10 "             | 10.48                      |
|   | 1228.02 "                      | 722.65 "             | 10.48                      |

## CALCULATIONS INVOLVED IN INDIRECT ANALYSIS.

There are three main types of Indirect Analysis, namely :—

(1) *The method of substitution*; an equivalent amount of some other radicle (or substance) is substituted for the radicle we wish to determine and is then estimated directly; for instance we may determine free Cl by adding to its solution KI when KCl is formed and free I, equivalent in amount to the Cl present, remains and can be estimated directly.

(2) *The residue method*; the body in which the radicle occurs undergoes a definite chemical change when acted upon by a known amount in excess of some reagent, and the excess of reagent is determined.

(3) *The method depending on the numerical differences between molecular weights*; with a mixture of two salts, differing considerably in molecular weight, but possessing a common constituent, it is possible from the estimation of the common radicle to calculate the quantities of each of the other radicles present in the mixture.

#### EXAMPLES.

(1) To 50 c.c. of a solution of Cl, an excess of potassium iodide solution was added; the liberated I was then estimated by means of a standard solution of  $\text{Na}_2\text{S}_2\text{O}_3$  using starch solution to indicate the end of the reaction. 1 c.c.  $\text{Na}_2\text{S}_2\text{O}_3$  solution = 0.0127 gram I, and 22.5 c.c. of this solution were used; what was the strength of the Cl solution in grams per c.c.?

Iodine set free =  $0.0127 \times 22.5$  gram.

which is equivalent to  $\frac{0.0127 \times 22.5 \times 35.37}{126.54}$  gram of Cl.

which was the weight of Cl contained in 50 c.c.

Hence, weight of Cl per c.c.

$$= \frac{0.0127 \times 22.5 \times 35.37}{50 \times 126.54} = 0.001597 \text{ gram.}$$

(2). 0.2815 gram of calcite was dissolved in 30 c.c. of normal  $\text{HNO}_3$ , and the excess of acid determined by normal  $\text{NaOH}$  of which 24.43 c.c. were required; what percentage of  $\text{CO}_2$  did the sample contain?

The  $\text{HNO}_3$  neutralized by the  $\text{CaCO}_3$  present in the calcite was  $30.00 - 24.43 = 5.57$  c.c.

126 grams  $\text{HNO}_3$  are equivalent to 44 grams  $\text{CO}_2$ .

Hence, amount of  $\text{CO}_2$  present was :—

$$\frac{0.063 \times 5.57 \times 44}{126} \text{ gram.}$$

$$\text{and hence \% of } \text{CO}_2 = \frac{0.063 \times 5.57 \times 44 \times 100}{126 \times 0.2815} = 43.53.$$

(3). Two grams of a mixture of barium carbonate and calcium carbonate evolve 0.67 gram of carbon dioxide ; find the percentages of Ca and Ba present in the mixture.

Taking the following atomic weights,—Ca, 40.0 ; Ba, 137.2 ; C. 12.0 ; O. 16 ; we have

$\text{BaCO}_3$  contains  $\frac{44}{197.2}$  of its weight of  $\text{CO}_2$ , and  $\text{CaCO}_3$  contains  $\frac{44}{100}$  of its weight of  $\text{CO}_2$ .

Let  $x$  be the weight of  $\text{BaCO}_3$  in the mixture taken, then  $(2 - x)$  is the weight of  $\text{CaCO}_3$  present.

$$\text{CO}_2 \text{ present is } \frac{44}{197.2} x + \frac{44}{100} (2 - x) = 0.67.$$

$$\text{hence, } \frac{44(197.2 - 100)}{100 \times 197.2} \cdot x = 0.21.$$

$$\therefore x = 0.968 \text{ gm. Ba CO}_3.$$

$$\text{and } 2 - x = 2 - 0.968 = 1.032 \text{ gm. Ca CO}_3.$$

$$\text{Whence \% of Ba in mixture} = \frac{0.968 \times 137.2 \times 100}{197.2 \times 2} = 33.67.$$

$$\text{and \% of Ca} = \frac{1.032 \times 40 \times 100}{100 \times 2} = 20.64.$$

#### QUESTIONS.

231. 0.2151 gram of uric acid was heated with soda-lime and the evolved  $\text{NH}_3$  absorbed in  $\text{HCl}$ . The  $\text{NH}_4\text{Cl}$  was evaporated to dryness and redissolved, the  $\text{Cl}$  being then thrown down as  $\text{AgCl}$ , of which 0.7390 gram was obtained ; what percentage of nitrogen did the sample of uric acid contain ?

232. 25 c.c. of a solution, containing 0.2105 gram of a copper alloy in the form of sulphates, was neutralized with  $\text{Na}_2\text{CO}_3$  and then rendered acid by acetic acid; to the acidulated solution an excess of freshly prepared potassium iodide solution was added and the liberated iodine titrated by a standard  $\text{Na}_2\text{S}_2\text{O}_3$  solution; 31.29 c.c. were required for the reaction. 25.22 c.c. of the thiosulphate solution were found to be equivalent to 25 c.c. of iodine solution of which 1 c.c. = 0.006313 gram of copper. Calculate the percentage amount of copper present in the alloy.

233. 0.5005 gram of a sample of calcite, was weighed out, dissolved in dilute  $\text{HCl}$  and precipitated as calcium oxalate; the washed precipitate was treated with dilute sulphuric acid and the solution titrated with potassium permanganate solution of which 1 c.c. = 0.0056 gram of iron; 100.08 c.c. of the permanganate were decolorized. What was the percentage of calcium in the mineral?

234. In an estimation of nitrogen by the soda-lime method, 0.2102 gram of benzamide was taken and the evolved ammonia absorbed in  $\frac{\text{N}}{2}$  sulphuric acid solution, 25 c.c. being taken; the residual acid required 21.517 c.c. of  $\frac{\text{N}}{2}$   $\text{NaOH}$  for neutralization. What was the percentage amount of nitrogen in the benzamide?

235. The subjoined data were obtained in an estimation of  $\text{NH}_3$  in  $(\text{NH}_4)_2\text{SO}_4$  by the method of distillation with soda-lime in the wet way.

Weight of ammonium sulphate taken = 0.3200 gram.

Amount of  $\text{H}_2\text{SO}_4$  solution taken = 60 c.c.

1 c.c. of acid solution = 0.855 c.c.  $\frac{\text{normal}}{2}$   $\cdot$   $\text{NaOH}$  sol.

41.7 c.c. of  $\frac{\text{N}}{2}$  soda just neutralized the residual acid.

Calculate from these data the percentage amount of ammonia in ammonium sulphate.

236. One hundred cubic centimetres of a semi-normal solution of sodium carbonate were added to 100 c.c. of a neutral solution containing copper sulphate. After filtration, the residual  $\text{Na}_2\text{CO}_3$  was determined by means of  $\frac{N}{2}$  sulphuric acid, of which 27 c.c. were required. What weight of  $\text{Cu SO}_4$  in grams was present in each litre of the solution?

237. The following results, obtained in an analysis of Rochelle salt, give sufficient data for the estimation of K and Na in the sample used ; find the percentage of each of these elements present.

|  |              |
|--|--------------|
| Weight of salt taken . . . . .             | 0.7012 gram. |
| Weight of mixed alkaline chlorides . . . . | 0.3305 „     |
| Weight of Ag Cl obtained . . . . .         | 0.7129 „     |

238. From 0.9330 gram of a mixture of sodium chloride and iodide, 0.9066 gram of sodium sulphate is obtained. What weights of the sodium chloride and sodium iodide are there in the weight of mixture taken ?

(Take Na = 23, S = 32, O = 16, Cl = 35.5 I, = 127.)

## GENERAL ANALYTICAL QUESTIONS.

239. CALCULATE the formula of a salt containing sodium and chlorine which yielded the following numbers on analysis :—

(a) 0.1998 gram of the salt gave  
 0.4865 gram of silver chloride, and  
 0.0032 „ metallic silver.

(b) 0.9543 gram of the salt gave  
 1.1584 grams of sodium sulphate.

240. 0.3951 gram of a substance supposed to be arsenic pentoxide was dissolved in dilute ammonia, and precipitated as magnesium-ammonium-arsenate. After drying at  $110^\circ$  the precipitate weighed 0.6544 gram. Was the substance  $\text{As}_2\text{O}_5$ ?

241. The mineral nontronite gave on analysis the following numbers. Calculate its formula.

|                                  |                         |
|----------------------------------|-------------------------|
| 1.4155 grams of the mineral gave | 0.5711 grams of silica. |
| and                              | 0.5157 „ ferric oxide.  |
| „                                | 0.0380 „ lime.          |
| 1.1205 „ lost on drying          | 0.2311 „ water.         |

242. 100 grams of a mixture of potassium and sodium chlorides have furnished 164.1 grams of potassium-platinum chloride. What is the composition of the mixture?

243. Calculate the formula of thallium perchlorate from the following determination:—0.1831 gram of salt gave 0.2476 gram of the double chloride of platinum and thallium.

244. Calculate the percentage amount of chlorine contained in vanadyl trichloride of which 3.9490 grams added to 7.383 grams of silver dissolved in nitric acid required 3 cubic centimetres of centesimal HCl solution for complete precipitation according to Gay-Lussac's method.

!245. Two equal volumes of a liquid found to contain an oxygen compound of bromine were completely reduced with sulphurous acid, the excess of which was removed by boiling: in one portion the sulphuric acid formed was estimated as barium salt, and in the other the bromine was weighed as silver bromide. Analysis gave: weight of  $\text{Ba SO}_4 = 0.402$  gram; weight of silver bromide, 0.3240 gram. Required the composition of the oxide of bromine.

246. 1.2185 grams of perchloric acid yielded 1.6785 grams of dry potassium salt: of this salt 0.9660 gram lost 0.444 gram on heating, and the residue required 0.744 gram of pure silver for complete precipitation. Required the percentage amount of acid contained in the quantity taken. (Roscoe.)

!247. Required the percentage of real acid contained in 1.483 grams of aqueous acetic acid, which evolved 0.427 gram of carbonic acid on adding it to bicarbonate of sodium.

248. 2.122 grams of aqueous formic acid required for neutralization 36.3 cubic centimetres of soda solution, of

which each cubic centimetre contained ( $0.9025 \times 31$ ) milligrams of soda. Required the percentage of pure acid contained in the liquid.

249. Calculate the volume of carbonic acid in 10,000 volumes of sea-air, from the following numbers, obtained by Pettenkofer's method :—

1 cubic centimetre of oxalic acid solution = 1 mgrm.  $\text{CO}_2$ .  
50 cubic centimetres of baryta water = 55.18 cubic centimetres of oxalic acid solution.

Capacity of flask used, 4815 cubic centimetres. Temp. of air  $13^\circ 9$ . Bar. 753.1 mm.

50 cubic centimetres of baryta solution taken : of this 25 cubic centimetres after the experiment required 26.29 cubic centimetres of oxalic acid solution for neutralization.

250. The following numbers express the amount of the constituents in 1,000 grams of the water of the Irish Channel :—

|   |          |
|---|----------|
| 1. Chlorine . . . . .                         | 18.62650 |
| 2. Bromine . . . . .                          | .06133   |
| 3. Sulphuric acid ( $\text{SO}_4$ ) . . . . . | 2.59280  |
| 4. Lime (total) . . . . .                     | 0.57512  |
| 5. Calcium carbonate . . . . .                | 0.04754  |
| 6. Magnesia . . . . .                         | 2.03233  |
| 7. Potassium . . . . .                        | 0.39131  |
| 8. Sodium . . . . .                           | 10.40200 |
| 9. Ferric oxide . . . . .                     | .00465   |
| 10. Ammonia . . . . .                         | .00011   |
| 11. Nitric acid . . . . .                     | .00156   |

|                          |                 |
|--------------------------|-----------------|
| Total fixed constituents | <u>33.83855</u> |
|--------------------------|-----------------|

Calculate the composition of the saline matter of the water on the following assumption : That the sodium, potassium, and ammonium are combined with chlorine, the excess of chlorine being united to magnesium. The bromine and nitric acid are also to be united to the magnesium. The sulphuric acid exists in combination with lime, the excess being united to magnesia. The ferric oxide exists as ferrous carbonate.

! 251. Calculate the illuminating power of a gas flame burning 5 cubic feet per hour, expressed in candles burn-



ing 120 grains (7.79 grams) of sperm per hour, from the following data :—

Rate at which gas issues = 4.8 cubic feet per hour.

Consumption of standard candle in 10 minutes = 1.38 grams.

Readings on the photometer scale for each minute of observation :—

(1), 27. (2), 22.5. (3), 17. (4), 21. (5), 18. (6), 19.  
(7), 19. (8), 20. (9), 19. (10), 21.

252. 0.5637 grams of the barium salt of an organic acid, obtained by the action of carbonic acid on  $C_6H_4BrC_2H_5$  in presence of sodium, lost, on drying at  $120^\circ C.$ , 0.0430 gram of water, and gave 0.2733 gram barium sulphate. Required the formula of the salt.

! 253. 4.826 grams of a nitrogenous organic body yielded, after heating with soda-lime, 1.532 grams of the double chloride of platinum and ammonium. Required the percentage of nitrogen contained in the organic substance.

! 254. Required the percentage composition, observed and calculated vapour density, and formula of a body which gave the following analytical results :—

(a) 0.4245 gram yielded

0.5670 gram of carbonic acid, and  
0.3025 „ water.

(b) 0.1810 gram yielded.

0.3855 gram of silver chloride, and  
0.0165 „ metallic silver.

(c) Determination of vapour density according to Gay-Lussac's method :—

Weight of substance employed, 0.0893 gram.

Temperature of the air,  $8^\circ C.$  Height of barometer,  
739 mm.

Temperature of vapour,  $50^\circ C.$  Volume, 46.2 cubic  
centimetres.

Difference of level, 140.5 mm. Coefficient of expansion of mercury = 0.0001815.

Coefficient of cubical expansion of glass, 0.0000262.

255. 1.5055 grams of a mixture of sodium and potassium chlorides gave 3.4222 grams of silver chloride. Calculate the relative amounts of the two chlorides.

256. 1.2060 grams of a mixture of sodium bromide and sodium chloride gave, on complete precipitation by silver nitrate, 2.6554 grams of mixed silver chloride and bromide, which, on reduction, yielded 1.8418 grams of metallic silver. Calculate the proportion of chloride and bromide.

## SOLUTION OF GASES IN LIQUIDS.

GASES fall into two groups when considered in relation to their solubility in liquids :—

(1). Those gases completely expelled from the solvent by raising its temperature or reducing the pressure to which it is subjected.

(2) Other gases.

I. In group (1), the amount of gas absorbed depends upon :—

I. The nature of the gas and of the absorbing liquid.

II. The actual pressure of the gas considered.

Henry's Law :—The quantity of any gas absorbed by a given quantity of a liquid is proportional to the pressure.

III. The temperature. Volume absorbed decreases with the increase of temperature ; it may be expressed by means of an empirical formula of the form  $V = a - bt + ct^2$ , where  $a$ ,  $b$ ,  $c$  are constants for each gas and  $t$  is the temperature.

The absorption-coefficient of a gas is a number which expresses the ratio of the volume of the gas, measured at 0° C. and the pressure of absorption, absorbed by the liquid at the temperature of observation to the volume of

the absorbing liquid. In a mixture of gases, each component behaves as if it alone were present under the partial pressure which is exerted by itself.

### EXAMPLE.

It is required to calculate the absorption coefficient of nitrogen dissolved in water at  $19^{\circ}\text{C}$ . from the appended data (Bunsen).

#### I. *Observations before Absorption.*

|   |                              |
|---|------------------------------|
| Lower level of mercury in outer cylinder            | $a = 423.6$ mm.              |
| Upper level of mercury in absorption tube . . . . . | $b = 124.1$ „                |
| Height of barometer . . . . .                       | $p = 746.9$ „                |
| Temperature of absorptiometer . . . . .             | $t = 19.2^{\circ}\text{C}$ . |
| Temperature of barometer . . . . .                  | $T = 19.0^{\circ}\text{C}$ . |

#### II. *Observations after Absorption.*

|   |                                |
|---|--------------------------------|
| Lower level of mercury in outer cylinder            | $a_1 = 352.2$ mm.              |
| Upper level of mercury in absorption tube . . . . . | $b_1 = 350.7$ „                |
| Water level in absorption tube . . . . .            | $c_1 = 65.5$ „                 |
| Water level in outer cylinder . . . . .             | $d_1 = 8.0$ „                  |
| Height of barometer . . . . .                       | $p_1 = 746.3$ „                |
| Temperature of absorptiometer . . . . .             | $t_1 = 19.0^{\circ}\text{C}$ . |
| Temperature of barometer . . . . .                  | $T_1 = 18.9^{\circ}\text{C}$ . |

#### III. *Tabular Data.*

Volumes, according to the calibration table, of: -

|   |                  |
|---|------------------|
| Gas taken. mark $b = 124.1$ mm. . . . .                               | $V = 34.90$ .    |
| Tube above $b_1 = 350.7$ mm. . . . .                                  | $200.04$ .       |
| Tube above $c_1 = 65.5$ mm., remaining gas. . . . .                   | $V_1 = 17.67$ .  |
| Hence water used for absorption. . . . .                              | $(h) = 182.37$ . |
| Coefficient of expansion of mercury for $1^{\circ}\text{C}$ . . . . . | $= 0.00018$ .    |

$$\text{The absorption coefficient } a = \frac{1}{h} \left( \frac{VP}{P_1} - V_1 \right)$$

$P$  and  $P_1$  being the pressures of the dry gas before and after absorption respectively,  $V$  and  $V_1$  being the corresponding volumes of gas reduced to  $0^\circ \text{C}$ .

$P = p$  reduced to  $0^\circ \text{C}$ . —  $(a - b)$  reduced to  $0^\circ \text{C}$ . — vapour pressure of water at  $19^\circ \text{C}$ .

$$= (744.4 - 298.5 - 16.6) \text{ mm.} = 429.3 \text{ mm.}$$

$P_1 = p_1$  reduced to  $0^\circ \text{C}$ . —  $(a_1 - b_1)$  reduced to  $0^\circ \text{C}$ .  
+  $\{(a_1 - b_1) + (c_1 - d_1)\}$  reduced to equivalent mercury column at  $0^\circ \text{C}$ . — vapour pressure of water at  $19^\circ \text{C}$ .

$$= (743.8 - 1.5 + 4.4 - 16.3) \text{ mm.} = 730.4 \text{ mm.}$$

$$V = v \cdot \frac{1}{(1 + 0.00367 \cdot 19.2)} = 34.90 \cdot \frac{1}{1 + 0.00367 \cdot 19.2} = 32.608.$$

$$V_1 = v_1 \cdot \frac{1}{(1 + 0.00367 \cdot 19)} = 17.67 \cdot \frac{1}{1 + 0.00367 \cdot 19} = 16.52.$$

$$\text{Hence } a = \frac{1}{182.37} \left( \frac{32.608 \times 429.3}{730.4} - 16.52 \right) = 0.01448.$$

#### QUESTIONS.

257. The absorption coefficient of nitrogen dissolved in water is 0.0152 at  $12.6^\circ \text{C}$ .; what volume of the gas measured at  $0^\circ \text{C}$ . and 760 mm. pressure is absorbed by one litre of water at  $12.6^\circ \text{C}$ . at each of the pressures :— 1000 mm., 748.2 mm., 391 mm., and 14.3 mm.?

258. What is the volume of nitrogen absorbed in each case in question 257, measured at the temperature and pressure of the experiment? What is the weight of the gas absorbed in each case?

259. The absorption coefficient of hydrogen dissolved in water is represented by the interpolation formula  $a = 0.0215286 - 0.00019216t + 0.0000017228t^2$  : what quantities of the gas measured ( $a$ ) under the experimental conditions, ( $b$ ) under standard conditions,

will be given off on boiling 325 c.c. of the solution made by agitating water in hydrogen (*A*) at  $10^{\circ}$  C. and 750 mm., (*B*) at  $14^{\circ}$  C. and 767 mm., (*C*) at  $18^{\circ}$  C. and 732 mm.?

260. The coefficient of absorption of carbon dioxide in water is found to be  $a = 1.7967 - 0.07761t + 0.0016424t^2$ ; find the coefficients for  $t = 4.4^{\circ}$  C.,  $8.4^{\circ}$  C.,  $13.8^{\circ}$  C.,  $16.6^{\circ}$  C.,  $19.1^{\circ}$  C., and  $22.4^{\circ}$  C.

261. The coefficient of absorption of hydrogen in alcohol is given by the interpolation formula  $a = 0.06925 - 0.0001487t + 0.000001t^2$ ; find the values of the coefficient at  $1^{\circ}$ ,  $5^{\circ}$ ,  $11.4^{\circ}$ ,  $14.4^{\circ}$ , and  $19.9^{\circ}$  C., and compare each value with the corresponding value of the coefficient for water as given in question 259.

262. Find an interpolation formula expressing the variation of the coefficient of absorption of carbonic oxide in water with alteration of temperature, the coefficients found by experiment being :—at  $5.8^{\circ}$ , 0.028636; at  $8.6^{\circ}$ , 0.027125; at  $17.4^{\circ}$ , 0.023854; at  $18.4^{\circ}$ , 0.023147; at  $9^{\circ}$ , 0.026855; and at  $22^{\circ}$ , 0.022907.

263. At  $23^{\circ}$  C. the absorption-coefficient of oxygen in water is 0.03402, that of nitrogen is given by the expression  $a = 0.020346 - 0.00053887t + 0.000011156t^2$ ; what will be the percentage composition by volume of the gas mixture obtained by boiling water previously saturated with air at  $23^{\circ}$  C.? (Air :—N, 79.1; O, 20.9.)

264. A litre of water saturated with carbon dioxide at  $4.4^{\circ}$  C. and 748 mm. is shaken up with a litre of nitrogen at  $23^{\circ}$  C. and 760 mm.; the temperature of the whole being now  $23^{\circ}$  C., what is the composition of the gas remaining over the solution,  $a$  for nitrogen being taken as in question 263, and for  $\text{CO}_2$  being equal to  $1.7967 - 0.07761t + 0.0016424t^2$ ?

265. A mixture of hydrogen and carbon dioxide is agitated with 356.4 c.c. of water at  $5.5^{\circ}$  C., volume of gas before absorption reduced to  $0^{\circ}$  C. = 171.29 c.c. and pressure = 0.5368 m.; vol. of gas after absorption at  $0^{\circ}$  C = 119.61 c.c., and its pressure = 0.6809 m.;  $a$  for H = 0.0193, for  $\text{CO}_2 = 1.4199$ ; what is the percentage composition of the original mixture?

## SOLUBILITY OF SOLIDS IN LIQUIDS. MOLECULAR WEIGHT AND THE LOWERING OF THE FREEZING-POINT OF SOLUTIONS.

THE solubility of solids in liquids does not admit of being represented by any simple law; the alteration of the solubility with temperature may generally be expressed by an equation of the form  $x = a + bt + ct^2 + dt^3$ , where  $a, b, c, d$  are constants for each set of substances considered, and  $t$  is the temperature.

As these constants have only been determined in a few cases, the consideration of problems arising in connection therewith does not fall within the scope of this book.

It has been found that substances dissolved in any solvents which solidify at attainable temperatures cause a lowering of the freezing-point according to the following law:—

If the molecular weight (in terms of any unit) of any substance be dissolved in 100 times the molecular weight (in terms of the same unit) of any liquid, the freezing-point of the latter is lowered by an amount always very near to  $0.63^\circ \text{C}$ .

Let  $A$  be the coefficient of lowering of the temperature of solidification (lowering produced by one gram dissolved in 100 grams of solvent),  $M$  be the molecular weight of the dissolved compound,  $T$  be the molecular lowering of the freezing-point (that produced by the molecular weight in grams of the substance dissolved in 100 grams of the solvent); then  $MA = T$ , and  $M = \frac{T}{A}$ .

If  $P$  be the weight of the solvent,  $P'$  the weight of the dissolved body,  $K$  the lowering of the freezing-point given by experiment, we have

$$A = K \cdot \frac{P}{P' \times 100}.$$

And hence  $M = \frac{T(P' \times 100)}{PK}$

If  $M'$  be the molecular weight of the solvent employed, then  $T = M' \times 0.63$  very nearly, with the exception of the solvent water.

$T$  has been determined by numerous experiments for the commoner solvents; its mean value for :

Acetic acid = (18.0 in a few cases), 38.6.

Formic acid = 27.7.

Benzene = 50.0.

Nitrobenzene = 70.7.

Water =  $\begin{cases} 18.5 \text{ (for organic substances, some salts of} \\ \text{diad metals, all the feeble bases and acids).} \\ 37 \text{ (for alkaline and alkaline earthy salts, and} \\ \text{all the strong acids and bases).} \end{cases}$

#### EXAMPLE.

The freezing-point of a sample of acetic acid was found to be  $16.490^\circ \text{C.}$ ; taking 62.014 grams of this acid and adding thereto 0.2540 gram of pure propionic acid, the solidifying point of the mixture is found to be  $16.277^\circ \text{C.}$  What is the molecular weight of propionic acid?

The observed lowering of the freezing-point is

$$16.490 - 16.277 = 0.213^\circ = K,$$

the weight of solvent  $P = 62.014$  gram, weight of dissolved body  $P' = 0.2540$  gram, and  $T = 38.6$  for acetic acid, hence

$$M = \frac{38.6 (0.2540 \times 100)}{62.014 \times 0.213} = 74.2$$

(Calculated molecular weight of  $\text{C}_2\text{H}_5\text{COOH} = 74)$

#### QUESTIONS.

266. If the molecular lowering of the freezing-point of acetic acid,  $16.75^\circ \text{C.}$ , be 43 in the case of benzoic acid, what is the temperature of solidification of a 4 per cent. solution?

267. Plot out a curve showing the relation between concentration and  $K_f$  in the case of ethyl formate dissolved in acetic acid,

| <i>Percentage of Ethyl Formate.</i> | <i>Observed <math>K_f</math>.</i> |
|-------------------------------------|-----------------------------------|
| 0.1977.                             | 0.101° C.                         |
| 0.3971.                             | 0.212° C.                         |
| 0.5935.                             | 0.315° C.                         |
| 0.9692.                             | 0.511° C.                         |
| 1.3907.                             | 0.758° C.,                        |

and find the mean molecular weight of the ethyl formate as given by this series of experiments.

268. Find the coefficient of lowering of the freezing-point of acetic acid by ethyl formate from the data of the preceding question.

269. What percentage of methyl acetate has been added to a sample of acetic acid freezing originally at 16.52° C. and after addition of the ester at 15.619° C.?

270. By what amounts should the freezing-point of benzene be lowered in 5 per cent. solutions of each of the following bodies—toluene, xylene, and anthracene?

271. Taking 56.7 gram of acetic acid freezing at 16.52° C. and adding methyl acetate in successive quantities as follows: (1) 0.0725 gram, (2) 0.0970 gram, (3) 0.0821 gram, (4) 0.1192 gram, the freezing-points after each addition are observed to be (1) 16.452° C., (2) 16.363° C., (3) 16.282° C., and (4) 16.177° C. respectively; what is the molecular weight of methyl acetate found from each observation?

272. What should be the normal molecular lowering of the freezing-point in the case of (a) anthracene, (b) sodium, (c) tin?

273. 6 grams of anhydrous magnesium sulphate are dissolved in 100 grams of water; the observed depression of the freezing-point is 0.958° C. Taking the value of  $T$  to be 37, which of the following formulæ most probably represents the state of the dissolved salt, (a)  $\text{MgSO}_4$ : (b)  $\text{MgSO}_4 \cdot 7\text{H}_2\text{O}$ ?



274. It has been found that the latent heat of fusion of a solvent is connected with the molecular lowering of its freezing-point as shown in the formula,

$$T = 0.02 \cdot \frac{(\text{absolute temperature})^2}{\text{latent heat of fusion}}.$$

The freezing-point of ethylene dibromide being  $7.9^{\circ}\text{C}$ ., and the molecular depression of its freezing-point  $117.9$ , find its latent heat of fusion.

275. The value of  $T$  for water is  $18.5$ , for formic acid  $27.7$ , and for acetic acid  $38.6$ , when organic substances are dissolved in each solvent. What inference may be drawn as to the relative complexity of the molecules of each of these solvents?

276. What conclusion would you draw as to the molecular weight of nitrogen tetroxide from the following data?

(a)  $0.5269$  gram of  $\text{CHCl}_3$  introduced into  $17.3046$  grams of nitrogen tetroxide lowers the freezing-point of the latter by  $1.06^{\circ}$ .

(b) Similarly  $0.4931$  gram of  $\text{C}_6\text{H}_5\text{Cl}$  mixed with  $16.7650$  grams of nitrogen tetroxide lowers its freezing-point  $1.09^{\circ}$ .

277. Find the molecular weight of gold, from the figures below showing the effect of Au in lowering the freezing-point of Na. (Take  $T = 104$ ).

| Weights of Na. | Weights of Au<br>added in<br>succession. | Freezing-point. |
|----------------|--|-----------------|
| 20.425         | —  | 97.44           |
| (a) "          | 2.1                                      | 91.99           |
| (b) "          | 1.316                                    | 88.59           |

278. Plot out a curve to show the variation of the molecular lowering of the freezing-point with concentration, using the data obtained by Haycock for mercury dissolved in sodium.

| Weight of Na. | Weights of Hg<br>added in<br>succession. | Freezing.point. |
|---------------|--|-----------------|
| 32'47         | —  | 97'47           |
| "             | 0'5605                                   | 96'6            |
| "             | 0'7410                                   | 95'38           |
| "             | 0'5740                                   | 94'46           |
| "             | 0'5170                                   | 93'64           |
| "             | 1'771                                    | 90'93           |
| "             | 4'950                                    | 83'35           |

## EXERCISES ON THE SPECIFIC HEAT, LATENT HEAT, AND ATOMIC HEAT OF SUBSTANCES.

THE capacity of a body for heat is measured by determining the number of units of heat required to raise that body one degree of temperature.

The *Specific Heat* of a body is the ratio of the quantity of heat required to raise that body one degree to the quantity required to raise an equal weight of water one degree.

*Latent Heat* is the quantity of heat which must be communicated to a body in a given state in order to convert it into another state without changing its temperature.

The *Atomic Heat* of an element is the product of its atomic weight into its specific heat; for the greater number of the elements, the mean value of this quantity is 6'40. This is expressed by Dulong and Petit in the form of a law, thus :—The atoms of all elementary bodies have exactly the same capacity for heat.

The following table by Regnault shows the specific heat of the more important elements and compound gases between 0°—100° C.

|                          |         |                            |         |
|--------------------------|---------|----------------------------|---------|
| Iron . . . . .           | 0'11379 | Sulphur . . . . .          | 0'20259 |
| Zinc . . . . .           | 0'09555 | Selenium . . . . .         | 0'08370 |
| Copper . . . . .         | 0'09515 | Tellurium . . . . .        | 0'05155 |
| Mercury . . . . .        | 0'03332 | Potassium . . . . .        | 0'16956 |
| „ (solid) . . . . .      | 0'03241 | Bromine (liquid) . . . . . | 0'11094 |
| Cadmium . . . . .        | 0'05669 | „ (solid -28°) . . . . .   | 0'08432 |
| Silver . . . . .         | 0'05701 | Iodine . . . . .           | 0'05412 |
| Arsenic . . . . .        | 0'08140 | Carbon . . . . .           | 0'24111 |
| Lead . . . . .           | 0'03140 | Phosphorus . . . . .       | 0'18870 |
| Bismuth . . . . .        | 0'03084 | Atmospheric Air . . . . .  | 0'2375  |
| Antimony . . . . .       | 0'05077 | Oxygen . . . . .           | 0'2175  |
| Tin . . . . .            | 0'05623 | Nitrogen . . . . .         | 0'2438  |
| Nickel . . . . .         | 0'10863 | Hydrogen . . . . .         | 3'4090  |
| Cobalt . . . . .         | 0'10696 | Carbon monoxide . . . . .  | 0'2479  |
| Platinum plate . . . . . | 0'03243 | Chlorine . . . . .         | 0'1214  |
| „ sponge . . . . .       | 0'03293 | Carbon dioxide . . . . .   | 0'2164  |
| Palladium . . . . .      | 0'05927 | Nitric oxide . . . . .     | 0'2238  |
| Gold . . . . .           | 0'03244 | Steam . . . . .            | 0'475   |

The following table, embodying the results obtained by Person, gives the latent heat of several bodies :—

|                             |       |                          |       |
|-----------------------------|-------|--------------------------|-------|
| Water . . . . .             | 79'25 | Bismuth . . . . .        | 12'64 |
| Phosphorus . . . . .        | 5'03  | Lead . . . . .           | 5'37  |
| Sulphur . . . . .           | 9'37  | Zinc . . . . .           | 28'13 |
| Sodium nitrate . . . . .    | 62'97 | Mercury . . . . .        | 2'83  |
| Potassium nitrate . . . . . | 47'37 | Steam . . . . .          | 537   |
| Sodium chloride . . . . .   | 40'70 | Alcohol vapour . . . . . | 208   |
| Tin . . . . .               | 14'25 | Ether vapour . . . . .   | 90    |

The heat required to raise the temperature of a kilogram of water through 1° C. is able to do work equivalent to the lifting of a kilogram weight through 425 metres. The *mechanical equivalent of heat* is 425 metre-kilograms.

A kilogram of water falling through a height of 425 metres, and having its motion suddenly arrested, would have its temperature raised 1° C.

## QUESTIONS.

279. The following quantities of water are mixed together :—

|             |    |        |
|-------------|----|--------|
| 1 kilogram  | at | 40° C. |
| 2 kilograms | „  | 30° „  |
| 3           | „  | 20° „  |
| 4           | „  | 5° „   |

Calculate the temperature of the mixture.

! 280. If one kilogram of mercury at 20° C. be mixed with one kilogram of water at 0°, the temperature of the mixture will be 0·634° C. Calculate the specific heat of mercury.

! 281. Determine the specific heat of mercury from the observation that when the same vessel is filled successively with water and mercury, and heated to the same temperature, the water and mercury cool through the same number of degrees in 10 minutes and 270 seconds respectively. The specific gravity of mercury being considered constantly at 13·6.

282. Calculate the specific heat of mercury from the following numbers obtained by Kopp, according to his method :—

|                                    |       |               |
|------------------------------------|-------|---------------|
| Temperature of mercury bath        | . .   | 51°·1 C.      |
| Initial temperature in calorimeter | . .   | 13°·41 „      |
| Final                              | „ „   | 16°·50 „      |
| Weight of water in calorimeter     | . .   | 26·945 grams. |
| Weight of mercury used             | . . . | 53°·015 „     |
| Thermal value of apparatus         | . . . | 0·651 „       |

283. Calculate the specific heat of phosphorus from the following determination by Kopp :—

|                                    |       |          |
|------------------------------------|-------|----------|
| Temperature of mercury bath        | . .   | 38°·8 C. |
| Initial temperature in calorimeter | . .   | 10°·05 „ |
| Final                              | „ „   | 13°·20 „ |
| Weight of water in calorimeter     | . .   | 26·95 „  |
| Weight of phosphorus employed      | . .   | 3·075 „  |
| Weight of water in tube            | . . . | 2·065 „  |

† 284. The specific heat of water is 4 times, and its density 770 times, that of air. Supposing a cubic mile of water to yield up one degree of its heat to a cold atmosphere, what quantity would 1000 cubic miles of the atmosphere be heated?

285. A bar of platinum weighing 150 grams is heated in a furnace until its temperature becomes constant, when it is thrown into a kilogram of water, the temperature of which it raises from  $15^{\circ}$  to  $20^{\circ}$ . Required the temperature of the furnace on the assumption that the specific heat of platinum is  $0.03308 + 0.0000042t$  between  $0^{\circ}$  and  $t^{\circ}$ . (Pouillet.)

286. A determination of the specific heat of iron made in the calorimeter of Lavoisier and Laplace yielded the following data. Calculate the specific heat of iron :—

|                               |               |        |
|-------------------------------|---------------|--------|
| Weight of iron taken . . .    | 100           | grams. |
| Weight of ice melted . . .    | 14.35         | "      |
| Initial temperature of iron . | $100^{\circ}$ | C.     |
| Latent heat of water . . .    | 79.25         |        |

287. The mechanical equivalent of heat is 425 metre-kilograms. What is this in foot-pounds?

288. From what height must a block of ice at  $0^{\circ}$  C. fall that the heat generated by its collision with the earth shall be just competent to melt it? From what height must it fall that the heat generated may be sufficient to convert it into steam?

289. If  $W_w$  = the number of scale divisions on a Bunsen's calorimeter equivalent to one gramme-degree unit of heat,  $T$  = the observed movement of the thread in scale divisions,  $G$  = the weight of substance taken and  $t$  its temperature, then  $\text{sp. ht.} = \frac{T}{W_w \cdot G \cdot t}$ . Find the sp. ht. of indium if  $G = 1.1514$ ,  $t = 99.82^{\circ}$  C.,  $W_w = 14.657$  and  $T = 100.2$ . (Time correction for  $T = -3.45$ .)

290. From the data given, find the specific heats of (A) cast silver, (B) cast zinc, (C) cast antimony, (D)

cast cadmium, (*E*) roll sulphur, as determined by Bunsen's method.  $W_w = 14.657$ .

|                               | A.     | B.      | C.      | D.      | E.     |
|-------------------------------|--------|---------|---------|---------|--------|
| Weight of substance . . . . . | 3.6320 | 2.5150  | 3.8575  | 1.8675  | 1.0708 |
| Temperature . . . . .         | 100°C. | 99.8°C. | 99.8°C. | 99.8°C. | 100 C. |
| Scale movement . . . . .      | 297.7  | 343.8   | 279.5   | 146.7   | 268.8  |

291. One kilogram of steam at  $100^{\circ}\text{C}$ . is condensed in forty-nine kilos of water at  $16^{\circ}\text{C}$ . ; what is the temperature of the mixture?

292. It is required to distil 2 kilos. of ethyl alcohol (BP.  $78.3^{\circ}$ ) per hour. What must be the supply of water at  $16^{\circ}\text{C}$ . in order that the temperature of the water round the worm may not average higher than  $25^{\circ}\text{C}$ . ? (Specific heat of ethyl alcohol = 0.615).

293. 75 grams of water are placed in a calorimeter of which the water equivalent is 5 grams ; when at  $15^{\circ}\text{C}$  , 5 grams of steam are passed into and condensed by the water with the result that the temperature of the calorimeter and its contents is raised to  $51.6^{\circ}\text{C}$ . ; from these data calculate the latent heat of vaporization of steam.

294. Using the atomic weights given in Appendix I., calculate the atomic heats of Pb, Ag, Cu, Fe, S, and P.

295. Taking the mean value of the atomic heats of the elements as 6.4, and the specific heats given in the table, find the atomic weights of Ag, Zn, Bi, Sn, and Fe. The stoichiometrical quantities of these elements found by analysis as equivalent to 35.37 parts of Cl are as follows :— Ag 107.66, Zn 32.44, Bi 69.16, Sn 29.339, and Fe 18.626 ; from these numbers deduce the exact atomic weights of the elements in question.

296. It is found that in many compounds the sum of the atomic heats of the atoms of which the molecule is built up equals the product of the molecular weight into the specific heat of the compound (the molecular heat) ; assuming this to be always the case, deduce the atomic heats in the solid state of Cl and O, from the data that the

sp. ht. of  $\text{PbCl}_2 = 0.0644$  (Regnault), of  $\text{Ga}_2\text{O}_3 = 0.1062$ , and of  $\text{In}_2\text{O}_3 = 0.0807$ .

(Specific heats,—Ga, 0.079 ; In, 0.057.)

297. Deduce the atomic heat of oxygen from the molecular heat 28.3 of potassium permanganate.

(Specific heats,—K, 0.166 ; Mn, 0.122.)

298. Find the approximate atomic heat of hydrogen if the molecular heat of  $\text{NH}_4\text{Cl}$  be taken as 20, and the atomic heats of N and Cl as 5.6 and 6.4 respectively.

299. The atomic heat of lead is deduced from Regnault's value for the specific heat to be about 6.3, the specific heat of cerussite = 0.080, of calc-spar = 0.206, of strontianite = 0.145, and of witherite = 0.109 ; find the atomic heats of Ca, Sr, and Ba.

## HEAT OF SOLUTION ; HEAT OF COMBINATION ; CALORIFIC POWER ; CALORIFIC INTENSITY.

CHEMICAL change is usually accompanied by changes in the distribution of energy in the system considered. By far the larger part of the energy lost to the changing systems during chemical reactions is given out in the form of heat ; reactions in which heat is evolved are said to be *exothermic*. There exists also a class of reactions requiring heat to be imparted from without the system to the reacting bodies to enable the change to occur ; such reactions are termed *endothermic*.

It is convenient to consider the thermal effects of the solution of substances together with the changes of energy-distribution due to strictly chemical reactions. The thermal unit in general use in connection with problems of this character is defined to be the amount of heat required to raise the temperature of one kilogram of water one degree Centigrade (the Calorie).

Generally the heat of combination is only one of a number of factors in the total thermal effect, heat being absorbed in the liquefaction or vaporization and evolved on the solidification of the reacting substances and products.

In the phenomena of ordinary combustion the terms *calorific power* and *calorific intensity* are used ; by the former we understand the amount of heat produced by the combustion of one unit of weight of the burning substance, whereas the latter indicates the temperature to which the products of combustion can be raised by the heat evolved.

The calorific intensity  $I = \frac{H}{m_1s_1 + m_2s_2 + m_3s_3 + \dots}$  where  $H$  represents the calorific power,  $s_1 s_2 s_3$  &c., the specific heats, and  $m_1 m_2 m_3$  &c., the masses of the products of the combustion of one unit weight of substance.

The following table expresses the calorific powers of a number of substances burnt in oxygen :—

|                |         |                 |         |
|----------------|---------|-----------------|---------|
| Hydrogen . . . | 34,462. | Tin. . . . .    | 1,144.  |
| Carbon . . .   | 8,080.  | Copper . . .    | 602.    |
| Sulphur . . .  | 2,220.  | Carbonic oxide. | 2,403.  |
| Phosphorus .   | 5,747.  | Marsh gas . .   | 13,063. |
| Zinc . . .     | 1,301.  | Olefiant gas. . | 11,858. |
| Iron . . .     | 1,576.  | Alcohol . . .   | 6,850.  |

The calorific power of any substance is a constant, being the same whether the body be burnt in oxygen or in air and whether it be burnt rapidly or slowly ; the calorific intensity is modified by the circumstances under which the combustion takes place, any mixture of inert material—*e.g.* nitrogen in air, ash in coal—lessening  $I$  since heat must be used to raise the temperature of the foreign matters. Again, if radiation be allowed to take place freely the temperature reached during slow combustion will not be nearly so high as that attained by a more rapid burning.

A special form of notation is used in thermo-chemistry—*e.g.*  $[H^2, Cl^2] = 44,000 +$  . in words means ‘two kilograms of hydrogen combine with seventy-one kilograms of chlorine with the evolution (+) of 44,000 Calories.’

#### EXAMPLES.

1. The calorific power of carbon is 8080, what is its calorific intensity when burnt in oxygen ?



12 parts of carbon give on combustion 44 parts of carbon dioxide, hence 1 kilo. produces 3.67 kilos. The specific heat of carbon dioxide is 0.2164.

$$\text{Hence } I = \frac{8080}{3.67 \times 0.2164} = 10,174^\circ \text{C.}$$

2. Find the calorific intensity of hydrogen burning in oxygen from the appended data.

Calorific power of hydrogen 34,462.

Weight of the product of combustion ( $\text{H}_2\text{O}$ ) yielded by 1 kilo. of hydrogen, 9 kilos.

Specific heat of steam 0.475.

Here it must be remembered that at the temperature of combustion the water produced remains in the gaseous state, whereas the calorific power given above includes the heat given out on the condensation of the water vapour produced to water; hence the latent heat of vaporization of the water must be deducted from the given calorific power in calculating the value for  $I$ .

Assuming that the initial temperature is  $0^\circ \text{C.}$  the total heat required to raise the temperature of the water produced to  $T^\circ = 9 \{100 + 537 + 0.475 (T - 100)\}$  and this is necessarily the same as the calorific power.

Hence  $I = T^\circ$ , and

$$9 \{100 + 537 - 47.5 + 0.475 T\} = 34,462.$$

$$589.5 + 0.475 T = \frac{34462}{9}$$

$$\text{therefore } I = T = \frac{\left(\frac{34462}{9} - 589.5\right)}{0.475} = 6820.2^\circ \text{C.}$$

3. Determine the heat of formation of  $\text{CH}_2\text{O}_2$  from its elements from the data :—

$$[\text{C}, \text{O}^2] = 96,960 + ; \quad [\text{H}^2, \text{O}] = 68,360 + ; \quad [\text{CH}^2\text{O}^2, \text{O}] = 65,900 +.$$

The total heat produced by the oxidation of free C. and  $\text{H}_2$  to  $\text{CO}_2$  and  $\text{H}_2\text{O}$  must evidently be equivalent to the heat of formation of  $\text{CH}_2\text{O}_2$  together with the heat pro-

duced by the oxidation of  $\text{CH}_2\text{O}_2$ , for we obtain the same final products in both cases.

$$[\text{C}, \text{O}^2] + [\text{H}^2, \text{O}] = [\text{C}, \text{H}^2, \text{O}^2] + [\text{CH}^2\text{O}^2, \text{O}]. \text{ and } [\text{C}, \text{O}^2] + [\text{H}^2, \text{O}] = 96,960 + 68,360 = 165,320 + .$$

$$\begin{aligned} \therefore [\text{C}, \text{H}^2, \text{O}^2] &= 165,320 - [\text{CH}^2\text{O}^2, \text{O}] \\ &= 165,320 - 65,900 \\ &= 99,420 + . \end{aligned}$$

4. Find the heat of solution of  $\text{HBr}$  from the data :—

$$(1) [\text{KOH Aq}, \text{HCl Aq}] = [\text{KOH Aq}, \text{HBr Aq}].$$

$$(2) [\text{K Br Aq}, \text{Cl}] = 11,500 + . \quad (3) [\text{Br}, \text{Aq}] = 500 + .$$

$$(4) [\text{H}, \text{Br}] = 8,400. \quad (5) [\text{H}, \text{Cl}, \text{Aq}] = 39,300.$$

$$\text{From (2). } [\text{KBr Aq}, \text{Cl}] = [\text{K}, \text{Cl}, \text{Aq}] + [\text{Br}, \text{Aq}] - [\text{K}, \text{Br}, \text{Aq}] = 11,500.$$

Replacement of  $\text{Br}$  by  $\text{Cl}$  gives 11500 thermal units.

From this (5) and (1) we have

$$[\text{H}, \text{Br}, \text{Aq}] = [\text{H}, \text{Cl}, \text{Aq}] = 11,000 = 28,300$$

$$\text{and } [\text{HBr}, \text{Aq}] = [\text{H}, \text{Br}, \text{Aq}] - [\text{H}, \text{Br}]$$

$$\text{that is } [\text{HBr}, \text{Aq}] = 28,300 - 8,400 = 19,900,$$

or the heat of solution of  $\text{HBr}$  is represented by 19,900 thermal units.

#### QUESTIONS.

300. What weight of water would be heated from  $0^\circ$  to  $1^\circ \text{C}$ . by the combustion of 1 gram of hydrogen?

301. One gram of phosphorus is burnt in oxygen. To what temperature would a kilogram of water at  $0^\circ \text{C}$ . be raised by the combustion?

302. Calculate the amount of water raised  $15^\circ$  by the combustion of 1 gram of sulphur in oxygen.

303. Calculate the calorific intensity of (1) ethylene, (2) of methane burning in air.

304. Calculate the calorific intensity of Newcastle Hartley coal possessing the following percentage composition :—

|                    |        |
|--------------------|--------|
| Carbon . . . . .   | 88.42  |
| Hydrogen . . . . . | 5.61   |
| Oxygen . . . . .   | 5.97   |
|                    | <hr/>  |
|                    | 100.00 |
|                    | <hr/>  |

305. Determine the amount of heat disengaged by the combination of 1 gram of carbon with oxygen from the following experiment by Andrews :—

|   |              |
|---|--------------|
| Weight of substance burnt . . . .   | 1.088 grams. |
| Temperature of the air . . . . .  | 10° 06 C.    |
| The excess of the final temperature<br>of the water above that of the air | { 0° 3    „  |
| Increment of temperature found . .  | 2° 473 „     |
| „     corrected .   | 2.464 „      |
| Weight of water in the calorimeter  | 318.3 grams. |
| Thermal value of the vessels . . .  | 180 „        |

! 306. Calculate the thermal power of charcoal from the following data :

|  |           |
|--|-----------|
| Weight of substance consumed . . .       | 10 parts. |
| „     the water . . . . .                | 8900 „    |
| „     the copper vessel . . .            | 1000 „    |
| Specific heat of copper . . . . .        | 0.09515   |
| Initial temperature . . . . .            | 11 C.     |
| Final                    „     . . . . . | 20° C.    |

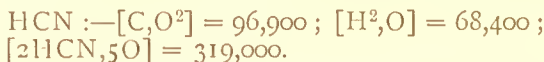
307. Calculate the height to which a ton weight would be raised by the combustion of a kilogram of this charcoal, supposing that all the heat evolved was utilised in the lifting.

308. Find the heat of formation of  $\text{H}_2\text{SO}_4$  from its elements.

Data given :— $[\text{H}^2\text{SO}^3\text{Aq}, \text{H}^2\text{O}, \text{Cl}^2] = 73,900$  ;  
 $[\text{H}, \text{Cl}, \text{Aq}] = 39,300$  ;  $[\text{H}^2, \text{O}] = 68,400$  ;  
 $[\text{SO}^2, \text{Aq}] = 7,700$  ;  $[\text{S}, \text{O}^2] = 69,900$  ;  $[\text{SO}^3, \text{Aq}] = 37,400$  ;  
 $[\text{H}^2\text{SO}^4, \text{Aq}] = 17,000$  ;

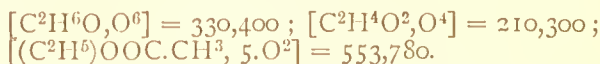
309. Given that  $[C, O^2] = 96,900$  and  $[H^2, O] = 68,400$ , find the heat of formation of  $CH_4$ , if the complete combustion of  $CH_4$  gives 213,500 heat units.

310. From the given data, find the heat of formation of



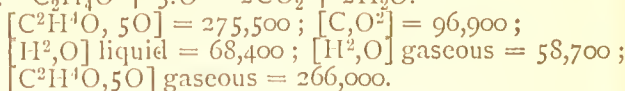
311. What is the thermal value of the reaction  $[N^2, O]$ ?  
Data :  $-[C, 2N^2O] = 133,900$ .  $[C, O^2] = 96,900$ .

312. Calculate the heat of combination of alcohol and acetic acid  $[C^2H^6O, C^2H^4O^2]$ , having given :—



313. Find the heat of formation of aldehyde from its elements, (a) liquid, (b) gaseous.

Data :  $-C_2H_4O + 5.O = 2CO_2 + 2H_2O$ .



314. The heat of solution of  $K_2SO_4$  is 6340 —, of  $CuSO_4, 5H_2O$  is 2430 —, of  $K_2SO_4.CuSO_4.7H_2O = 14,360$  —. What is the heat of formation of the double salt in solution?

315.  $[P^2, O^5] = 369,100$  + with ordinary phosphorus,  $[P^2, O^5] = 326,800$  + with amorphous phosphorus. What is the thermal value of the change from the yellow to the red variety?

316. In the reaction  $[H^3PO^3Aq, x NaOH Aq]$  the heat of neutralization for  $x = \frac{1}{2}$  is 7,400 ; for  $x = 1$  is 14,800 ; for  $x = 2$  is 28,500 ; for  $x = 3$  is 28,900. What deductions may be drawn as to the basicity of this acid?

Questions marked thus (l) are from the Owens College Calendars. Questions marked thus (t) are from the examination papers of the Science and Art Department.

# APPENDIX.

TABLE I.

*Atomic Weights and Symbols of the Elements.*

|                      |              |        |
|----------------------|--------------|--------|
| Aluminium . . . . .  | Al . . . . . | 27'1   |
| Antimony . . . . .   | Sb . . . . . | 120'2  |
| Argon . . . . .      | A . . . . .  | 39'9   |
| Arsenic . . . . .    | As . . . . . | 75'0   |
| Barium . . . . .     | Ba . . . . . | 137'4  |
| Bismuth . . . . .    | Bi . . . . . | 208'0  |
| Boron . . . . .      | B . . . . .  | 11'0   |
| Bromine . . . . .    | Br . . . . . | 79'96  |
| Cadmium . . . . .    | Cd . . . . . | 112'4  |
| Cæsium . . . . .     | Cs . . . . . | 132'9  |
| Calcium . . . . .    | Ca . . . . . | 40'1   |
| Carbon . . . . .     | C . . . . .  | 12'00  |
| Cerium . . . . .     | Ce . . . . . | 140'25 |
| Chlorine . . . . .   | Cl . . . . . | 35'45  |
| Chromium . . . . .   | Cr . . . . . | 52'1   |
| Cobalt . . . . .     | Co . . . . . | 59'0   |
| Columbium . . . . .  | Cb . . . . . | 94     |
| Copper . . . . .     | Cu . . . . . | 63'6   |
| Erbium . . . . .     | Er . . . . . | 166    |
| Europium . . . . .   | Eu . . . . . | 152    |
| Fluorine . . . . .   | F . . . . .  | 19'0   |
| Gadolinium . . . . . | Gd . . . . . | 156    |
| Gallium . . . . .    | Ga . . . . . | 70     |
| Germanium . . . . .  | Ge . . . . . | 72'5   |
| Glucinum . . . . .   | Gl . . . . . | 9'1    |
| Gold . . . . .       | Au . . . . . | 197'2  |
| Helium . . . . .     | He . . . . . | 4'0    |
| Hydrogen . . . . .   | H . . . . .  | 1'008  |
| Indium . . . . .     | In . . . . . | 115    |
| Iodine . . . . .     | I . . . . .  | 126'97 |
| Iridium . . . . .    | Ir . . . . . | 193'0  |
| Iron . . . . .       | Fe . . . . . | 55'9   |
| Krypton . . . . .    | Kr . . . . . | 81'8   |
| Lanthanum . . . . .  | La . . . . . | 138'9  |
| Lead . . . . .       | Pb . . . . . | 206'9  |
| Lithium . . . . .    | Li . . . . . | 7'03   |
| Magnesium . . . . .  | Mg . . . . . | 24'36  |
| Manganese . . . . .  | Mn . . . . . | 55'0   |

|                        |              |        |
|------------------------|--------------|--------|
| Mercury . . . . .      | Hg . . . . . | 200'0  |
| Molybdenum . . . . .   | Mo . . . . . | 96'0   |
| Neodymium . . . . .    | Nd . . . . . | 143'6  |
| Neon . . . . .         | Ne . . . . . | 20     |
| Nickel . . . . .       | Ni . . . . . | 58'7   |
| Nitrogen . . . . .     | N . . . . .  | 14'01  |
| Osmium . . . . .       | Os . . . . . | 191    |
| Oxygen . . . . .       | O . . . . .  | 16'00  |
| Palladium . . . . .    | Pd . . . . . | 106'5  |
| Phosphorus . . . . .   | P . . . . .  | 31'0   |
| Platinum . . . . .     | Pt . . . . . | 194'8  |
| Potassium . . . . .    | K . . . . .  | 39'15  |
| Praseodymium . . . . . | Pr . . . . . | 140'5  |
| Radium . . . . .       | Rd . . . . . | 225    |
| Rhodium . . . . .      | Rh . . . . . | 103'0  |
| Rubidium . . . . .     | Rb . . . . . | 85'5   |
| Ruthenium . . . . .    | Ru . . . . . | 101'7  |
| Samarium . . . . .     | Sa . . . . . | 150'3  |
| Scandium . . . . .     | Sc . . . . . | 44'1   |
| Selenium . . . . .     | Se . . . . . | 79'2   |
| Silicon . . . . .      | Si . . . . . | 28'4   |
| Silver . . . . .       | Ag . . . . . | 107'93 |
| Sodium . . . . .       | Na . . . . . | 23'05  |
| Strontium . . . . .    | Sr . . . . . | 87'6   |
| Sulphur . . . . .      | S . . . . .  | 32'06  |
| Tantalum . . . . .     | Ta . . . . . | 181    |
| Tellurium . . . . .    | Te . . . . . | 127'6  |
| Terbium . . . . .      | Tb . . . . . | 159'2  |
| Thallium . . . . .     | Tl . . . . . | 204'1  |
| Thorium . . . . .      | Th . . . . . | 232'5  |
| Thulium . . . . .      | Tm . . . . . | 171    |
| Tin . . . . .          | Sn . . . . . | 119'0  |
| Titanium . . . . .     | Ti . . . . . | 48'1   |
| Tungsten . . . . .     | W . . . . .  | 184    |
| Uranium . . . . .      | U . . . . .  | 238'5  |
| Vanadium . . . . .     | V . . . . .  | 51'2   |
| Xenon . . . . .        | Xe . . . . . | 128    |
| Ytterbium . . . . .    | Yb . . . . . | 173'0  |
| Yttrium . . . . .      | Yt . . . . . | 89'0   |
| Zinc . . . . .         | Zn . . . . . | 65'4   |
| Zirconium . . . . .    | Zr . . . . . | 90'6   |

TABLE II.

*Weight of one Cubic Centimetre of Atmospheric Air at different Temperatures from 0° to 300°, at 760 mm. pressure.*

| °  |          | °  |          | °   |          | °   |          |
|----|----------|----|----------|-----|----------|-----|----------|
| 0  | 0'001293 | 46 | 0'001108 | 92  | 0'000967 | 138 | 0'000858 |
| 1  | 001288   | 47 | 001105   | 93  | 000964   | 139 | 000856   |
| 2  | 001284   | 48 | 001102   | 94  | 000962   | 140 | 000854   |
| 3  | 001279   | 49 | 001098   | 95  | 000959   | 141 | 000852   |
| 4  | 001275   | 50 | 001095   | 96  | 000956   | 142 | 000850   |
| 5  | 001270   | 51 | 001091   | 97  | 000953   | 143 | 000848   |
| 6  | 001266   | 52 | 001088   | 98  | 000951   | 144 | 000846   |
| 7  | 001261   | 53 | 001084   | 99  | 000948   | 145 | 000844   |
| 8  | 001257   | 54 | 001081   | 100 | 000946   | 146 | 000842   |
| 9  | 001252   | 55 | 001077   | 101 | 000943   | 147 | 000840   |
| 10 | 001248   | 56 | 001074   | 102 | 000941   | 148 | 000838   |
| 11 | 001243   | 57 | 001070   | 103 | 000938   | 149 | 000836   |
| 12 | 001239   | 58 | 001067   | 104 | 000936   | 150 | 000834   |
| 13 | 001234   | 59 | 001063   | 105 | 000933   | 151 | 000832   |
| 14 | 001230   | 60 | 001060   | 106 | 000931   | 152 | 000830   |
| 15 | 001225   | 61 | 001057   | 107 | 000928   | 153 | 000828   |
| 16 | 001221   | 62 | 001053   | 108 | 000926   | 154 | 000826   |
| 17 | 001217   | 63 | 001050   | 109 | 000923   | 155 | 000824   |
| 18 | 001213   | 64 | 001047   | 110 | 000921   | 156 | 000822   |
| 19 | 001209   | 65 | 001044   | 111 | 000919   | 157 | 000821   |
| 20 | 001205   | 66 | 001041   | 112 | 000916   | 158 | 000819   |
| 21 | 001201   | 67 | 001038   | 113 | 000914   | 159 | 000817   |
| 22 | 001197   | 68 | 001035   | 114 | 000911   | 160 | 000815   |
| 23 | 001193   | 69 | 001032   | 115 | 000909   | 161 | 000813   |
| 24 | 001189   | 70 | 001029   | 116 | 000907   | 162 | 000811   |
| 25 | 001185   | 71 | 001026   | 117 | 000905   | 163 | 000809   |
| 26 | 001181   | 72 | 001023   | 118 | 000903   | 164 | 000807   |
| 27 | 001177   | 73 | 001020   | 119 | 000900   | 165 | 000806   |
| 28 | 001173   | 74 | 001017   | 120 | 000898   | 166 | 000804   |
| 29 | 001169   | 75 | 001014   | 121 | 000896   | 167 | 000802   |
| 30 | 001165   | 76 | 001011   | 122 | 000894   | 168 | 000800   |
| 31 | 001161   | 77 | 001008   | 123 | 000891   | 169 | 000798   |
| 32 | 001157   | 78 | 001005   | 124 | 000889   | 170 | 000796   |
| 33 | 001154   | 79 | 001002   | 125 | 000887   | 171 | 000794   |
| 34 | 001150   | 80 | 001000   | 126 | 000884   | 172 | 000793   |
| 35 | 001146   | 81 | 000997   | 127 | 000882   | 173 | 000791   |
| 36 | 001142   | 82 | 000994   | 128 | 000880   | 174 | 000789   |
| 37 | 001138   | 83 | 000992   | 129 | 000878   | 175 | 000788   |
| 38 | 001134   | 84 | 000989   | 130 | 000876   | 176 | 000786   |
| 39 | 001131   | 85 | 000986   | 131 | 000874   | 177 | 000784   |
| 40 | 001128   | 86 | 000983   | 132 | 000871   | 178 | 000782   |
| 41 | 001124   | 87 | 000980   | 133 | 000869   | 179 | 000781   |
| 42 | 001121   | 88 | 000977   | 134 | 000867   | 180 | 000779   |
| 43 | 001118   | 89 | 000974   | 135 | 000865   | 181 | 000777   |
| 44 | 001114   | 90 | 000972   | 136 | 000863   | 182 | 000776   |
| 45 | 001111   | 91 | 000969   | 137 | 000860   | 183 | 000774   |

TABLE II.—(continued.)

|     |          |     |          |     |          |     |          |
|-----|----------|-----|----------|-----|----------|-----|----------|
| 184 | 0'000772 | 213 | 0'000725 | 242 | 0'000685 | 271 | 0'000648 |
| 185 | 000770   | 214 | 000724   | 243 | 000683   | 272 | 000647   |
| 186 | 000769   | 215 | 000722   | 244 | 000682   | 273 | 000646   |
| 187 | 000767   | 216 | 000721   | 245 | 000681   | 274 | 000645   |
| 188 | 000765   | 217 | 000719   | 246 | 000679   | 275 | 000643   |
| 189 | 000763   | 218 | 000718   | 247 | 000678   | 276 | 000642   |
| 190 | 000762   | 219 | 000716   | 248 | 000677   | 277 | 000641   |
| 191 | 000760   | 220 | 000715   | 249 | 000675   | 278 | 000640   |
| 192 | 000758   | 221 | 000713   | 250 | 000674   | 279 | 000639   |
| 193 | 000757   | 222 | 000712   | 251 | 000673   | 280 | 000638   |
| 194 | 000755   | 223 | 000710   | 252 | 000672   | 281 | 000636   |
| 195 | 000754   | 224 | 000709   | 253 | 000670   | 282 | 000635   |
| 196 | 000752   | 225 | 000708   | 254 | 000669   | 283 | 000634   |
| 197 | 000751   | 226 | 000706   | 255 | 000668   | 284 | 000633   |
| 198 | 000749   | 227 | 000705   | 256 | 000666   | 285 | 000631   |
| 199 | 000748   | 228 | 000703   | 257 | 000665   | 286 | 000630   |
| 200 | 000746   | 229 | 000702   | 258 | 000664   | 287 | 000629   |
| 201 | 000744   | 230 | 000701   | 259 | 000663   | 288 | 000628   |
| 202 | 000743   | 231 | 000699   | 260 | 000662   | 289 | 000627   |
| 203 | 000740   | 232 | 000698   | 261 | 000660   | 290 | 000626   |
| 204 | 000739   | 233 | 000697   | 262 | 000659   | 291 | 000625   |
| 205 | 000737   | 234 | 000695   | 263 | 000658   | 292 | 000624   |
| 206 | 000736   | 235 | 000694   | 264 | 000657   | 293 | 000623   |
| 207 | 000734   | 236 | 000692   | 265 | 000655   | 294 | 000622   |
| 208 | 000733   | 237 | 000691   | 266 | 000654   | 295 | 000621   |
| 209 | 000731   | 238 | 000690   | 267 | 000653   | 296 | 000620   |
| 210 | 000730   | 239 | 000689   | 268 | 000652   | 297 | 000619   |
| 211 | 000728   | 240 | 000688   | 269 | 000651   | 298 | 000618   |
| 212 | 000727   | 241 | 000686   | 270 | 000650   | 299 | 000617   |
|     |          |     |          |     |          | 300 | 000616   |

TABLE III.

*The weight of 1000 c.c. of water of  $t^{\circ}$  C., when determined by means of brass weights in air of  $0^{\circ}$  C., and of a tension 0'76m., is equal to  $1000 - x$  grms.*

| $t^{\circ}$ | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   | 11   | 12   |
|-------------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| $x$         | 1'26 | 1'20 | 1'16 | 1'13 | 1'12 | 1'12 | 1'14 | 1'17 | 1'22 | 1'28 | 1'35 | 1'44 | 1'54 |
| $t^{\circ}$ | 13   | 14   | 15   | 16   | 17   | 18   | 19   | 20   | 21   | 22   | 23   | 24   | 25   |
| $x$         | 1'65 | 1'78 | 1'92 | 2'07 | 2'23 | 2'40 | 2'58 | 2'78 | 2'99 | 3'20 | 3'43 | 3'66 | 3'90 |
| $t^{\circ}$ | 26   | 27   | 28   | 29   | 30   |      |      |      |      |      |      |      |      |
| $x$         | 4'17 | 4'45 | 4'72 | 4'99 | 5'26 |      |      |      |      |      |      |      |      |



TABLE IV.

*Volume and Density of Water at different Temperatures,*  
(ROSSETTI).

| Temp.<br>°C. | Volume of<br>Water<br>(at 0° = 1). | Sp. Gr. of<br>Water<br>(at 0° = 1). | Volume of<br>Water<br>(at 4° = 1). | Sp. Gr. of<br>Water<br>(at 4° = 1). |
|--------------|------------------------------------|-------------------------------------|------------------------------------|-------------------------------------|
| 0            | 1'00000                            | 1'000000                            | 1'00013                            | 0'999871                            |
| 1            | 0'99994                            | 1'000057                            | 1'00007                            | 0'999928                            |
| 2            | 0'99990                            | 1'000098                            | 1'00003                            | 0'999969                            |
| 3            | 0'99988                            | 1'000120                            | 1'00001                            | 0'999991                            |
| 4            | 0'99987                            | 1'000129                            | 1'00000                            | 1'000000                            |
| 5            | 0'99988                            | 1'000119                            | 1'00001                            | 0'999990                            |
| 6            | 0'99990                            | 1'000099                            | 1'00003                            | 0'999970                            |
| 7            | 0'99994                            | 1'000062                            | 1'00007                            | 0'999933                            |
| 8            | 0'99999                            | 1'000015                            | 1'00011                            | 0'999886                            |
| 9            | 1'00005                            | 0'999953                            | 1'00018                            | 0'999824                            |
| 10           | 1'00012                            | 0'999876                            | 1'00025                            | 0'999747                            |
| 11           | 1'00022                            | 0'999784                            | 1'00034                            | 0'999655                            |
| 12           | 1'00032                            | 0'999678                            | 1'00045                            | 0'999549                            |
| 13           | 1'00044                            | 0'999559                            | 1'00057                            | 0'999430                            |
| 14           | 1'00057                            | 0'999429                            | 1'00070                            | 0'999299                            |
| 15           | 1'00071                            | 0'999289                            | 1'00084                            | 0'999160                            |
| 16           | 1'00087                            | 0'999131                            | 1'00100                            | 0'999002                            |
| 17           | 1'00103                            | 0'998970                            | 1'00116                            | 0'998841                            |
| 18           | 1'00122                            | 0'998782                            | 1'00135                            | 0'998654                            |
| 19           | 1'00141                            | 0'998588                            | 1'00154                            | 0'998460                            |
| 20           | 1'00161                            | 0'998388                            | 1'00174                            | 0'998259                            |
| 21           | 1'00183                            | 0'998176                            | 1'00196                            | 0'998047                            |
| 22           | 1'00205                            | 0'997956                            | 1'00217                            | 0'997828                            |
| 23           | 1'00228                            | 0'997730                            | 1'00240                            | 0'997601                            |
| 24           | 1'00251                            | 0'997495                            | 1'00264                            | 0'997367                            |
| 25           | 1'00276                            | 0'997249                            | 1'00289                            | 0'997120                            |
| 26           | 1'00301                            | 0'996994                            | 1'00314                            | 0'996866                            |
| 27           | 1'00328                            | 0'996732                            | 1'00341                            | 0'996603                            |
| 28           | 1'00355                            | 0'996460                            | 1'00368                            | 0'996331                            |
| 29           | 1'00383                            | 0'996179                            | 1'00396                            | 0'996051                            |
| 30           | 1'00412                            | 0'99589                             | 1'00425                            | 0'99577                             |
| 40           | 1'00757                            | ...                                 | ...                                | ...                                 |
| 50           | 1'01182                            | ...                                 | ...                                | ...                                 |
| 60           | 1'01678                            | ...                                 | ...                                | ...                                 |
| 70           | 1'02243                            | ...                                 | ...                                | ...                                 |
| 80           | 1'02874                            | ...                                 | ...                                | ...                                 |
| 90           | 1'03554                            | ...                                 | ...                                | ...                                 |
| 100          | 1'04299                            | ...                                 | ...                                | ...                                 |

TABLE V.

For the Calculation of  $\frac{1}{1 + 0.00367T}$ .

| T  |         | T  |         | T   |         | T   |         |
|----|---------|----|---------|-----|---------|-----|---------|
| 1  | 0.99634 | 38 | 0.87761 | 75  | 0.78416 | 112 | 0.70870 |
| 2  | 99271   | 39 | 87479   | 76  | 78191   | 113 | 70686   |
| 3  | 98911   | 40 | 87199   | 77  | 77967   | 114 | 70503   |
| 4  | 98553   | 41 | 86921   | 78  | 77745   | 115 | 70321   |
| 5  | 98198   | 42 | 86645   | 79  | 77523   | 116 | 70140   |
| 6  | 97845   | 43 | 86370   | 80  | 77304   | 117 | 69960   |
| 7  | 97495   | 44 | 86097   | 81  | 77085   | 118 | 69781   |
| 8  | 97148   | 45 | 85826   | 82  | 76867   | 119 | 69603   |
| 9  | 96803   | 46 | 85556   | 83  | 76651   | 120 | 69425   |
| 10 | 96460   | 47 | 85289   | 84  | 76436   | 121 | 69249   |
| 11 | 96120   | 48 | 85022   | 85  | 76222   | 122 | 69073   |
| 12 | 95782   | 49 | 84758   | 86  | 76010   | 123 | 68899   |
| 13 | 95446   | 50 | 84495   | 87  | 75798   | 124 | 68725   |
| 14 | 95113   | 51 | 84234   | 88  | 75588   | 125 | 68552   |
| 15 | 94782   | 52 | 83974   | 89  | 75379   | 126 | 68380   |
| 16 | 94454   | 53 | 83716   | 90  | 75171   | 127 | 68209   |
| 17 | 94127   | 54 | 83460   | 91  | 74964   | 128 | 68038   |
| 18 | 93803   | 55 | 83205   | 92  | 74758   | 129 | 67869   |
| 19 | 93482   | 56 | 82952   | 93  | 74554   | 130 | 67700   |
| 20 | 93162   | 57 | 82700   | 94  | 74354   | 131 | 67532   |
| 21 | 92844   | 58 | 82450   | 95  | 74148   | 132 | 67365   |
| 22 | 92529   | 59 | 82201   | 96  | 73947   | 133 | 67199   |
| 23 | 92216   | 60 | 81954   | 97  | 73747   | 134 | 67034   |
| 24 | 91905   | 61 | 81708   | 98  | 73548   | 135 | 66870   |
| 25 | 91596   | 62 | 81464   | 99  | 73350   | 136 | 66706   |
| 26 | 91289   | 63 | 81221   | 100 | 73153   | 137 | 66543   |
| 27 | 90984   | 64 | 80979   | 101 | 72957   | 138 | 66380   |
| 28 | 90682   | 65 | 80740   | 102 | 72762   | 139 | 66219   |
| 29 | 90381   | 66 | 80501   | 103 | 72568   | 140 | 66059   |
| 30 | 90082   | 67 | 80264   | 104 | 72376   | 141 | 65899   |
| 31 | 89785   | 68 | 80028   | 105 | 72184   | 142 | 65740   |
| 32 | 89490   | 69 | 79794   | 106 | 71993   | 143 | 65582   |
| 33 | 89197   | 70 | 79561   | 107 | 71803   | 144 | 65424   |
| 34 | 88906   | 71 | 79329   | 108 | 71615   | 145 | 65268   |
| 35 | 88617   | 72 | 79099   | 109 | 71427   | 146 | 65112   |
| 36 | 88330   | 73 | 78870   | 110 | 71240   | 147 | 64957   |
| 37 | 88044   | 74 | 78642   | 111 | 71055   | 148 | 64802   |

TABLE VI.

*Pressure (tension) of Water Vapour between  $-19^{\circ}$  and  $101^{\circ}$  C.,  
(BROCH).*

| T.°C. | mm.    | T.°C. | mm.     | T.°C. | mm.      | T.°C. | mm.      |
|-------|--------|-------|---------|-------|----------|-------|----------|
| -19   | 1'0288 | 12    | 10'4322 | 43    | 64'3104  | 74    | 276'8675 |
| -18   | 1'1202 | 13    | 11'1370 | 44    | 67'7568  | 75    | 288'7640 |
| -17   | 1'2187 | 14    | 11'8835 | 45    | 71'3619  | 76    | 301'0860 |
| -16   | 1'3248 | 15    | 12'6739 | 46    | 75'1314  | 77    | 313'8475 |
| -15   | 1'4390 | 16    | 13'5103 | 47    | 79'0714  | 78    | 327'0549 |
| -14   | 1'5618 | 17    | 14'3950 | 48    | 83'1883  | 79    | 340'7265 |
| -13   | 1'6939 | 18    | 15'3304 | 49    | 87'4882  | 80    | 354'8730 |
| -12   | 1'8357 | 19    | 16'3189 | 50    | 91'9780  | 81    | 369'5075 |
| -11   | 1'9880 | 20    | 17'3632 | 51    | 96'6644  | 82    | 384'6432 |
| -10   | 2'1514 | 21    | 18'4659 | 52    | 101'5541 | 83    | 400'2933 |
| -9    | 2'3266 | 22    | 19'6297 | 53    | 106'6546 | 84    | 416'4721 |
| -8    | 2'5143 | 23    | 20'8576 | 54    | 111'9730 | 85    | 433'1938 |
| -7    | 2'7153 | 24    | 22'1524 | 55    | 117'5162 | 86    | 450'4730 |
| -6    | 2'9304 | 25    | 23'5174 | 56    | 123'2925 | 87    | 468'3240 |
| -5    | 3'1605 | 26    | 24'9556 | 57    | 129'3095 | 88    | 486'7635 |
| -4    | 3'4065 | 27    | 26'4705 | 58    | 135'5750 | 89    | 505'8059 |
| -3    | 3'6693 | 28    | 28'0654 | 59    | 142'0973 | 90    | 525'4676 |
| -2    | 3'9499 | 29    | 29'7439 | 60    | 148'8848 | 91    | 545'7650 |
| -1    | 4'2493 | 30    | 31'5096 | 61    | 155'9456 | 92    | 566'7149 |
| 0     | 4'5687 | 31    | 33'3664 | 62    | 163'2889 | 93    | 588'3349 |
| +1    | 4'9091 | 32    | 35'3181 | 63    | 170'9236 | 94    | 610'6426 |
| 2     | 5'2719 | 33    | 37'3689 | 64    | 178'8585 | 95    | 633'6567 |
| 3     | 5'6582 | 34    | 39'5228 | 65    | 187'1028 | 96    | 657'3956 |
| 4     | 6'0693 | 35    | 41'7842 | 66    | 195'6663 | 97    | 681'8791 |
| 5     | 6'5067 | 36    | 44'1577 | 67    | 204'5586 | 98    | 707'1271 |
| 6     | 6'9718 | 37    | 46'6477 | 68    | 213'7895 | 99    | 733'1602 |
| 7     | 7'4660 | 38    | 49'2950 | 69    | 223'3691 | 100   | 760'0000 |
| 8     | 7'9909 | 39    | 51'9965 | 70    | 233'3079 | 101   | 787'6678 |
| 9     | 8'5484 | 40    | 54'8651 | 71    | 243'6163 |       |          |
| 10    | 9'1398 | 41    | 57'8700 | 72    | 254'3048 |       |          |
| 11    | 9'7671 | 42    | 61'0167 | 73    | 265'3849 |       |          |

TABLE VII.

*For the Conversion of the Degrees (T') of a Mercurial Thermometer into the corresponding values (T'') of a Hydrogen Thermometer.*

| T'      | T''     | T'      | T'' | T'      | T'' | T'      | T'' |
|---------|---------|---------|-----|---------|-----|---------|-----|
| -10°·07 | -10°·00 | 100°    | 100 | 189°·65 | 190 | 280°·52 | 280 |
| 0°·00   | 0°·00   | 109°·98 | 110 | 199°·70 | 200 | 290°·81 | 290 |
| +10°·05 | +10°·00 | 119°·95 | 120 | 209°·75 | 210 | 301°·08 | 300 |
| 20°·08  | 20°·00  | 129°·91 | 130 | 219°·80 | 220 | 311°·45 | 310 |
| 30°·10  | 30°·00  | 139°·85 | 140 | 229°·85 | 230 | 321°·80 | 320 |
| 40°·11  | 40°·00  | 149°·80 | 150 | 239°·90 | 240 | 332°·40 | 330 |
| 50°·10  | 50°·00  | 159°·74 | 160 | 250°·05 | 250 | 343°·00 | 340 |
| 60°·09  | 60°·00  | 169°·68 | 170 | 260°·20 | 260 | 354°·00 | 350 |
| 70°·07  | 70°·00  | 179°·63 | 180 | 270°·38 | 270 |         |     |
| 80°·05  | 80°·00  |         |     |         |     |         |     |
| 90°·03  | 90°·00  |         |     |         |     |         |     |

TABLE VIII.

*For the Correction of Thermometer Readings.*

| $t - t'$ | $n$  |      |      |      |      |      |      |      |      |      |
|----------|------|------|------|------|------|------|------|------|------|------|
|          | 10   | 20   | 30   | 40   | 50   | 60   | 70   | 80   | 90   | 100  |
| 10       | 0'01 | 0'03 | 0'04 | 0'06 | 0'07 | 0'09 | 0'10 | 0'11 | 0'13 | 0'14 |
| 20       | 0'02 | 0'06 | 0'09 | 0'11 | 0'14 | 0'17 | 0'20 | 0'22 | 0'26 | 0'29 |
| 30       | 0'04 | 0'09 | 0'13 | 0'17 | 0'21 | 0'26 | 0'30 | 0'34 | 0'39 | 0'43 |
| 40       | 0'05 | 0'11 | 0'17 | 0'23 | 0'28 | 0'34 | 0'40 | 0'47 | 0'52 | 0'57 |
| 50       | 0'07 | 0'14 | 0'21 | 0'29 | 0'36 | 0'43 | 0'50 | 0'60 | 0'64 | 0'71 |
| 60       | 0'08 | 0'17 | 0'25 | 0'35 | 0'43 | 0'51 | 0'60 | 0'70 | 0'77 | 0'86 |
| 70       | 0'10 | 0'20 | 0'30 | 0'40 | 0'50 | 0'60 | 0'70 | 0'80 | 0'90 | 1'00 |
| 80       | 0'11 | 0'23 | 0'34 | 0'45 | 0'57 | 0'68 | 0'80 | 0'91 | 1'03 | 1'14 |
| 90       | 0'13 | 0'26 | 0'39 | 0'51 | 0'64 | 0'77 | 0'90 | 1'03 | 1'16 | 1'30 |
| 100      | 0'14 | 0'28 | 0'43 | 0'57 | 0'71 | 0'85 | 1'00 | 1'14 | 1'29 | 1'43 |
| 110      | 0'16 | 0'31 | 0'47 | 0'63 | 0'79 | 0'94 | 1'10 | 1'26 | 1'42 | 1'58 |
| 120      | 0'17 | 0'34 | 0'51 | 0'69 | 0'86 | 1'03 | 1'20 | 1'37 | 1'54 | 1'71 |

| $t - t'$ | $n$  |      |      |      |      |      |      |      |      |      |
|----------|------|------|------|------|------|------|------|------|------|------|
|          | 110  | 120  | 130  | 140  | 150  | 160  | 170  | 180  | 190  | 200  |
| 10       | 0'16 | 0'17 | 0'19 | 0'20 | 0'21 | 0'22 | 0'24 | 0'26 | 0'27 | 0'29 |
| 20       | 0'31 | 0'34 | 0'37 | 0'40 | 0'43 | 0'46 | 0'49 | 0'51 | 0'54 | 0'57 |
| 30       | 0'47 | 0'51 | 0'56 | 0'60 | 0'64 | 0'68 | 0'73 | 0'77 | 0'82 | 0'86 |
| 40       | 0'63 | 0'69 | 0'74 | 0'80 | 0'86 | 0'91 | 0'97 | 1'03 | 1'09 | 1'14 |
| 50       | 0'79 | 0'86 | 0'93 | 1'00 | 1'07 | 1'14 | 1'22 | 1'29 | 1'36 | 1'43 |
| 60       | 0'94 | 1'03 | 1'12 | 1'20 | 1'29 | 1'37 | 1'46 | 1'54 | 1'63 | 1'72 |
| 70       | 1'10 | 1'20 | 1'30 | 1'40 | 1'50 | 1'60 | 1'70 | 1'80 | 1'90 | 2'00 |
| 80       | 1'26 | 1'37 | 1'49 | 1'60 | 1'72 | 1'83 | 1'94 | 2'05 | 2'17 | 2'29 |
| 90       | 1'42 | 1'54 | 1'66 | 1'80 | 1'93 | 2'05 | 2'17 | 2'31 | 2'45 | 2'54 |
| 100      | 1'58 | 1'71 | 1'84 | 2'00 | 2'15 | 2'29 | 2'43 | 2'57 | 2'72 | 2'86 |
| 110      | 1'73 | 1'89 | 2'04 | 2'20 | 2'36 | 2'51 | 2'67 | 2'83 | 2'99 | 3'15 |
| 120      | 1'89 | 2'06 | 2'23 | 2'40 | 2'57 | 2'74 | 2'92 | 3'09 | 3'26 | 3'43 |

TABLE IX.

*Useful Constants.*

|  | Number.       | Logarithm. |
|--|---------------|------------|
| $\pi$ . . . . .  | 3'1416        | 0'4971499  |
| $g$ , at Greenwich. . . . .  | 981'17 cms.   | 2'9917443  |
| Coefficient of expansion of Hg. for 1° C. . . . .  | 0'0001802     | 4'2557548  |
| Mass of 1 c.c. of Hg. at 0° C. . . . .   | 13'596 grams. | 1'1334112  |
| Volume of 31'92 gm. of oxygen in litres. . . . .   | 22'325        | 1'3487915  |
| Conventional molecular vol. in litres. . . . .   | 22'4          | 1'3502480  |
| Coeff. exp. air, at constant pressure . . . . .  | 0'00367       | 3'5646661  |
| Coeff. elasticity of air at constant volume . . . . .  | 0'003665      | 3'5640740  |
| One litre of hydrogen at 0°C and 760 mm.<br>barometric pressure and at the level of<br>the sea and latitude 45° weighs . . . . . | 0'08958 grms. | 2'9522111  |
| Do. oxygen. . . . .  | 1'4298 "      | 0 1552753  |
| Do. nitrogen . . . . .   | 1'2562 "      | 0'0990588  |
| Do. air . . . . .  | 1'2932 "      | 0'1116657  |

| Nat.<br>numb. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|---------------|------|------|------|------|------|------|------|------|------|------|---|---|----|----|----|----|----|----|----|
| 10            | 0000 | 0043 | 0086 | 0128 | 0170 | 0212 | 0253 | 0294 | 0334 | 0374 | 4 | 8 | 12 | 17 | 21 | 25 | 29 | 33 | 37 |
| 11            | 0414 | 0453 | 0492 | 0531 | 0569 | 0607 | 0645 | 0682 | 0719 | 0755 | 4 | 8 | 11 | 15 | 19 | 23 | 26 | 30 | 34 |
| 12            | 0792 | 0828 | 0864 | 0899 | 0934 | 0969 | 1004 | 1038 | 1072 | 1106 | 3 | 7 | 10 | 14 | 17 | 21 | 24 | 28 | 31 |
| 13            | 1139 | 1173 | 1206 | 1239 | 1271 | 1303 | 1335 | 1367 | 1399 | 1430 | 3 | 6 | 10 | 13 | 16 | 19 | 23 | 26 | 29 |
| 14            | 1461 | 1492 | 1523 | 1553 | 1584 | 1614 | 1644 | 1673 | 1703 | 1732 | 3 | 6 | 9  | 12 | 15 | 18 | 21 | 24 | 27 |
| 15            | 1761 | 1790 | 1818 | 1847 | 1875 | 1903 | 1931 | 1959 | 1987 | 2014 | 3 | 6 | 8  | 11 | 14 | 17 | 20 | 22 | 25 |
| 16            | 2041 | 2068 | 2095 | 2122 | 2148 | 2175 | 2201 | 2227 | 2253 | 2279 | 3 | 5 | 8  | 10 | 13 | 16 | 18 | 21 | 24 |
| 17            | 2304 | 2330 | 2355 | 2380 | 2405 | 2430 | 2455 | 2480 | 2504 | 2529 | 2 | 5 | 7  | 9  | 12 | 15 | 17 | 20 | 22 |
| 18            | 2553 | 2577 | 2601 | 2625 | 2648 | 2672 | 2695 | 2718 | 2742 | 2765 | 2 | 5 | 7  | 9  | 12 | 14 | 16 | 19 | 21 |
| 19            | 2788 | 2810 | 2833 | 2856 | 2878 | 2900 | 2923 | 2945 | 2967 | 2989 | 2 | 4 | 7  | 9  | 11 | 13 | 16 | 18 | 20 |
| 20            | 3010 | 3032 | 3054 | 3075 | 3096 | 3118 | 3139 | 3160 | 3181 | 3201 | 2 | 4 | 6  | 8  | 11 | 13 | 15 | 17 | 19 |
| 21            | 3222 | 3243 | 3263 | 3284 | 3304 | 3324 | 3345 | 3365 | 3385 | 3404 | 2 | 4 | 6  | 8  | 10 | 12 | 14 | 16 | 18 |
| 22            | 3417 | 3444 | 3464 | 3483 | 3502 | 3522 | 3541 | 3560 | 3579 | 3598 | 2 | 4 | 6  | 7  | 9  | 11 | 13 | 15 | 17 |
| 23            | 3617 | 3636 | 3655 | 3674 | 3692 | 3711 | 3729 | 3747 | 3766 | 3784 | 2 | 4 | 5  | 7  | 9  | 11 | 12 | 14 | 16 |
| 24            | 3802 | 3820 | 3838 | 3856 | 3874 | 3892 | 3909 | 3927 | 3945 | 3962 | 2 | 3 | 5  | 7  | 9  | 10 | 12 | 14 | 15 |
| 25            | 3979 | 3997 | 4014 | 4031 | 4048 | 4065 | 4082 | 4099 | 4116 | 4133 | 2 | 3 | 5  | 7  | 8  | 10 | 11 | 13 | 15 |
| 26            | 4150 | 4166 | 4183 | 4200 | 4216 | 4232 | 4249 | 4265 | 4281 | 4298 | 2 | 3 | 5  | 6  | 8  | 9  | 11 | 13 | 14 |
| 27            | 4314 | 4330 | 4346 | 4362 | 4378 | 4393 | 4409 | 4425 | 4440 | 4456 | 2 | 3 | 5  | 6  | 8  | 9  | 11 | 12 | 14 |
| 28            | 4472 | 4487 | 4502 | 4518 | 4533 | 4548 | 4564 | 4579 | 4594 | 4609 | 2 | 3 | 5  | 6  | 8  | 9  | 11 | 12 | 14 |
| 29            | 4624 | 4639 | 4654 | 4669 | 4683 | 4698 | 4713 | 4728 | 4742 | 4757 | 1 | 3 | 4  | 6  | 7  | 9  | 10 | 12 | 13 |
| 30            | 4771 | 4786 | 4800 | 4814 | 4829 | 4843 | 4857 | 4871 | 4886 | 4900 | 1 | 3 | 4  | 6  | 7  | 9  | 10 | 11 | 13 |
| 31            | 4914 | 4928 | 4942 | 4955 | 4969 | 4983 | 4997 | 5011 | 5024 | 5038 | 1 | 3 | 4  | 6  | 7  | 8  | 9  | 11 | 12 |
| 32            | 5031 | 5045 | 5059 | 5072 | 5085 | 5109 | 5132 | 5145 | 5159 | 5172 | 1 | 3 | 4  | 5  | 7  | 8  | 9  | 10 | 12 |
| 33            | 5185 | 5198 | 5211 | 5224 | 5237 | 5250 | 5263 | 5276 | 5289 | 5302 | 1 | 3 | 4  | 5  | 6  | 8  | 9  | 10 | 12 |
| 34            | 5315 | 5328 | 5340 | 5353 | 5366 | 5378 | 5391 | 5403 | 5416 | 5428 | 1 | 3 | 4  | 5  | 6  | 7  | 9  | 10 | 11 |
| 35            | 5441 | 5453 | 5465 | 5478 | 5490 | 5502 | 5514 | 5527 | 5539 | 5551 | 1 | 2 | 4  | 5  | 6  | 7  | 8  | 10 | 11 |
| 36            | 5563 | 5575 | 5587 | 5599 | 5611 | 5623 | 5635 | 5647 | 5658 | 5670 | 1 | 2 | 4  | 5  | 6  | 7  | 8  | 9  | 10 |
| 37            | 5682 | 5694 | 5705 | 5717 | 5729 | 5740 | 5752 | 5763 | 5775 | 5786 | 1 | 2 | 3  | 5  | 6  | 7  | 8  | 9  | 10 |
| 38            | 5798 | 5809 | 5821 | 5832 | 5843 | 5855 | 5866 | 5877 | 5888 | 5899 | 1 | 2 | 3  | 5  | 6  | 7  | 8  | 9  | 10 |
| 39            | 5911 | 5922 | 5933 | 5944 | 5955 | 5966 | 5977 | 5988 | 5999 | 6010 | 1 | 2 | 3  | 4  | 5  | 7  | 8  | 9  | 10 |

## LOGARITHMS.

## Proportional Parts.

| Nat.<br>numb. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---------------|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|---|---|---|---|
| 40            | 6021 | 6031 | 6042 | 6053 | 6064 | 6075 | 6085 | 6096 | 6107 | 6117 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 41            | 6128 | 6138 | 6149 | 6160 | 6170 | 6180 | 6191 | 6201 | 6212 | 6222 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 42            | 6232 | 6243 | 6253 | 6263 | 6274 | 6284 | 6294 | 6304 | 6314 | 6325 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 43            | 6335 | 6345 | 6355 | 6365 | 6375 | 6385 | 6395 | 6405 | 6415 | 6425 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 44            | 6435 | 6444 | 6454 | 6464 | 6474 | 6484 | 6493 | 6503 | 6513 | 6522 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 45            | 6532 | 6542 | 6551 | 6561 | 6571 | 6580 | 6590 | 6599 | 6609 | 6618 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 46            | 6628 | 6637 | 6646 | 6656 | 6665 | 6675 | 6684 | 6693 | 6702 | 6712 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 7 | 8 |
| 47            | 6721 | 6730 | 6739 | 6749 | 6758 | 6767 | 6776 | 6785 | 6794 | 6803 | 1 | 2 | 3 | 4 | 5 | 5 | 6 | 7 | 8 |
| 48            | 6812 | 6821 | 6830 | 6839 | 6848 | 6857 | 6866 | 6875 | 6884 | 6893 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 | 8 |
| 49            | 6902 | 6911 | 6920 | 6928 | 6937 | 6946 | 6955 | 6964 | 6972 | 6981 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 | 7 |
| 50            | 6990 | 6998 | 7007 | 7016 | 7024 | 7033 | 7042 | 7050 | 7059 | 7067 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 | 7 |
| 51            | 7076 | 7084 | 7093 | 7101 | 7110 | 7118 | 7126 | 7135 | 7143 | 7152 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 7 | 8 |
| 52            | 7160 | 7168 | 7177 | 7185 | 7193 | 7202 | 7210 | 7218 | 7226 | 7235 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 7 | 7 |
| 53            | 7243 | 7251 | 7259 | 7267 | 7275 | 7284 | 7292 | 7300 | 7308 | 7316 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 54            | 7324 | 7332 | 7340 | 7348 | 7356 | 7364 | 7372 | 7380 | 7388 | 7396 | 1 | 2 | 2 | 3 | 4 | 5 | 6 | 6 | 7 |
| 55            | 7404 | 7412 | 7419 | 7427 | 7435 | 7443 | 7451 | 7459 | 7466 | 7474 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 56            | 7482 | 7490 | 7497 | 7505 | 7513 | 7520 | 7528 | 7536 | 7543 | 7551 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 57            | 7559 | 7566 | 7574 | 7582 | 7589 | 7597 | 7604 | 7612 | 7619 | 7627 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 |
| 58            | 7634 | 7642 | 7649 | 7657 | 7664 | 7672 | 7679 | 7686 | 7694 | 7701 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 59            | 7704 | 7716 | 7723 | 7731 | 7738 | 7745 | 7752 | 7760 | 7767 | 7774 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 |
| 60            | 7782 | 7789 | 7796 | 7803 | 7810 | 7818 | 7825 | 7832 | 7839 | 7846 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 61            | 7853 | 7860 | 7868 | 7875 | 7882 | 7889 | 7896 | 7903 | 7910 | 7917 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 6 |
| 62            | 7924 | 7931 | 7938 | 7945 | 7952 | 7959 | 7966 | 7973 | 7980 | 7987 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 6 | 6 |
| 63            | 7993 | 8000 | 8007 | 8014 | 8021 | 8028 | 8035 | 8041 | 8048 | 8055 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 64            | 8062 | 8069 | 8075 | 8082 | 8089 | 8096 | 8102 | 8109 | 8116 | 8122 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 65            | 8129 | 8136 | 8142 | 8149 | 8156 | 8162 | 8169 | 8176 | 8182 | 8189 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 66            | 8195 | 8202 | 8209 | 8215 | 8222 | 8228 | 8235 | 8241 | 8248 | 8254 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 67            | 8261 | 8267 | 8274 | 8280 | 8287 | 8293 | 8299 | 8306 | 8312 | 8319 | 1 | 1 | 2 | 3 | 3 | 4 | 5 | 5 | 6 |
| 68            | 8325 | 8331 | 8338 | 8344 | 8351 | 8357 | 8363 | 8370 | 8376 | 8382 | 1 | 1 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 69            | 8388 | 8395 | 8401 | 8407 | 8414 | 8420 | 8426 | 8432 | 8439 | 8445 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |



| Nat.<br>numb. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---------------|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|---|---|---|---|
| 70            | 8451 | 8457 | 8463 | 8470 | 8476 | 8482 | 8488 | 8494 | 8500 | 8506 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 6 |
| 71            | 8513 | 8519 | 8525 | 8531 | 8537 | 8543 | 8549 | 8555 | 8561 | 8567 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 72            | 8573 | 8579 | 8585 | 8591 | 8597 | 8603 | 8609 | 8615 | 8621 | 8627 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 73            | 8633 | 8639 | 8645 | 8651 | 8657 | 8663 | 8669 | 8675 | 8681 | 8686 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 74            | 8692 | 8698 | 8704 | 8710 | 8716 | 8722 | 8727 | 8733 | 8739 | 8745 | 1 | 1 | 2 | 2 | 3 | 4 | 4 | 5 | 5 |
| 75            | 8751 | 8756 | 8762 | 8768 | 8774 | 8779 | 8785 | 8791 | 8797 | 8802 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 76            | 8808 | 8814 | 8820 | 8825 | 8831 | 8837 | 8842 | 8848 | 8854 | 8859 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 5 | 5 |
| 77            | 8865 | 8871 | 8876 | 8882 | 8887 | 8893 | 8899 | 8904 | 8910 | 8915 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 78            | 8921 | 8927 | 8932 | 8938 | 8943 | 8949 | 8954 | 8960 | 8965 | 8971 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 79            | 8976 | 8982 | 8987 | 8993 | 8998 | 9004 | 9009 | 9015 | 9020 | 9025 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 80            | 9031 | 9036 | 9042 | 9047 | 9053 | 9058 | 9063 | 9069 | 9074 | 9079 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 81            | 9085 | 9090 | 9096 | 9101 | 9106 | 9112 | 9117 | 9122 | 9128 | 9133 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 82            | 9138 | 9143 | 9149 | 9154 | 9159 | 9165 | 9170 | 9175 | 9180 | 9186 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 83            | 9191 | 9196 | 9201 | 9206 | 9212 | 9217 | 9222 | 9227 | 9232 | 9238 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 84            | 9243 | 9248 | 9253 | 9258 | 9263 | 9269 | 9274 | 9279 | 9284 | 9289 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 85            | 9294 | 9299 | 9304 | 9309 | 9315 | 9320 | 9325 | 9330 | 9335 | 9340 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 86            | 9345 | 9350 | 9355 | 9360 | 9365 | 9370 | 9375 | 9380 | 9385 | 9390 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 87            | 9395 | 9400 | 9405 | 9410 | 9415 | 9420 | 9425 | 9430 | 9435 | 9440 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 88            | 9445 | 9450 | 9455 | 9460 | 9465 | 9469 | 9474 | 9479 | 9484 | 9489 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 89            | 9494 | 9499 | 9504 | 9509 | 9513 | 9518 | 9523 | 9528 | 9533 | 9538 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 90            | 9542 | 9547 | 9552 | 9557 | 9562 | 9566 | 9571 | 9576 | 9581 | 9586 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 91            | 9590 | 9595 | 9600 | 9605 | 9609 | 9614 | 9619 | 9624 | 9628 | 9633 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 92            | 9638 | 9643 | 9647 | 9652 | 9657 | 9661 | 9666 | 9671 | 9675 | 9680 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 93            | 9685 | 9689 | 9694 | 9699 | 9703 | 9708 | 9713 | 9717 | 9722 | 9727 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 94            | 9731 | 9736 | 9741 | 9745 | 9750 | 9754 | 9759 | 9763 | 9768 | 9773 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 95            | 9777 | 9782 | 9786 | 9791 | 9795 | 9800 | 9805 | 9809 | 9814 | 9818 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 96            | 9823 | 9827 | 9832 | 9836 | 9841 | 9845 | 9850 | 9854 | 9859 | 9863 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 97            | 9868 | 9872 | 9877 | 9881 | 9886 | 9890 | 9894 | 9899 | 9903 | 9908 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 98            | 9912 | 9917 | 9921 | 9926 | 9930 | 9934 | 9939 | 9943 | 9948 | 9952 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |
| 99            | 9956 | 9961 | 9965 | 9969 | 9974 | 9978 | 9983 | 9987 | 9991 | 9996 | 0 | 1 | 1 | 2 | 2 | 2 | 3 | 3 | 4 |

## ANTI-LOGARITHMS.

Proportional Parts.

| Log. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|------|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|---|---|---|---|
| '00  | 1000 | 1002 | 1005 | 1007 | 1009 | 1012 | 1014 | 1016 | 1019 | 1021 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 2 | 2 |
| '01  | 1023 | 1026 | 1028 | 1030 | 1033 | 1035 | 1038 | 1040 | 1042 | 1045 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| '02  | 1047 | 1050 | 1052 | 1054 | 1057 | 1059 | 1062 | 1064 | 1067 | 1069 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| '03  | 1072 | 1074 | 1076 | 1079 | 1081 | 1084 | 1086 | 1089 | 1091 | 1094 | 0 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 |
| '04  | 1096 | 1099 | 1102 | 1104 | 1107 | 1109 | 1112 | 1114 | 1117 | 1119 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| '05  | 1122 | 1125 | 1127 | 1130 | 1132 | 1135 | 1138 | 1140 | 1143 | 1146 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| '06  | 1148 | 1151 | 1153 | 1156 | 1159 | 1161 | 1164 | 1167 | 1169 | 1172 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| '07  | 1175 | 1178 | 1180 | 1183 | 1186 | 1189 | 1191 | 1194 | 1197 | 1199 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| '08  | 1202 | 1205 | 1208 | 1211 | 1213 | 1216 | 1219 | 1222 | 1225 | 1227 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| '09  | 1230 | 1233 | 1236 | 1239 | 1242 | 1245 | 1247 | 1250 | 1253 | 1256 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| '10  | 1259 | 1262 | 1265 | 1268 | 1271 | 1274 | 1276 | 1279 | 1282 | 1285 | 0 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 3 |
| '11  | 1288 | 1291 | 1294 | 1297 | 1300 | 1303 | 1306 | 1309 | 1312 | 1315 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 |
| '12  | 1318 | 1321 | 1324 | 1327 | 1330 | 1334 | 1337 | 1340 | 1343 | 1346 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 2 | 3 |
| '13  | 1349 | 1352 | 1355 | 1358 | 1361 | 1365 | 1368 | 1371 | 1374 | 1377 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| '14  | 1380 | 1384 | 1387 | 1390 | 1393 | 1396 | 1400 | 1403 | 1406 | 1409 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| '15  | 1413 | 1416 | 1419 | 1422 | 1426 | 1429 | 1432 | 1435 | 1439 | 1442 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| '16  | 1445 | 1449 | 1452 | 1455 | 1459 | 1462 | 1466 | 1469 | 1472 | 1476 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| '17  | 1479 | 1483 | 1486 | 1489 | 1493 | 1496 | 1500 | 1503 | 1507 | 1510 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| '18  | 1514 | 1517 | 1521 | 1524 | 1528 | 1531 | 1535 | 1538 | 1542 | 1545 | 0 | 1 | 1 | 1 | 2 | 2 | 2 | 3 | 3 |
| '19  | 1549 | 1552 | 1556 | 1560 | 1563 | 1567 | 1570 | 1574 | 1578 | 1581 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 |
| '20  | 1585 | 1589 | 1592 | 1596 | 1600 | 1603 | 1607 | 1611 | 1614 | 1618 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 |
| '21  | 1622 | 1626 | 1629 | 1633 | 1637 | 1641 | 1644 | 1648 | 1652 | 1656 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 |
| '22  | 1660 | 1663 | 1667 | 1671 | 1675 | 1679 | 1683 | 1687 | 1690 | 1694 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 3 |
| '23  | 1698 | 1702 | 1706 | 1710 | 1714 | 1718 | 1722 | 1726 | 1730 | 1734 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |
| '24  | 1738 | 1742 | 1746 | 1750 | 1754 | 1758 | 1762 | 1766 | 1770 | 1774 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |
| '25  | 1778 | 1782 | 1786 | 1791 | 1795 | 1799 | 1803 | 1807 | 1811 | 1816 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |
| '26  | 1820 | 1824 | 1828 | 1832 | 1837 | 1841 | 1845 | 1849 | 1854 | 1858 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |
| '27  | 1862 | 1866 | 1871 | 1875 | 1879 | 1884 | 1886 | 1892 | 1897 | 1901 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |
| '28  | 1905 | 1910 | 1914 | 1919 | 1923 | 1928 | 1932 | 1936 | 1941 | 1945 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |
| '29  | 1950 | 1954 | 1959 | 1963 | 1968 | 1973 | 1977 | 1982 | 1986 | 1991 | 0 | 1 | 1 | 1 | 2 | 2 | 3 | 3 | 4 |

| Log. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|------|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|---|---|---|---|
| 30   | 1995 | 2000 | 2004 | 2009 | 2014 | 2018 | 2023 | 2028 | 2032 | 2037 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |
| 31   | 2042 | 2046 | 2051 | 2056 | 2061 | 2065 | 2070 | 2075 | 2080 | 2084 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |
| 32   | 2089 | 2094 | 2099 | 2104 | 2108 | 2113 | 2118 | 2123 | 2128 | 2133 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |
| 33   | 2138 | 2143 | 2148 | 2153 | 2158 | 2163 | 2168 | 2173 | 2178 | 2183 | 0 | 1 | 1 | 2 | 2 | 3 | 3 | 3 | 4 |
| 34   | 2188 | 2193 | 2198 | 2203 | 2208 | 2213 | 2218 | 2223 | 2228 | 2234 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 35   | 2239 | 2244 | 2249 | 2254 | 2259 | 2265 | 2270 | 2275 | 2280 | 2286 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 36   | 2291 | 2296 | 2301 | 2307 | 2312 | 2317 | 2323 | 2328 | 2333 | 2339 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 37   | 2344 | 2350 | 2355 | 2360 | 2366 | 2371 | 2377 | 2382 | 2388 | 2393 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 38   | 2399 | 2404 | 2410 | 2415 | 2421 | 2427 | 2432 | 2438 | 2443 | 2449 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 39   | 2455 | 2460 | 2466 | 2472 | 2477 | 2483 | 2489 | 2495 | 2500 | 2506 | 1 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 |
| 40   | 2512 | 2518 | 2523 | 2529 | 2535 | 2541 | 2547 | 2553 | 2559 | 2564 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 41   | 2570 | 2576 | 2582 | 2588 | 2594 | 2600 | 2606 | 2612 | 2618 | 2624 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 42   | 2630 | 2636 | 2642 | 2649 | 2655 | 2661 | 2667 | 2673 | 2679 | 2685 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 43   | 2692 | 2698 | 2704 | 2710 | 2716 | 2723 | 2729 | 2735 | 2742 | 2748 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 44   | 2754 | 2761 | 2767 | 2773 | 2780 | 2786 | 2793 | 2799 | 2805 | 2812 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 45   | 2818 | 2825 | 2831 | 2838 | 2844 | 2851 | 2858 | 2864 | 2871 | 2877 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 46   | 2884 | 2891 | 2897 | 2904 | 2911 | 2917 | 2924 | 2931 | 2938 | 2944 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 47   | 2951 | 2958 | 2965 | 2972 | 2979 | 2985 | 2992 | 2999 | 3006 | 3013 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 48   | 3020 | 3027 | 3034 | 3041 | 3048 | 3055 | 3062 | 3069 | 3076 | 3083 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 49   | 3090 | 3097 | 3105 | 3112 | 3119 | 3126 | 3133 | 3141 | 3148 | 3155 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 5 |
| 50   | 3162 | 3170 | 3177 | 3184 | 3192 | 3199 | 3206 | 3214 | 3221 | 3228 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 51   | 3236 | 3243 | 3251 | 3258 | 3266 | 3273 | 3281 | 3289 | 3296 | 3304 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 52   | 3311 | 3319 | 3327 | 3334 | 3342 | 3350 | 3357 | 3365 | 3373 | 3381 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 53   | 3388 | 3396 | 3404 | 3412 | 3420 | 3428 | 3436 | 3443 | 3451 | 3459 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 54   | 3467 | 3475 | 3483 | 3491 | 3499 | 3508 | 3516 | 3524 | 3532 | 3540 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 55   | 3548 | 3556 | 3565 | 3573 | 3581 | 3589 | 3597 | 3606 | 3614 | 3622 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 56   | 3631 | 3639 | 3648 | 3656 | 3664 | 3673 | 3681 | 3690 | 3698 | 3707 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 57   | 3715 | 3724 | 3733 | 3741 | 3750 | 3758 | 3767 | 3776 | 3784 | 3793 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 58   | 3802 | 3811 | 3819 | 3828 | 3837 | 3846 | 3855 | 3864 | 3873 | 3882 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |
| 59   | 3890 | 3899 | 3908 | 3917 | 3926 | 3936 | 3945 | 3954 | 3963 | 3972 | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 5 | 6 |

## ANTI-LOGARITHMS.

Proportional Parts.

| Log. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
|------|------|------|------|------|------|------|------|------|------|------|---|---|---|---|---|----|----|----|----|
| .60  | 3981 | 3990 | 3999 | 4009 | 4018 | 4027 | 4036 | 4046 | 4955 | 4064 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .61  | 4074 | 4083 | 4093 | 4102 | 4111 | 4121 | 4130 | 4140 | 4150 | 4159 | 1 | 2 | 3 | 4 | 5 | 6  | 6  | 7  | 8  |
| .62  | 4169 | 4178 | 4188 | 4198 | 4207 | 4217 | 4227 | 4236 | 4246 | 4256 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .63  | 4266 | 4276 | 4285 | 4295 | 4305 | 4315 | 4325 | 4335 | 4345 | 4355 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .64  | 4365 | 4375 | 4385 | 4395 | 4406 | 4416 | 4426 | 4436 | 4446 | 4457 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .65  | 4467 | 4477 | 4487 | 4498 | 4508 | 4519 | 4529 | 4539 | 4550 | 4560 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .66  | 4571 | 4581 | 4592 | 4603 | 4613 | 4624 | 4634 | 4645 | 4656 | 4667 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .67  | 4677 | 4688 | 4699 | 4710 | 4721 | 4732 | 4742 | 4753 | 4764 | 4775 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .68  | 4786 | 4797 | 4808 | 4819 | 4831 | 4842 | 4853 | 4864 | 4875 | 4887 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .69  | 4898 | 4909 | 4920 | 4932 | 4943 | 4955 | 4966 | 4977 | 4989 | 5000 | 1 | 2 | 3 | 4 | 5 | 6  | 7  | 8  | 9  |
| .70  | 5012 | 5023 | 5035 | 5047 | 5058 | 5070 | 5082 | 5093 | 5105 | 5117 | 1 | 2 | 4 | 5 | 6 | 7  | 8  | 9  | 11 |
| .71  | 5129 | 5140 | 5152 | 5164 | 5176 | 5188 | 5200 | 5212 | 5224 | 5236 | 1 | 2 | 4 | 5 | 6 | 7  | 8  | 10 | 11 |
| .72  | 5248 | 5260 | 5272 | 5284 | 5297 | 5309 | 5321 | 5333 | 5346 | 5358 | 1 | 2 | 4 | 5 | 6 | 7  | 9  | 10 | 11 |
| .73  | 5370 | 5383 | 5395 | 5408 | 5420 | 5433 | 5445 | 5458 | 5470 | 5483 | 1 | 3 | 4 | 5 | 6 | 8  | 9  | 10 | 11 |
| .74  | 5495 | 5508 | 5521 | 5534 | 5546 | 5559 | 5572 | 5585 | 5598 | 5610 | 1 | 3 | 4 | 5 | 6 | 8  | 9  | 10 | 12 |
| .75  | 5623 | 5636 | 5649 | 5662 | 5675 | 5689 | 5702 | 5715 | 5728 | 5741 | 1 | 3 | 4 | 5 | 7 | 8  | 9  | 10 | 12 |
| .76  | 5754 | 5768 | 5781 | 5794 | 5808 | 5821 | 5834 | 5848 | 5861 | 5875 | 1 | 3 | 4 | 5 | 7 | 8  | 9  | 11 | 12 |
| .77  | 5888 | 5902 | 5916 | 5929 | 5943 | 5957 | 5970 | 5984 | 5998 | 6012 | 1 | 3 | 4 | 5 | 7 | 8  | 10 | 11 | 12 |
| .78  | 6026 | 6039 | 6053 | 6067 | 6081 | 6095 | 6109 | 6124 | 6138 | 6152 | 1 | 3 | 4 | 6 | 7 | 8  | 10 | 11 | 13 |
| .79  | 6166 | 6180 | 6194 | 6209 | 6223 | 6237 | 6252 | 6266 | 6281 | 6295 | 1 | 3 | 4 | 6 | 7 | 9  | 10 | 11 | 13 |
| .80  | 6310 | 6324 | 6339 | 6353 | 6368 | 6383 | 6397 | 6412 | 6427 | 6442 | 1 | 3 | 4 | 6 | 7 | 9  | 10 | 12 | 13 |
| .81  | 6457 | 6471 | 6486 | 6501 | 6516 | 6531 | 6546 | 6561 | 6577 | 6592 | 2 | 3 | 5 | 6 | 8 | 9  | 11 | 12 | 14 |
| .82  | 6607 | 6622 | 6637 | 6653 | 6668 | 6683 | 6699 | 6714 | 6730 | 6745 | 2 | 3 | 5 | 6 | 8 | 9  | 11 | 13 | 14 |
| .83  | 6761 | 6776 | 6792 | 6808 | 6823 | 6839 | 6855 | 6871 | 6887 | 6902 | 2 | 3 | 5 | 6 | 8 | 9  | 11 | 14 | 15 |
| .84  | 6918 | 6934 | 6950 | 6966 | 6982 | 6998 | 7015 | 7031 | 7047 | 7065 | 2 | 3 | 5 | 6 | 8 | 10 | 11 | 13 | 15 |
| .85  | 7079 | 7096 | 7112 | 7129 | 7145 | 7161 | 7178 | 7194 | 7211 | 7228 | 2 | 3 | 5 | 7 | 8 | 10 | 12 | 13 | 15 |
| .86  | 7244 | 7261 | 7278 | 7295 | 7311 | 7328 | 7345 | 7362 | 7379 | 7396 | 2 | 3 | 5 | 7 | 8 | 10 | 12 | 14 | 15 |
| .87  | 7413 | 7430 | 7447 | 7464 | 7482 | 7499 | 7516 | 7534 | 7551 | 7568 | 2 | 3 | 5 | 7 | 9 | 10 | 12 | 14 | 16 |
| .88  | 7586 | 7603 | 7621 | 7638 | 7656 | 7674 | 7691 | 7709 | 7727 | 7745 | 2 | 4 | 5 | 7 | 9 | 11 | 12 | 14 | 16 |
| .89  | 7762 | 7780 | 7798 | 7816 | 7834 | 7852 | 7870 | 7889 | 7907 | 7925 | 2 | 4 | 5 | 7 | 9 | 11 | 13 | 14 | 16 |

## ANTI-LOGARITHMS.

Proportional Parts.

| Log. | 0    | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 1 | 2 | 3 | 4 | 5  | 6  | 7  | 8  | 9  |
|------|------|------|------|------|------|------|------|------|------|------|---|---|---|---|----|----|----|----|----|
| '90  | 7943 | 7962 | 7980 | 7998 | 8017 | 8035 | 8054 | 8072 | 8091 | 8110 | 2 | 4 | 6 | 7 | 9  | 11 | 13 | 15 | 17 |
| '91  | 8123 | 8147 | 8166 | 8185 | 8204 | 8222 | 8241 | 8260 | 8279 | 8299 | 2 | 4 | 6 | 8 | 9  | 11 | 13 | 15 | 17 |
| '92  | 8318 | 8337 | 8356 | 8375 | 8395 | 8414 | 8433 | 8453 | 8472 | 8492 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 15 | 17 |
| '93  | 8511 | 8531 | 8551 | 8570 | 8590 | 8610 | 8630 | 8650 | 8670 | 8690 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| '94  | 8710 | 8730 | 8750 | 8770 | 8790 | 8810 | 8831 | 8851 | 8872 | 8892 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
| '95  | 8913 | 8933 | 8954 | 8974 | 8995 | 9016 | 9036 | 9057 | 9078 | 9099 | 2 | 4 | 6 | 8 | 10 | 12 | 15 | 17 | 19 |
| '96  | 9120 | 9141 | 9162 | 9183 | 9204 | 9226 | 9247 | 9268 | 9290 | 9311 | 2 | 4 | 6 | 8 | 11 | 13 | 15 | 17 | 19 |
| '97  | 9338 | 9354 | 9376 | 9397 | 9419 | 9441 | 9462 | 9484 | 9506 | 9528 | 2 | 4 | 7 | 9 | 11 | 13 | 15 | 17 | 20 |
| '98  | 9550 | 9572 | 9594 | 9616 | 9638 | 9661 | 9683 | 9705 | 9727 | 9750 | 2 | 4 | 7 | 9 | 11 | 13 | 16 | 18 | 20 |
| '99  | 9772 | 9795 | 9817 | 9840 | 9863 | 9886 | 9908 | 9931 | 9954 | 9977 | 2 | 5 | 7 | 9 | 11 | 14 | 16 | 18 | 20 |



A KEY  
TO THE SERIES OF  
CHEMICAL PROBLEMS





## KEY TO CHEMICAL PROBLEMS.

### METRIC SYSTEM OF WEIGHTS AND MEASURES.

1. 43·7 millimetres : 4·37 centimetres.
2. 109876542·1 centimetres : 10987654·21 decimetres : 1098765·421 metres.
3. 70 square decimetres : 7,000 square centimetres : 700,000 square millimetres.
4. The weight of a cubic centimetre of pure water weighed at 4° C. in the latitude of Paris, is styled a gram. A litre denotes a volume equivalent to 1 cubic decimetre. 1,725 grams.
5. 256,700 centigrams.
6. 5,000 milligrams.
7. 78·54 square centimetres.
8. 1·60931 kilometres.
9. 761·985 millimetres.
10. 567·875 cubic centimetres.
11. 113·097 cubic centimetres.

12. 12,732,394 metres  
 13. 14·826 millimetres.  
 14. 7 pieces and 0·023 gram will remain.  
 15. (a) 0·00083 gram, (b) 0·00148 gram, (c) 0·00231 gram, (d) 0·00333 gram, (e) 0·00593 gram, (f) 0·00926 gram.  
 16. 3·76 millimetres.  
 17. 8·305 centimetres.  
 18. 1·4 millimetres. 0·25 gram.  
 19. 1·11 cubic centimetres.  
 20. 50·10 cubic centimetres.  
 21. — 0·03 c.c., + 0·20 c.c., + 0·41 c.c.

### CONVERSION OF THERMOMETRIC SCALES.

- |   |             |             |
|---|-------------|-------------|
| 22. 15°·5 C.  | 0° C.       | — 12°·5 C.  |
| 100°·0 C.   | — 26°·38 C. | 31°·87 C.   |
| 17°·7 C.  | 260°·0 C.   | — 17°·6 C.  |
| 23. 12°·5 R.  | 519°·1 R.   | 0°·20 R.    |
| 12°·44 R.   | — 32°·0 R.  | — 14°·22 R. |
| 0°·0 R.   | 192°·0 R.   | — 7°·55 R.  |
| 24. 39°·2 F.  | 59°·0 F.    | 413°·6 F.   |
| 59°·9 F.  | 32°·18 F.   | 842°·0 F.   |
| 140°·0 F.   | 212°·0 F.   | 33°·8 F.    |
| 25. 59°·28 C.                                       |             |             |
| 26. 94°·82 F., 173°·12 F., 640°·4 F.                |             |             |
| 27. — 31°·04 R., — 37·84° F.; 285°·8 R., 675°·05 F. |             |             |
| 28. 2822° F., 793°·4 F. 633°·2 F., 455° F.          |             |             |
| 29. — 40°, — 32° R.                                 |             |             |

## CORRECTION OF THERMOMETER READINGS.

30.  $57^{\circ}4$ .
31. (a)  $150^{\circ}76$  to  $151^{\circ}56$ , (b)  $151^{\circ}56$  to  $152^{\circ}17$ ,  
(c)  $152^{\circ}17$  to  $152^{\circ}38$ , (d)  $152^{\circ}38$  to  $152^{\circ}78$ .
32.  $131^{\circ}54$  to  $131^{\circ}64$ ;  $131^{\circ}64$  to  $131^{\circ}74$ .
33.  $21^{\circ}78$ ,  $58^{\circ}11$ ,  $76^{\circ}22$ ,  $107^{\circ}32$ ,  $127^{\circ}37$ .

## CORRECTION OF BAROMETER READINGS.

34.  $752^{\circ}82$  mm.,  $754^{\circ}20$  mm.,  $755^{\circ}38$  mm.,  $756^{\circ}25$  mm.
35.  $753^{\circ}29$  mm.,  $752^{\circ}69$  mm.,  $750^{\circ}57$  mm.,  $749^{\circ}97$  mm.
36. A.  $752^{\circ}63$  mm. E.  $755^{\circ}49$  mm.  
B.  $760^{\circ}72$  mm. F.  $758^{\circ}87$  mm.  
C.  $755^{\circ}58$  mm. G.  $762^{\circ}30$  mm.  
D.  $761^{\circ}75$  mm.

CORRECTION OF THE VOLUMES OF GASES  
FOR TEMPERATURE AND PRESSURE;  
LAW OF PARTIAL PRESSURES.

37.  $163^{\circ}992$  volumes.
38.  $1^{\circ}3663$  litres.
39.  $13^{\circ}3746$  litres.
40. (a)  $1585^{\circ}165$  cubic centimetres, (b)  $1774^{\circ}725$  cubic centimetres, (c)  $2049^{\circ}45$  cubic centimetres, (d)  $3148^{\circ}35$  cubic centimetres.  $-91^{\circ}$  C.
41.  $0^{\circ}002036$  for  $1^{\circ}$  F.,  $0^{\circ}004581$  for  $1^{\circ}$  R
42. From  $760$  mm. to  $767^{\circ}77$  mm.
43.  $1743^{\circ}4$  cubic metres.

44. 143.518 c.c.

45. 3677° C.

46. The volume reduced to 0° C. and 760 mm. of the added hydrogen will be 24.10 c.c.

The reading of the upper level of Hg = 423.1 mm.

47. 1.68 per cent.

48. 1.66 per cent., and 0.85 per cent.

49. 48.79 c.c.

50. 24.06 c.c.

## RELATIVE DENSITY OF SOLIDS, LIQUIDS, AND GASES ; VAPOUR DENSITY.

51. 6.503.

52. 19.11.

53. Granite 2.72 ; marble 2.68 ; hæmatite 5.07.

54. 0.8793.

55. 0.268 mm.

56. 0.49 mm.

57. 0.0000219 mm.

58. Relative density of alloy is 8.516.

Percentage of copper = 74.7.

„ „ tin = 25.3.

59. 3 cubic centimetres.

60. 1.58.

61. Quartz 2.65 ; heavy-spar 4.48 ;  
calcite 2.72 ; iron pyrites 5.0.

62. 1.0272.

63. *A.* 1.00585 ; *B.* 1.841 ; *C.* 1.920 ; *D.* 0.792.

64. Sulphuric acid 1·84 ; mercury 13·54.  
 65. 0·8.  
 66. Metal 2·7, liquid 1·19.  
 67. (a) 1·26 ; (b) 0·915 ; (c) 0·87.  
 68. Glycerine 1·26 ; mercury 13·598.  
 69. 0·97176.  
 70. 0·06935.  
 71. 59·56.  
 72. 1·177 ; 16·99.  
 73. (Air = 1). 1·773 ; 1·712 ; 1·578 ; 1·377 ;  
                   1·321 ; 1·270 ; 1·115 ; 1·021.  
       (H = 1). 25·59 ; 24·71 ; 22·77 ; 19·87 ;  
                   19·06 ; 18·33 ; 16·10 ; 14·73.  
 74. 47·29.  
 75. (1). 0·0792 ; 1·1205 ; 1·5292.  
       (2). 0·0770 ; 1·1199 ; 1·5414.  
 76.       I.                   II.                   III.  
       (A).   7·67               7·71.               7·69.  
       (B). 110·7               111·29.               111·0.  
 77. (A). 49·60 ; (B). 44·70 ; (C). 36·07 ;  
       (D). 34·95 ; (E). 35·54.  
 78. 50·29.   4·494 grams.  
 79. I. 5·75 ; II. 5·74.  
 80. (Air = 1). A. 4·036 ; B. 2·621 ; C. 0·6012 ; D. 8·665.  
       (H = 1). A. 58·26 ; B. 37·83 ; C. 8·678 ; D. 125·1  
 81. 347·96 kilos.  
 82. 51·77.  
 83. 76·33.  
 84. I. 2·21 ; II. 2·30 ; III. 2·20.  
 85. 137·7 (H = 1).

# DENSITY AND MOLECULAR WEIGHT; VALENCY, EQUIVALENTS, AND ATOMIC WEIGHTS.

86.  $\text{SH}_2$ , 34.38 ;  $\text{NH}_3$ , 17.23 ;  $\text{N}_2\text{O}$ , 43.88 ;  $\text{CH}_4$ , 16.02 ;  
 $\text{CHCl}_3$ , 121.25 ;  $\text{SnCl}_4$ , 265.6.

|                      |              |
|----------------------|--------------|
| 87. Oxygen . . . . . | 1.4297 gram. |
| Chlorine . . . . .   | 3.1666 „     |
| Iodine . . . . .     | 11.3355 „    |
| Sulphur . . . . .    | 2.8648 „     |
| Phosphorus . . . . . | 5.546 „      |
| Nitrogen . . . . .   | 1.255 „      |
| Sodium . . . . .     | 2.0598 „     |
| Arsenic . . . . .    | 13.419 „     |
| Mercury . . . . .    | 8.949 „      |

|                         |               |
|-------------------------|---------------|
| 88. Carbon monoxide . . | 799.3 litres. |
| Hydrogen sulphide . .   | 657.0 „       |
| Marsh gas . . . . .     | 1397.7 „      |
| Water . . . . .         | 1243.1 „      |
| Ethylene . . . . .      | 799.1 „       |
| Carbon oxysulphide . .  | 372.6 „       |
| Bromine . . . . .       | 139.9 „       |
| Hydrochloric acid. . .  | 613.8 „       |

89.  $\text{PbCl}_2$ , 277.13 gm ;  $\text{Si F}_4$ , 104.24 gm ;  
 $\text{Fe Cl}_3$ , 161.99 „ ;  $\text{CH}_3\text{Br}$ , 94.73 „ .

90.  $\text{CO}$ , 0.967 ;  $\text{CS}_2$ , 2.630 ;  $\text{SO}_3$ , 2.766 ;  $\text{BF}_3$ , 2.358 ;  
 $\text{PF}_5$ , 4.373.

91. O, 15.96 ; Ag, 107.66 ; Cl, 35.37 ; Sb, 119.58 ;  
Cu, 63.18.

92. The most probable value for the atomic weight of oxygen is 15.96, for this number represents the smallest quantity by weight of oxygen occurring in the molecular weight of any of the given compounds.

93. The approximate molecular weights, calculated from the relative density in each case, are :—16.0 ; 141.0 ; 121.3 ; 27.96 ; 76.4,—hence the parts given in the third column

refer to parts by weight per molecule and therefore the atomic weight of carbon is 11'97.

94. Cd, 113'7; P, 125'6; Hg, 201'5.

95. Atomic weight of phosphorus 30'96. From molecular weight found above, molecule is  $P_4$ .

## DEDUCTION OF EMPIRICAL FORMULA FROM PERCENTAGE COMPOSITION, FORMULÆ OF MINERALS.

96.  $H_2O_2$ . 97.  $NO_2$ . 98.  $Fe_2O_3$ . 99. COS.

100.  $KHSO_4$ . 101.  $MgSO_4 + 7H_2O$ .

102.  $ZnSO_4 + 7H_2O$ . 103.  $Ca_3P_2O_8$ . 104.  $Na_3AlF_6$ .

105.  $KNO_2$ . 106.  $Al_2(SO_4)_3$ .

107.  $CuCO_3 + CuH_2O_2$ . 108.  $NiSO_4 \cdot 2NH_3$ .

109.  $C_nH_{2n}$ . 110.  $C_2H_2$ . 111.  $C_2H_6SO_4$ . 112.  $C_{10}H_{14}N_2$ .

113.  $(C_{21}H_{22}N_2O_2)_2H_2PtCl_6$ .

114. A comparison of the amount of oxygen contained in the various bases with that contained in the acid, shows that the two quantities are in the ratio of 1 : 2, in conformity with the formula  $MOCO_2$  thus—

|                         |      | <i>Containing oxygen.</i> | <i>Ratio.</i> |
|-------------------------|------|---------------------------|---------------|
| CaO . . . .             | 28'4 | 8'11                      | 16'19         |
| MgO . . . .             | 12'3 | 4'92                      |               |
| FeO . . . .             | 12'3 | 2'73                      |               |
| MnO . . . .             | 1'9  | 0'43                      |               |
| CO <sub>2</sub> . . . . | 44'4 | 32'3                      | 2             |
|                         | 99'3 |                           |               |

115.  $2(MgO \cdot SiO_2) + 3H_2O$ .

116.  $Co_3As_2O_8 + 8H_2O$ .

117.  $Na_2O \cdot Al_2O_3 \cdot 6SiO_2$ .

118.  $3CaO, Na_2O, 4Al_2O_3, 12SiO_2$ .

# TO CALCULATE THE PERCENTAGE COMPOSITION OF A COMPOUND FROM ITS FORMULA.

|                            |                            |
|----------------------------|----------------------------|
| 119. Hydrogen . . . 11'14  | 125. Calcium . . . 40'00   |
| Oxygen . . . 88'86         | Carbon . . . 12'01         |
| <hr/>                      | Oxygen . . . 47'99         |
| 100'00                     | <hr/>                      |
| <hr/>                      | 100'00                     |
| 120. Potassium . . . 31'92 | 126. Silver . . . 75'27    |
| Chlorine . . . 28'93       | Chlorine . . . 24'73       |
| Oxygen . . . 39'15         | <hr/>                      |
| <hr/>                      | 100'00                     |
| 100'00                     | <hr/>                      |
| <hr/>                      | 127. Magnesium . . . 21'61 |
| 121. Mercury . . . 92'57   | Phosphorus . . . 27'95     |
| Oxygen . . . 7'43          | Oxygen . . . 50'44         |
| <hr/>                      | <hr/>                      |
| 100'00                     | 100'00                     |
| <hr/>                      | <hr/>                      |
| 122. Potassium . . . 38'67 | 128. Potassium . . . 16'11 |
| Nitrogen . . . 13'88       | Platinum . . . 40'10       |
| Oxygen . . . 47'45         | Chlorine . . . 43'79       |
| <hr/>                      | <hr/>                      |
| 100'00                     | 100'00                     |
| <hr/>                      | <hr/>                      |
| 123. Sodium . . . 27'09    | 129. Sodium . . . 18'57    |
| Nitrogen . . . 16'50       | Sulphur . . . 25'83        |
| Oxygen . . . 56'41         | Oxygen . . . 19'33         |
| <hr/>                      | Water . . . 36'27          |
| 100'00                     | <hr/>                      |
| <hr/>                      | 100'00                     |
| <hr/>                      | <hr/>                      |
| 124. Barium . . . 58'82    | Or—Sodium . . . 18'57      |
| Sulphur . . . 13'74        | Sulphur . . . 25'83        |
| Oxygen . . . 27'44         | Hydrogen . . . 4'04        |
| <hr/>                      | Oxygen . . . 51'56         |
| 100'00                     | <hr/>                      |
| <hr/>                      | 100'00                     |
|                            | <hr/>                      |



|   |                           |
|---|---------------------------|
| 130. Iron . . . . 72'42                         | 136. Lithia . . . . 6'44  |
| Oxygen . . . . 27'58                            | Alumina. . . . 29'21      |
| <hr/>   | Silica. . . . 64'35       |
| 100'00  | <hr/>                     |
| <hr/>   | 100'00                    |
| <hr/>   | <hr/>                     |
| 131. Manganese. . . 72'03                       | 137. Lime. . . . 44'42    |
| Oxygen . . . . 27'97                            | Silicon dioxide 23'82     |
| <hr/>   | Titanium „ 31'76          |
| 100'00  | <hr/>                     |
| <hr/>   | 100'00                    |
| <hr/>   | <hr/>                     |
| 132. Copper . . . . 34'52                       | 138. Lead . . . . 76'34   |
| Iron . . . . 30'53                              | Phosphorus . . 6'87       |
| Sulphur. . . . 34'95                            | Chlorine. . . . 2'62      |
| <hr/>   | Oxygen . . . . 14'17      |
| 100'00  | <hr/>                     |
| <hr/>   | 100'00                    |
| <hr/>   | <hr/>                     |
| 133. Silver . . . . 53'07                       | 139. Carbon . . . . 52'16 |
| Copper . . . . 31'15                            | Hydrogen . . . 13'07      |
| Sulphur. . . . 15'88                            | Oxygen. . . . 34'77       |
| <hr/>   | <hr/>                     |
| 100'00  | 100'00                    |
| <hr/>   | <hr/>                     |
| <hr/>   | <hr/>                     |
| 134. Lime (CaO) . . 9'20                        | 140. Carbon . . . . 42'10 |
| Alumina (Al <sub>2</sub> O <sub>3</sub> ) 16'79 | Hydrogen . . . 6'45       |
| Silica (SiO <sub>2</sub> ) . . 59'21            | Oxygen . . . . 51'45      |
| Water . . . . 14'80                             | <hr/>                     |
| <hr/>   | 100'00                    |
| 100'00  | <hr/>                     |
| <hr/>   | <hr/>                     |
| <hr/>   | <hr/>                     |
| 135. Lime. . . . 43'49                          | 141. Carbon . . . . 90'54 |
| Alumina. . . . 17'64                            | Hydrogen . . . 9'46       |
| Silica. . . . 38'87                             | <hr/>                     |
| <hr/>   | 100'00                    |
| 100'00  | <hr/>                     |
| <hr/>   | <hr/>                     |

|                            |                         |
|----------------------------|-------------------------|
| 142. Carbon . . . 89'53    | 146. Carbon . . . 32'18 |
| Hydrogen . . . 10'47       | Hydrogen . . . 6'05     |
| <hr/>                      | Nitrogen . . . 28'25    |
| 100'00                     | Oxygen . . . 21'45      |
| <hr/>                      | Water . . . 12'07       |
|                            | <hr/>                   |
|                            | 100'00                  |
|                            | <hr/>                   |
| 143. Silicon . . . 19'48   | 147. Carbon . . . 75'19 |
| Carbon . . . 66'61         | Hydrogen . . . 6'60     |
| Hydrogen . . . 13'91       | Nitrogen . . . 13'20    |
| <hr/>                      | Oxygen . . . 5'01       |
| 100'00                     | <hr/>                   |
| <hr/>                      | 100'00                  |
|                            | <hr/>                   |
| 144. Carbon . . . 21'02    | 148. Carbon . . . 75'41 |
| Hydrogen . . . 2'63        | Hydrogen . . . 6'60     |
| Potassium . . . 34'26      | Nitrogen . . . 8'42     |
| Oxygen . . . 14'01         | Oxygen . . . 9'57       |
| Sulphur . . . 28'08        | <hr/>                   |
| <hr/>                      | 100'00                  |
| 100'00                     | <hr/>                   |
| <hr/>                      |                         |
| 145. Potassium . . . 42'44 |                         |
| Iron . . . 15'19           |                         |
| Carbon . . . 19'52         |                         |
| Nitrogen . . . 22'85       |                         |
| <hr/>                      |                         |
| 100'00                     |                         |
| <hr/>                      |                         |

CALCULATIONS OF THE AMOUNT OF MATERIAL REQUIRED TO PRODUCE A GIVEN WEIGHT OF ANY SUBSTANCE, OR OF THE QUANTITY OF THE SUBSTANCE PRODUCED BY THE DECOMPOSITION OF A KNOWN WEIGHT OF MATERIAL.

149. 2'554. lbs.  
150. (a) 27'038 kilos., (b) 5'1088 kilos., (c) 16'307 kilos.,  
(d) 12'208 kilos.  
151. 33'275 grams ; 13'029 grams.  
152. 709'84 grams.  
153. 4306'0856 kilos. zinc ; 6492'3134 kilos.  $\text{H}_2\text{SO}_4$ .  
154. 3708'8 kilos. iron ; 4306'1 kilos. zinc ;  
32461'5 kilos. sulphuric acid.  
155. 177'256 grams.  
156. 12,939'8 c.c. hydrogen ; 6469'9 c.c. oxygen.  
157. 322'216 grams  $\text{Fe}_3\text{O}_4$  ; 132'029 litres of hydrogen.  
158. 0'91048 lbs. copper ; 0'1784 lbs. phosphorus.  
159. 6'096 grams ammonia ; 9'506 grams chlorine.  
160. 140'1 kilos.  $\text{KNO}_3$  ; 117'8 kilos.  $\text{NaNO}_3$ .  
161. 10'116 lbs. nitre ; 9'805 lbs. sulphuric acid.  
162. 9'08 litres.  
163. 4'246 grams.  
164. 5'477 kilos. lime ; 10'446 kilos. sal-ammoniac.  
165. 183'03 kilos. of coal.

166. Assuming air to contain 23 per cent. by weight of oxygen, 11'94 tons.

167. 42'36 grams marble ; 140'42 grams hydrochloric acid solution.

168. 146'215 tons carbon ; 3275 cubic feet.

169. (1) 130'53 litres ; (2) 130'53 litres.

170. 40'223 grams oxalic acid ; 20'559 grams formic acid ; 27'444 grams potassium ferrocyanide.

171. 36'67 grams sodium acetate.

172. 707'333 kilograms.

173. 76'395 kilos. air ; 10'73 kilos. water ;  
12'353 kilos carbon dioxide.

174. 106'99 grams silver chloride ; the solution will contain 17'79 per cent. of hydrocyanic acid.

175. 43'647 grams.

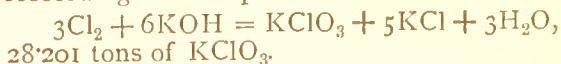
176. 16'501 tons of salt ; 20'778 tons of manganese dioxide ; 47'683 tons of sulphuric acid.

177. 51'294 tons of hydrochloric acid ;  
2,558,701 litres will escape.

178. 1'7355 grams precipitated ; 1'907 grams in solution.

179. 192'33 tons of  $\{Ca(OCl)(OH)\}_2$ ,  $CaCl_2$ .

180. According to the equation



181. 181'10 grams.

182. 72'135 grams iodine ; 100'815 grams chlorine.

183. 8'49 grams copper ; 26'29 grams sulphuric acid.

184. 54'487 tons of pyrites ; if 3 per cent. of the theoretical yield of sulphur remained unburnt, 97 tons of the dilute acid would be produced.

185. 224.28 litres.
186. 3.935 grams ferrous sulphide ; 9.325 grams air.
187. 1.802 litres.
188. 2.0488 grams microcosmic salt.
189. 82.19 tons of sulphur ; 68 tons of salt cake :  
107.742 tons of bicarbonate ; 185.398 tons of soda  
crystals ; 56.87 tons of solid caustic.
190. 17.474 tons of limestone.
191. 138.14 grams  $\text{Fe}_3\text{O}_4$  ; 289.889 grams  $\text{Fe}_2\text{Cl}_6$ .

## COMBINATION AND DECOMPOSITION OF GASEOUS BODIES.

192. 20 litres of hydrochloric acid gas ; 10 litres of  
hydrogen remain in excess.
193. 1 cubic foot of hydrobromic acid gas.
194. 50 vols. of chlorine ; 25 vols. of oxygen.
195. 154.97 c.c.
196. 3 litres of oxygen.
197. 110.34 c.c.
198. 500 c.c. nitrogen ; 1500 c.c. hydrogen.
199. V. 1.25. n vols. oxygen ; V.n vols. carbon dioxide.
200. (1) 95.42 litres ; (2) 143.13 litres ; (3) 119.27 litres.
201. 5 litres phosgene gas ; 5 litres carbon dioxide,  
weighing 9.8296 grams, and 10 litres hydrochloric acid  
gas, weighing 16.2903 grams.
202. 1 litre, on the assumption that its density is  
normal.

## GAS ANALYSIS CALCULATIONS.

203. N, 79.060 per cent. ; O, 20.940 per cent.

204. N, 83.37 per cent. ; O, 13.80 per cent. ; CO<sub>2</sub>, 2.83 per cent.

205. 3.48 per cent. of aqueous vapour.

206. 26.46 vols. of oxygen unite with 52.71 vols. of hydrogen.

207. C (hypothetical vapour volume), 1.025 ; H, 3.129 ; O, 0.484.

The empirical formula of methyl ether is C<sub>2</sub>H<sub>6</sub>O.

208. N<sub>2</sub>O.

209. N, 81.81 per cent. ; O, 14.21 per cent. ;  
CO<sub>2</sub>, 2.44 per cent. ; SO<sub>2</sub>, 1.54 per cent. ;  
H, 45.07 per cent. ; SH<sub>2</sub>, 24.25 per cent.

210. CO<sub>2</sub>, 29.96 per cent. ; N, 0.72 per cent. ;  
CO & CH<sub>4</sub>, none.

211. The percentages of N are :—*A*, 7.39 ; *B*, 16.28 ;  
*C*, 16.16 ; *D*, 15.00 ; *E*, 13.99 ; *F*, 4.48.

The volumes of gases obtained, reduced to 0 C.  
& 760 mm. are :—

|     | A.        | B.         | C.         | D.        | E.        | F.        |
|-----|-----------|------------|------------|-----------|-----------|-----------|
| N.  | 7.21 c.c. | 10.34 c.c. | 10.07 c.c. | 9.96 c.c. | 9.66 c.c. | 4.48 c.c. |
| NO. | 0.47 "    | 0.91 "     | 1.16 "     | 0.55 "    | 0.25 "    | 0.03 "    |

212. Total oxygen added = 239.3, of which 236.98 is used. Carbon dioxide formed = 118.8 = oxygen used in burning C. Hence O used to burn H = 118.18.

∴ Vol. of H would be 236.36 and hypothetical vol. of C.  $\frac{118.8}{2} = 59.4$ .

Hence composition of marsh gas is represented by CH<sub>4</sub>.

213. 0.53 per cent. by volume.

214. 0.47 per cent. by volume.

215. The percentage composition of this sample of coal-gas is :—

|                            |        |               |         |
|----------------------------|--------|---------------|---------|
| $\text{CO}_2$              | 1.41 ; | $\text{CO}$   | 6.15 ;  |
| $\text{C}_2\text{H}_4$ &c. | 3.84 ; | $\text{H}_2$  | 47.73 ; |
| $\text{C}_6\text{H}_6$     | 1.04 ; | $\text{CH}_4$ | 35.63 ; |
| $\text{O}$                 | 0.30 ; | $\text{N}$    | 3.90.   |

216. 3 vols. ethylene ; 1.98 vols. butylene. Equal in illuminating power to a gas containing 6.96 per cent. of ethylene.

## ATOMIC WEIGHT DETERMINATIONS.

217. 1.00108.

|                                       |        |                |
|---------------------------------------|--------|----------------|
| 218. From synthesis of silver nitrate | 13.967 | Mean<br>13.979 |
| By precipitation with potassium       |        |                |
| chloride                              | 14.026 |                |
| By precipitation with ammonium        |        |                |
| chloride                              | 13.945 |                |

219. 35.356.

220. 39.033.

221. 199.6.

222. (1) 12.014, (2) 12.014, (3) 12.030. Mean = 12.019.

223. 27.029.

224. 27.028.

225. 27.012.

226. 48.06 ; 48.07 ; 47.98 ; 48.04 ; 48.04.

227. 196.88 ; 196.90 ; 196.86 ; 196.85 ;  
196.89 ; 196.86 ; 196.85 ; 196.89.

228. 28.347 ; 28.303 ; 28.347 ; 28.352 ; 28.243.

229. 52.061.

230. 65.506.

## INDIRECT ANALYSIS.

231. 33.51.

232. 93.03.

233. 39.98.

234. 11.61.

235. 25.51.

236. 58.035 grams.

237. K, 13.75 per cent. ; Na, 8.25 per cent.

238. 0.6281 gram NaCl ; and 0.3049 gram Na I.

## GENERAL ANALYTICAL QUESTIONS.

239. (a) 0.1998 gram of the salt gave 0.4865 gram silver chloride, and 0.0032 reduced silver.

$$0.0032 \text{ gm. Ag} = 0.00425 \text{ Ag Cl ;}$$

$$0.4865 + 0.00425 = 0.49075 \text{ gm. Ag Cl ;}$$

$$\frac{0.49075 \times 35.37 \times 100}{143.03 \times 0.1998} = 60.74 \text{ per cent. chlorine.}$$

(b) 0.9543 gram of the salt gave 1.1584 gram sodium sulphate.

$$\frac{1.1584 \times 45.99}{141.81} = 0.37568 ;$$

$$\text{and } \frac{0.37568 \times 100}{0.9543} = 39.36 \text{ per cent. sodium.}$$

$\frac{60.74}{35.37} = 1.7 ; \frac{39.36}{23} = 1.7$  : hence the chlorine and sodium in the compound are in the ratio of atom to atom, and the formula of the salt is Na Cl.



240. 0.3951 gram of substance gave 0.6544 gram of  $\text{NH}_4\text{MgAsO}_4$ ,  $\text{H}_2\text{O} = 0.3781$  gram  $\text{As}_2\text{O}_5$ : hence the substance contained 95.70 per cent. arsenic anhydride.

241. The percentage results of the analysis are :—

|                        |        |
|------------------------|--------|
| Silica . . . . .       | 40.35  |
| Ferric oxide . . . . . | 36.43  |
| Water . . . . .        | 20.62  |
| Lime . . . . .         | 2.68   |
|                        | <hr/>  |
|                        | 100.08 |
|                        | <hr/>  |

Neglecting the lime as an unessential constituent, the percentage composition of the mineral becomes :—

|                        |        |
|------------------------|--------|
| Silica . . . . .       | 41.46  |
| Ferric oxide . . . . . | 37.43  |
| Water . . . . .        | 21.19  |
|                        | <hr/>  |
|                        | 100.08 |
|                        | <hr/>  |

The simplest ratios of the oxygen contained in each of the constituents is 6 : 3 : 5. Hence the formula of the compound is  $3 \text{SiO}_2$ ,  $\text{Fe}_2\text{O}_3$ ,  $5 \text{H}_2\text{O}$ .

242. 164.1 grams of  $\text{K}_2\text{PtCl}_6$  are equivalent to 50.39 grams of potassium chloride. Hence the composition of the mixture is :—

|                              |        |
|------------------------------|--------|
| Potassium chloride . . . . . | 50.39  |
| Sodium chloride . . . . .    | 49.61  |
|                              | <hr/>  |
|                              | 100.00 |
|                              | <hr/>  |

243. 0.2476 gram  $\text{Tl}_2\text{PtCl}_6 = 0.1239$  grams thallium, or 67.67 per cent. Its composition is therefore :—

|                           |        |
|---------------------------|--------|
| Tl. . . . .               | 67.67  |
| $\text{Cl O}_4$ . . . . . | 32.33  |
|                           | <hr/>  |
|                           | 100.00 |
|                           | <hr/>  |

$$\frac{67.67}{203.7} = 0.332. \quad \frac{32.33}{99.21} = 0.325.$$

Hence the formula is  $\text{TiClO}_4$ .

244. Centesimal hydrochloric acid corresponds to 1.0766 grams of Ag per litre, hence Ag used =  $7.383 - 0.0032298$  grams = 7.37977 grams; and  $\frac{7.37977 \times 35.37 \times 100}{107.66 \times 3.949} = 61.40$  per cent. chlorine.

245.  $2 \text{BaSO}_4 = \text{O}$ .  $\text{AgBr} = \text{Br}$ .

0.402 gram  $\text{BaSO}_4 = 0.01378 \text{ O}$ .

0.324 gram Ag Br = 0.1372 Br.

$$\frac{0.01378}{15.96} = 0.00086. \quad \frac{0.1372}{79.76} = 0.00172.$$

Hence the formula is  $\text{Br}_2 \text{O}$ .

246.  $\text{KClO}_4 = \text{HClO}_4$ . 1.6785  $\text{KClO}_4 = 1.2167 \text{ HClO}_4$  or 99.85 per cent.  $\text{HClO}_4$ .

0.966 gm. lost 0.444 gm. O, or 45.97 per cent.:  $\text{KClO}_4$  ought to lose 46.18 per cent.

0.966 - 0.444 = 0.522 KCl; this required 0.744 gram of silver for precipitation: theory requires 0.7523 gram.

247.  $\text{NaHCO}_3 + \text{CH}_3 \cdot \text{COOH} = \text{CH}_3 \cdot \text{COONa} + \text{CO}_2 + \text{H}_2\text{O}$  or 43.89 parts of  $\text{CO}_2 = 59.86$  parts of  $\text{CH}_3 \cdot \text{COOH}$ . Then 0.427  $\text{CO}_2 = 0.5823 \text{ CH}_3 \cdot \text{COOH}$ ,

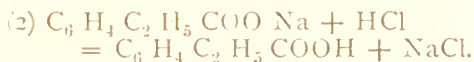
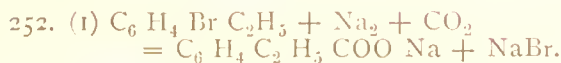
$$\text{and } \frac{0.5823 \times 100}{1.483} = 39.26 \text{ per cent.}$$

248.  $\text{NaOH} = \text{HCOOH}$ . Then 1.01558  $\text{NaOH} = 1.1664 \text{ HCOOH}$  and  $\frac{1.1664 \times 100}{2.122} = 54.967$  per cent.

249. 2.921 vols.  $\text{CO}_2$  in 10,000 vols. of air.

|                                |          |
|--------------------------------|----------|
| 250. Sodium chloride . . . . . | 26.402.  |
| Potassium chloride . . . . .   | 0.7459.  |
| Magnesium chloride . . . . .   | 3.0368.  |
| Magnesium bromide . . . . .    | 0.0705.  |
| Magnesium sulphate . . . . .   | 2.0648.  |
| Calcium sulphate . . . . .     | 1.2896.  |
| Calcium carbonate . . . . .    | 0.0475.  |
| Ammonium chloride . . . . .    | 0.00035. |
| Magnesium nitrate . . . . .    | 0.00185. |
| Ferrous carbonate . . . . .    | 0.00674. |
| MgO unaccounted for . . . . .  | 0.02904. |

251. 22.53 candle power.



and the acid gave on treating with baryta water the barium compound, of which 0.5637 gram lost 0.0430 gram water, or 7.63 per cent.; and gave 0.2733 gram barium sulphate, or 28.517 per cent. Ba. Hence the composition of the salt is :—

|  |        |
|--|--------|
| $\text{C}_9 \text{H}_9 \text{O}_2$ . . . . . | 63.85  |
| Ba. . . . .                                  | 28.52  |
| $\text{H}_2 \text{O}$ . . . . .              | 7.63   |
|  | <hr/>  |
|  | 100.00 |
|  | <hr/>  |

$$\frac{63.85}{148.65} = 0.429; \quad \frac{28.52}{136.86} = 0.209; \quad \frac{7.63}{17.96} = 0.425.$$

Hence formula is  $\text{Ba} (\text{C}_9 \text{H}_9 \text{O}_2)_2, 2 \text{H}_2 \text{O}$ .

253. 1.994 per cent. nitrogen.

254. The composition of the body, as determined by experiment, is :—

|                    |       |
|--------------------|-------|
| Carbon . . . . .   | 36.43 |
| Hydrogen . . . . . | 7.91  |
| Chlorine. . . . .  | 55.66 |

The simplest relation between these numbers is represented by  $C_2 H_5 Cl_x$  which formula requires :—

|                    |       |
|--------------------|-------|
| Carbon . . . . .   | 37.22 |
| Hydrogen . . . . . | 7.77  |
| Chlorine. . . . .  | 55.01 |

The vapour density found is 32.44, calculated 32.15.

255. NaCl. 66.39 per cent.  
KCl. 33.61 per cent.

256. NaCl. 60.3 per cent.  
NaBr. 39.7 per cent.

### SOLUTION OF GASES.

257. 20 c.c. ; 14.96 c.c. ; 7.82 c.c. ; 0.286 c.c.

258. The volume is the same in each case, 15.90 c.c.  
The weights are respectively :—

|                  |                 |
|------------------|-----------------|
| 0.025124 gram ;  | 0.018792 gram ; |
| 0.0098237 gram ; | 0.0003593 gram. |

| 259. (A)         | (B)          | (C)        |
|------------------|--------------|------------|
| (a) 6.664 c.c. ; | 6.553 c.c. ; | 6.454 c.c. |
| (b) 6.344 c.c. ; | 6.291 c.c. ; | 5.832 c.c. |

260. 1.4584 ; 1.2607 ; 1.0385 ;  
0.9610 ; 0.9134 ; 0.8852.

261. 0.06910 ; 0.06853 ; 0.06769 ; 0.06732 ; 0.06669.  
Water : 0.02134 ; 0.02099 ; 0.01956 ; 0.01912 ;  
0.01839.

262.  $0.032874 - 0.00081632 t + 0.000016421 t^2$ .

263. 39.36 per cent. O. and 60.64 per cent. N.

264. By volume :—44.7 per cent.  $CO_2$  ;  
55.3 per cent. N.

265. 92.07 per cent. H. ;  
7.93 per cent.  $CO_2$ .

# MOLECULAR WEIGHT AND LOWERING OF THE FREEZING-POINT.

266.  $15.34^{\circ}\text{C.}$

267.  $73.44^{\circ}$ .

268.  $0.5256^{\circ}$ .

269.  $1.69$  per cent.

270.  $2.867^{\circ}$  ;  $2.488^{\circ}$  ;  $1.482^{\circ}$ .

271. (1)  $72.58$  ; (2)  $73.50$  ; (3)  $71.97$  ; (4)  $73.60$ .

272. (a)  $111.87$  ; (b) for Na,  $14.49$  ; (c) for Sn,  $73.93$ .

273.  $\text{MgSO}_4, 7 \text{ H}_2\text{O}$ .

274.  $L = \frac{0.02 \cdot (280.9)^2}{117.9} = 13.38$ .

275.  $\frac{18.5}{.63} = 29$  ;  $\frac{27.7}{.63} = 44$  ;  $\frac{38.6}{.63} = 61$  ; the numbers

here obtained according to Raoult should represent the molecular weight of the solvent in each case ; in the cases of formic and acetic acids this holds very nearly but in the case of water 29 bears no simple relation to 18 the molecular weight of water in the gaseous state, the conclusion may therefore be drawn that the molecule of water in the liquid state is more complex than the molecules of formic and acetic acids under similar conditions.

276. From (a) the molecular weight deduced is  $65.80$ , from (b)  $65.99$  ; for  $\text{N}_2\text{O}_4$  molecular weight is  $92$ , for  $\text{NO}_2$  it is  $46$  ; hence it is probable that at the temperature of the experiment nitrogen tetroxide consists of a mixture of  $\text{N}_2\text{O}_4$  and  $\text{NO}_2$ .

277. (a)  $196.2$  ; (b)  $196.5$ .

# SPECIFIC HEAT, LATENT HEAT, AND ATOMIC HEAT.

279.  $18^{\circ}$  C.                      280. 0.0327.                      281. 0.03308.
282. 0.0335.                      283. 0.208.                      284.  $3^{\circ}$ 08.
285.  $893^{\circ}$  C.                      286. 0.1137.                      287. 774.6 for  $1^{\circ}$  F.
288. 33681 metres.                      289. Sp. Ht. of Indium is  
0.0574.
290. (A) 0.0559 ; (B) 0.0935 ; (C) 0.0495 ;  
(D) 0.0548 ; (E) 0.1712.
291.  $28.4^{\circ}$  C.                      292. 7.284 kilos. per hour.
293. 537.2.
294. Pb 6.48 ; Ag 6.13 ; Cu 6.01 ;  
Fe 6.36 ; S 6.48 ; P 5.84.
295. Approximate atomic weights :—Ag, 112.3 ;  
Zn, 66.98 ; Bi, 207.5 ; Sn, 113.8 ; Fe, 56.23.  
Exact atomic weights :—Ag, 107.66.  
Zn 64.88 ; Bi, 207.5 ; Sn, 117.35 ; Fe, 55.88.
296. 5.67 = atomic heat of solid chlorine.  
2.98 and 3.06 are the atomic heats for O calcu-  
lated from the respective oxides.
297. 3.8.
298. 2.
299. Ca 5.6 ; Sr, 6.3 ; Ba 6.4.

## HEAT OF SOLUTION AND COMBINATION.

300. 34.462 kilos.

301. 5.747° C.

302. 0.148 kilos.

303. (1) ethylene 2714.5°; (2) methane 2381.3°.

304. 2677.6°.

305. 7,614 thermal units.

306. 8095.6.

307. 3386.4 metres.

308. 192,700 +.

309. 20,200 +.

310. 28,400 -.

311. 18,500 -.

312. 13,080 -.

313. (a) 55,100 +; 45,200 -.

314. 5,590 -.

315. 21,150 +.

316. It may be concluded that  $\text{H}_3\text{PO}_3$  is a dibasic acid, for the addition of sodic hydrate beyond two equivalents causes but a very slight liberation of heat, and from nothing to two equivalents the heat evolved is considerable and proportional (or nearly so) to the amount of sodic hydrate added.



RICHARD CLAY AND SONS, LIMITED,  
BREAD STREET HILL, E.C., AND  
BUNGAY, SUFFOLK.



MACMILLAN AND CO.'S BOOKS  
FOR  
**STUDENTS OF CHEMISTRY.**

ESSAYS IN HISTORICAL CHEMISTRY. By T. E. THORPE, C.B., LL.D., F.R.S. Second Edition, enlarged. 8vo, 12s. net.

CHEMISTRY OF THE PROTEIDS. By Dr. GUSTAV MANN. Based on Professor COHNHEIM'S "Chemie der Eiweiss Körper." 8vo, 15s. net.

INTRODUCTION TO PHYSICAL CHEMISTRY. By JAMES WALKER, D.Sc., Ph.D. Fourth Edition. 8vo, 10s. net.

OUTLINES OF INDUSTRIAL CHEMISTRY. A Text-Book for Students. By FRANK HALL THORP, Ph.D. 8vo, 15s. net.

GASES OF THE ATMOSPHERE: The History of their Discovery. By Sir W. RAMSAY. Third Edition. Ex. crown 8vo, 6s. net.

HISTORY OF CHEMISTRY FROM THE EARLIEST TIMES TO THE PRESENT DAY. By ERNST VON MEYER, Ph.D. Third Edition. Translated by GEORGE MCGOWAN, Ph.D. 8vo, 17s. net.

THEORETICAL CHEMISTRY FROM THE STAND-POINT of AVOGADRO'S RULE & THERMO-DYNAMICS. By Professor NERNST. Translated by Professor CHARLES SKEELE PALMER, of the University of Colorado. Re-edited and Revised in accordance with the Fourth German Edition, by Dr. R. A. LEHFELDT. 8vo, 15s. net.

A MANUAL OF MICROCHEMICAL ANALYSIS. By Professor H. BEHRENS With an Introductory Chapter by Professor J. W. JUDD, F.R.S. 6s.

A TEXT-BOOK OF THE PHYSIOLOGICAL CHEMISTRY OF THE ANIMAL BODY, including an Account of the Chemical Changes occurring in Disease. By ARTHUR GAMGEE, M.D., F.R.S. Vol. II. 8vo, 18s.

THE CHEMICAL BASIS OF THE ANIMAL BODY. An Appendix to Foster's "Text-Book of Physiology." By A. SHERIDAN LEA, M.A., D.Sc., F.R.S. 8vo, 7s. 6d.

CHEMICAL TECHNOLOGY AND ANALYSIS OF OILS, FATS, AND WAXES. By Dr. J. LEWKOWITSCH, F.C.S., Examiner in Soap Manufacture and in Fats and Oils to the City and Guilds of London Institute. Third Edition entirely re-written and enlarged. In 2 Vols. With 88 Illustrations and numerous Tables. Medium 8vo, 36s. net.

MACMILLAN AND CO., LTD., LONDON.

MACMILLAN AND CO.'S BOOKS  
FOR  
**STUDENTS OF CHEMISTRY.**

---

**A TREATISE ON CHEMISTRY.** By Sir H. E. ROSCOE, F.R.S., and the late C. SCHORLEMMER, F.R.S. 8vo. Vol. I. The Non-Metallic Elements. New Edition. Completely revised by Sir H. E. ROSCOE, assisted by Drs. H. G. COLMAN and A. HARDEN. With 374 Illustrations and a Portrait of Dalton engraved by C. H. JENNS. 21s. net. Vol. II. Metals. 31s. 6d. Vol. III. Organic Chemistry. Parts II., IV., and VI., 21s. each. Part III., 18s.

**THE PRACTICAL METHODS OF ORGANIC CHEMISTRY.** By LUDWIG GATTERMANN, Ph.D. Authorised Translation by WILLIAM B. SHOBER, Ph.D. With numerous Illustrations. Globe 8vo, 8s. 6d.

**A LABORATORY MANUAL OF ORGANIC CHEMISTRY:** a Compendium of Laboratory Methods for the use of Chemists, Physicians, and Pharmacists. By Dr. LASSAR-COHN. Translated from the Second German Edition by ALEXANDER SMITH, B.Sc., Ph.D. Crown 8vo, 8s. 6d.

**PRINCIPLES OF INORGANIC CHEMISTRY.** By Professor W. OSTWALD. Translated by A. FINDLAY. Second Edition 8vo, 18s. net.

**THE SCIENTIFIC FOUNDATIONS OF ANALYTICAL CHEMISTRY TREATED IN AN ELEMENTARY MANNER.** By WILHELM OSTWALD, Ph.D. Translated by GEORGE MCGOWAN, Ph.D. Crown 8vo, 6s. net.

**MANUAL OF PHYSICO-CHEMICAL MEASUREMENTS.** By Professor W. OSTWALD. Translated by JAMES WALKER, D.Sc. Ph.D. Illustrated. 8vo, 7s. net.

**ANALYTICAL CHEMISTRY.** By A. MENSCHUTKIN. Translated from the Third German Edition, under the supervision of the Author, by JAMES LOCKE. Medium 8vo, 17s. net.

**QUALITATIVE CHEMICAL ANALYSIS OF INORGANIC SUBSTANCES.** By A. A. NOYES. 8vo, 5s. net.

**A DICTIONARY OF CHEMICAL SOLUBILITIES, INORGANIC.** By ARTHUR MESSENGER COMEY, Ph.D. Demy 8vo, 15s. net.

**A NEW VIEW OF THE ORIGIN OF DALTON'S ATOMIC THEORY.** A Contribution to Chemical History. Together with Letters and Documents concerning the Life and Labours of John Dalton, now for the first time published from manuscript in the possession of the Literary and Philosophical Society of Manchester. By Sir HENRY E. ROSCOE, F.R.S., and ARTHUR HARDEN. With Portrait. Six page plates. 8vo, 6s. net.

MACMILLAN AND CO., LTD., LONDON.

MACMILLAN AND CO.'S BOOKS  
FOR  
**STUDENTS OF CHEMISTRY.**

- A PRIMER OF CHEMISTRY. By Sir H. E. ROSCOE, F.R.S. Illustrated. Pott 8vo, 1s.
- ELEMENTARY PHYSICS AND CHEMISTRY. By R. A. GREGORY and A. T. SIMMONS, B.Sc. (Lond.). First, Second, and Third Stages. Globe 8vo, 1s. 6d. each.
- INTRODUCTORY CHEMISTRY FOR INTERMEDIATE SCHOOLS. By LIONEL M. JONES, B.Sc. Globe 8vo, 2s.
- INTRODUCTION TO THE STUDY OF CHEMISTRY. By W. H. PERKIN, Jr., Ph.D., F.R.S., and BEVAN LEAN, D.Sc. Globe 8vo, 2s. 6d.
- INTRODUCTION TO CHEMISTRY AND PHYSICS. By W. H. PERKIN, Jr., Ph.D., F.R.S., and BEVAN LEAN, D.Sc. 2 vols. Globe 8vo, 2s. each.
- THE ELEMENTS OF CHEMISTRY. By IRA REMSEN, Professor of Chemistry in the Johns Hopkins University. Fcap. 8vo, 2s. 6d.
- INORGANIC CHEMISTRY FOR BEGINNERS. By Sir HENRY E. ROSCOE, F.R.S., and J. LUNT, B.Sc. Globe 8vo, 2s. 6d.
- LESSONS IN ELEMENTARY CHEMISTRY, INORGANIC AND ORGANIC. By Sir H. E. ROSCOE, F.R.S. Fcap. 8vo, 4s. 6d.
- INORGANIC CHEMISTRY FOR ADVANCED STUDENTS. By Sir H. E. ROSCOE, F.R.S., and ARTHUR HARDEN, Ph.D. Adapted to the Advanced Stage of the South Kensington Syllabus. Globe 8vo, 4s. 6d.
- AN INTRODUCTION TO THE STUDY OF CHEMISTRY (INORGANIC CHEMISTRY). By IRA REMSEN. Crown 8vo, 6s. 6d.
- ELEMENTS OF INORGANIC CHEMISTRY. By Prof. H. C. JONES. Crown 8vo, 6s. 6d.
- OUTLINES OF INORGANIC CHEMISTRY. By Prof. F. A. GOOCH and C. F. WALKER. Ex. crown 8vo, 7s. 6d. net.
- COLLEGE TEXT-BOOK OF CHEMISTRY. By IRA REMSEN. Ex. crown 8vo, 8s. 6d. net.
- EXPERIMENTAL PROOFS OF CHEMICAL THEORY FOR BEGINNERS. By Sir WILLIAM RAMSAY, Ph.D., Professor of Chemistry in University College, London. Pott 8vo, 2s. 6d.

MACMILLAN AND CO., LTD., LONDON.

MACMILLAN AND CO.'S BOOKS  
FOR  
**STUDENTS OF CHEMISTRY.**

---

- CHEMICAL THEORY FOR BEGINNERS.** By LEONARD DOBBIN, Ph.D., and JAMES WALKER, Ph.D., D.Sc., Professor of Chemistry in University College, Dundee. Pott 8vo, 2s. 6d.
- CHEMISTRY FOR ORGANISED SCHOOLS OF SCIENCE.** By S. PARRISH, B.Sc. With Introduction by D. FORSYTH, D.Sc. Globe 8vo, 2s. 6d.
- PRACTICAL INORGANIC CHEMISTRY.** By G. S. TURPIN, M.A. Globe 8vo, 2s. 6d.
- JUNIOR COURSE OF PRACTICAL CHEMISTRY.** By FRANCIS JONES, F.R.S.E. With a Preface by Sir HENRY E. ROSCOE, F.R.S. Illustrated. Globe 8vo, 2s. 6d.
- PRACTICAL INORGANIC CHEMISTRY FOR ADVANCED STUDENTS.** By CHAPMAN JONES, F.I.C., F.C.S. Globe 8vo, 2s. 6d.
- ELEMENTS OF QUANTITATIVE ANALYSIS.** By G. H. BAILEY, D.Sc. Globe 8vo, 4s. 6d.
- INORGANIC CHEMICAL PREPARATIONS.** By FELIX LENGFELD, Assistant Professor of Inorganic Chemistry in the University of Chicago. Globe 8vo, 2s. 6d. net.
- PRACTICAL CHEMISTRY.** By R. ABEGG and W. HERZ, Professor and Demonstrator of Analytical Chemistry at Breslau University. Translated by H. T. CALVERT, B.Sc. Crown 8vo, 6s. (Table of Ions sold separately, 1s. per dozen).
- LESSONS IN ORGANIC CHEMISTRY.** By G. S. TURPIN, D.Sc. Globe 8vo, 2s. 6d.
- PRACTICAL ORGANIC CHEMISTRY for ADVANCED STUDENTS.** By JULIUS B. COHEN. Globe 8vo, 3s. 6d.
- THEORETICAL ORGANIC CHEMISTRY.** By JULIUS B. COHEN, Ph.D. Globe 8vo, 6s.
- COMPOUNDS OF CARBON ; or, An Introduction to the Study of Organic Chemistry.** By IRA REMSEN. Crown 8vo, 6s. 6d.
- CHEMICAL ARITHMETIC.** With 1,200 Problems. By SYDNEY LUPTON, M.A. Fcap. 8vo, 4s. 6d.
- EXPERIMENTS FOR CHEMICAL LECTURES.** By F. G. BENEDICT, Ph.D. Crown 8vo, 8s. 6d. net.
- SCIENCE OF COMMON LIFE (Experimental Hygiene).** By A. T. SIMMONS, B.Sc., and E. STENHOUSE, B.Sc. Globe 8vo, 2s. 6d.

MACMILLAN AND CO., LTD., LONDON.









